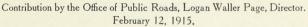
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USDEPARTMENT OF AGRICULTURE

No. 136



HIGHWAY BONDS:

A COMPILATION OF DATA AND AN ANALYSIS OF ECONOMIC FEATURES AFFECTING CONSTRUCTION AND MAINTENANCE OF HIGHWAYS FINANCED BY BOND ISSUES, AND THE THEORY OF HIGHWAY BOND CALCULATIONS.

BY

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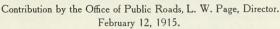
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INTRODUCTION.

The practice of issuing bonds for highway and bridge construction by counties and their subdivisions has become common. In 1,230 counties, or 41.1 per cent of all the counties in this country, there were outstanding highway bonds on January 1, 1914. The total amount of such bonds voted, as ascertained by the Office of Public Roads up to that date, was \$286,557,073, of which township bonds alone amounted to \$57,153,718. The amount of outstanding local highway bonds on January 1, 1913, was approximately \$202,007,776. This amount was increased during the year 1913 by current issues noted below, but was also slightly decreased by maturing payments.

The county highway bond is essentially a municipal bond; that is, a bond issued by a public corporation. Statistics indicate that all municipal bonds constitute about 20 per cent of the total of all bonds issued, while Government bonds are about 10 per cent. Municipal bonds are regarded as excellent investments and are frequently used by banks as a second reserve. The amount of highway bonds issued is indicated by comparison with the \$79,741,688 of irrigation and drainage bonds authorized in the interval from 1907 to 1912, inclusive.

^{1 &}quot;Voted" is almost equivalent to "issued," except in State highway bonds. The difference between bonds voted and bonds sold in 1912 was a little over 3 per cent.

The progress of the local highway-bond movement is further indicated by the diagram of first issues for the interval 1900–1913. Dates of first issues were reported, however, for only 579 counties. First issues for 1912 and 1913 are practically complete. (Pl. I, fig. 1.)

During the past three years county, district, and township highway and bridge bonds were voted as follows: 1911, \$29,200,022; 1912, \$32,022,703; 1913, \$50,445,756; making a total of \$111,668,481.

There have also been voted State highway bonds which now total \$158,590,000.¹ The grand total of all highway bonds voted and reported to the Office of Public Roads to January 1, 1914, is, therefore, \$445,147,073.

There is given in Appendix A of this publication a list of all the State highway bonds with their dates of issue, terms, and nominal interest rates, together with other pertinent information concerning the issues.

In Appendix B are given three lists of local highway and bridge bonds. First there is a list of county and district highway and bridge bonds voted to January 1, 1914, with their terms and interest rates where reported. A similar table of township bonds is next presented. In a separate table is a list, by counties, districts, and townships in the several States, of highway and bridge bonds reported voted during each of the years 1912 and 1913.

The approximate distribution of local highway bonds is shown in the map, Plate II, by counties. State highway bonds are not included.

In collecting data for this publication the Office of Public Roads corresponded directly with county and township officials and the tables of bonds were submitted to State highway officials and other State officials for corrections and additions. Many county officials failed to state the term of the highway bond issues; it was found, however, that the mean term for approximately \$47,000,000 issued prior to 1913 was 24.8 years. For the years 1912 and 1913, the term of issue, the number of issues, and the total amount issued by municipalities with complete reports are presented in the following table:

Table 1.—Bond issues during 1912 and 1913 in counties, districts, and townships, with complete returns.

Total number of issues.	Terms of issues.	Total amounts of issues.
17	5-year	\$442, 175
100	10-year	5, 165, 383
13	15-year	1, 266, 500
68	20-year	8, 906, 538
31	25-year	5, 518, 150
45	30-year	7, 399, 000
129	Serials	15, 300, 819
47	Above 30-year	7, 170, 971
47	Other term	1, 816, 541

¹ Including \$3,415,000 issued by Connecticut, Massachusetts, and New Hampshire in 1913. Massachusetts authorized, in 1912, \$5,000,000 to be issued during the years 1913 to 1917, inclusive, which is part of the total given. New York's second \$50,000,000 will probably not be entirely issued for several years.

These figures represent 61.2 per cent of all the counties, townships, and districts reporting bond issues during 1912 and 1913.

The reports on the mileage of road constructed from the proceeds of local bond issues are very incomplete and in many instances contradictory. After eliminating all reports which were obviously incorrect or defective, a list of counties and districts giving complete returns of classified mileage of roads constructed has been made. A similar list for township work has also been made. These two lists are presented in Appendix B. It is quite probable that omissions in reports from counties and their subdivisions concerning mileage built are due in part to the frequent changing of local officials.

It will be seen from the diagram of first issues (Pl. I, fig. 1) and from the fact that probably over 80 per cent of local bonds for highways and bridges are still outstanding (see p. 3), that the highway bond movement has yet to meet the test of repayment. The maximum outlay for retirement of outstanding highway loans will apparently be reached in about 20 years.

If highway bond issues are to continue successfully, certain fundamental principles require attention. They are, therefore, discussed briefly in this publication. Necessary information is presented in considerable detail with illustrations and tables to guide highway officials in borrowing and expending highway funds.

COUNTY HIGHWAYS.

The highways of a county may usually be classified into main market roads, intercounty roads, and neighborhood roads. A relatively large percentage of the total mileage—more than 80 per cent in many counties—may be classed as neighborhood roads, which are either feeders to market roads or crossroads of relatively small importance. The intercounty roads are usually in part also main market roads. The market roads are, therefore, the roads for which the question of borrowing money frequently arises. The total mileage of main market roads varies greatly from county to county, but usually does not exceed 150 miles.

The distribution and individual lengths of market roads is of much importance to the highway engineer, who must plan for improvements. Rules can not be laid down which will apply universally for the selection of such roads. The area served by a given market road depends upon the length of the road and the form of the road network, which, in turn, is largely governed by topography and the situation of shipping points. In regions where the public land survey system prevails the roads very generally follow the section lines and radial roads are not common.

It is usual to find from four to eight main market roads radiating from market centers. The average number of such roads of considerable length is about six for each shipping point. The traffic on radial roads will tend to vary inversely with their number. Plates IV, VI, and IX show the distribution of the main market roads in three counties.

ECONOMIC VALUE OF THE MARKET ROAD.

The service rendered by highways radiating from a town may be measured directly by the tonnage which is hauled over them; and their economic importance is indicated by this tonnage and varies directly with it. There are two ways of computing the tonnage of traffic on a road: (a) By actual count, and (b) by determining traffic areas supplemented with producers' and merchants' estimates of tonnage.

The actual count of traffic determines the average number of teams hauling produce each day, their loads, and the average distance traveled. From the count on a sufficient number of days a close estimate of the average annual traffic may be had.

Table 2.—Traffic record of seven unimproved roads.

Road No.	Location.1	Length in miles.	Tons per day, each area.	Average haul (nearest mile).	Equiva- lent annual ton-miles.	Mer- chants' and pro- ducers' estimates (ton- miles).	Traffic area (acres).	Reported costs (cents per ton- mile).
1	Lauderdale County,	28.3	58	10	367,894	228, 046	154, 432	16.0
3	Boone and Story Counties, Iowa (16) Cumberland and Sa-	45.1	10	2	162,342	105, 662	113, 521	37.2
	gadahoc Counties, Me. (8)	32.1	18	4	227,451		38,182	23. 6
4	Leflore County, Miss.	24.1	33	7	197,386	90,628	60,736	36. 2
5	Montgomery County, Md. (1)	5. 4	21	2	14,044	5,892	12,531	26.0
6	Muskingum County, Ohio (2)	20.9	28	6	111,026	132, 711	41,952	28.0
7	Jackson County, Oreg.	50. 5	11	4	51, 810	32,170	73, 881	36.6
	Totals and averages	206. 4	26	5	1,131,953		495, 235	29.1

¹ Numbers in parentheses indicate the number of traffic areas.

From a map, supplemented by field observations, the traffic area served by a highway may be determined. This is the area on which originates market produce and for which supplies must be hauled from market. In a wheat country, for example, the average annual wheat acreage tributary to a highway will determine approximately the principal market traffic. Even a rough estimate of the traffic area is valuable for determining the relative importance of highways and indicates the order in which their improvement should be undertaken. It is also an excellent check on traffic count. Traffic data for a number of roads recently investigated by the

Office of Public Roads are given in Table 2. Actual traffic count was made four times for seven consecutive days on all the roads. The traffic areas, traffic estimates, and the hauling-cost data were determined in the field. The weight derived from loaded teams and motor trucks only is entered in this table, and the ton-mile hauling costs include a slight increment for loading and unloading.

Highway improvement with borrowed money must be regarded as an investment. The only way, however, that a measurable income arises from the investment is by the reduction of hauling costs. From the standpoint of public economy the annual cost of hauling represents the operating expenses of the road system. The direct return upon the highway investment, then, is the reduction in operating expenses. This difference between the old hauling costs and the hauling costs over the improved roads is a real saving to the community. In the language of railroad bookkeeping, this difference is an operating income to the community. It is invariably true that the improvement of market roads is followed by an increase in annual tonnage, so that estimates based on the existing tonnage are usually conservative. Doubtless much more money can be spent for well-planned and well-built roads without overcapitalizing them.

The unit in which hauling costs are measured is the ton-mile. The cost of hauling a ton 1 mile on a poor road probably varies on an average from 20 to 35 cents. (See Table 2.) It depends on the condition of the road and changes greatly during the year. Recent figures for hauling over unimproved roads in the mountain regions of West Virginia and Kentucky also show seven instances where the cost per ton-mile varied from 23 to 37 cents. Ton-mile costs as low as 10 cents are common in Europe on first-class highways. Even with the extreme variations of wages it is doubtful if the cost per ton-mile anywhere in this country on an adequately improved road exceeds 15 cents. Cross ties were hauled over improved gravel roads in Spotsylvania County, Va., in April, 1913, for about 12.7 cents and less per ton-mile, and apples were hauled by motor trucks on good roads in Jackson County, Oreg., in October, 1913, for a little more than 11 cents a ton-mile.

To understand how many tons a highway can carry in a year, assume a market town from which radiate six roads uniformly distributed and 12 miles long. There is then a circular traffic area of 12 miles radius and each road serves theoretically one-sixth of this area, which is 75.4 square miles. The average haul for each separate road is about 8 miles. (See p. 8.) If each acre tributary to this road supplies only 200 pounds of produce, which must move to market an average distance of 8 miles, the road carries an annual traffic of at least 38,605 ton-miles. Another way to view this traffic

is to divide the total number of tons by the number of hauling days, which is usually taken at 300. With an acreage yield of 200 pounds there result 16 tons per day which may be assumed to move an average distance of 8 miles. This would make a total of 128 ton-miles daily. The daily average weight over the entire road is therefore about 10.7 tons. The tonnage hauled is the most direct and reliable basis from which to determine the economic value of a road. (See Table 2.)

It is common to find that when a poor market road is improved the cost of hauling is reduced by from 2 to 10 cents per ton-mile. The saving to the community during a year can then be readily computed for each mile. (See Pl. III, fig. 2.)

Table 3 shows the annual saving per mile and the capitalized amount of this annual saving at 5 per cent interest for daily traffic varying from 5 to 80 tons.

Table 3.—Annual saving per mile in hauling costs at 5 cents per ton-mile reduction.

Tons per day.	Total saved in year of 300 days.	Capital- ized at 5 per cent.	Tons per day.	Total saved in year of 300 days.	Capital- ized at 5 per cent.
5	\$75	\$1,500	45	\$675	\$13,500
10	150	3,000	50	750	15,000
15	225	4,500	55	825	16,500
20	300	6,000	60	900	18,000
25	375	7,500	65	975	19,500
30	450	9,000	70	1,050	21,000
35	525	10,500	75	1,125	22,500
40	600	12,000	80	1,200	24,000

If the roads do not radiate uniformly from a town it is evident that in a uniformly producing area the traffic lost to one road must go over some adjoining road. However produce is distributed along the road, in general, the portion of the road nearer the market will receive much more use than the distant portion. The first few miles of radial road from a town are also much used by vehicles other than market vehicles.

Although a very important matter, the average haul on a market road is somewhat difficult to determine. It may be estimated from the maximum haul or the known radius of the traffic area, and may usually be assumed to be two-thirds of the average maximum haul.

To show further the service which market roads render to a community, there is given in Table 4 the yearly and daily tonnage pass-

¹ In Bulletin No. 49 of the Bureau of Statistics of the U. S. Department of Agriculture, entitled "Cost of Hauling Crops from the Farms to Shipping Points," the average haul is assumed to be the radius of the circle whose area is one-half the area of a circle whose radius is the maximum haul. The average haul is then about seventy-one hundredths of the maximum haul. If all produce on a traffic area of one-sixth of a complete circle were hauled directly from the point where it originates to the market at the center, the resulting average haul would be sixty-seven hundredths of the maximum haul, which is the radius of the sector. If all produce were first concentrated on the middle radius of the sector, the average haul resulting would be sixty-four hundredths of the radius.

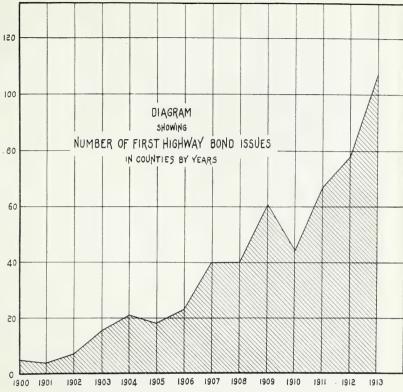


Fig. 1.—Diagram Showing Number of First Highway Bond Issues in Counties by Years.



FIG. 2.—POOR MACADAM CONSTRUCTION OF 1911 AFTER 1 YEAR.



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Map of the United States Showing the Distribution by Counties of Highway and Bridge Bonds Voted to January 1, 1914.



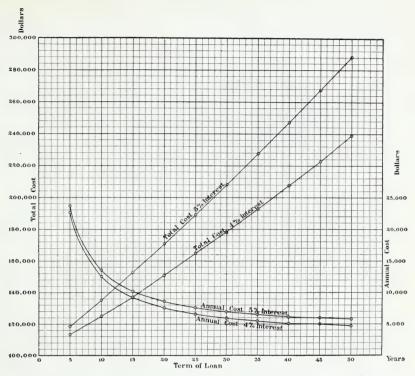


Fig. 1.—Diagram Showing the Relation Between Annual and Total Cost and the Period of Highway Bonds—\$100,000 Sinking Fund, $3\frac{1}{2}$ Per Cent.

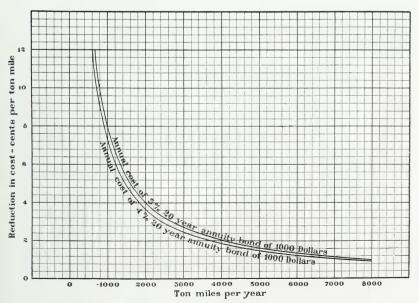


Fig. 2.—Diagram Showing the Relation Between Total Reduction in Cost of Hauling and Annual Cost of a \$1,000 Bond.



MAP SHOWING MARI





Map Showing Market Road System, Dallas County, Ala.



ing over six market roads assumed uniformly distributed about a market center and extending from 1 to 15 miles through a territory each acre of which yields the same weight of market products.

Table 4.—Theoretical average tonnage on each of six uniformly distributed market roads.

			Uniform yield per acre of—								
Maxi- mum haul.		One-tenth ton.		One-fourth ton.			One-half ton.				
	Average haul.	age		Fons hauled per day.		Tons hauled per day.		Total	Tons hauled per day.		
			Over first mile	Over eighth mile.	tons per year.	Over first mile.	Over eighth mile.	tons per year.	Over first mile.	Over eighth mile.	
1 2 3 4 5 6 7 8 9 9 10 11 12 13 14 15	0.66 1.32 2.00 2.67 3.33 4.00 4.67 5.33 6.00 6.67 7.33 8.00 8.67 9.33	33. 5 134. 0 301. 6 536. 2 837. 8 1, 206. 2 2, 144. 8 2, 714. 5 3, 351. 2 4, 055. 8 4, 825. 7 5, 663. 3 6, 568. 0 7, 540. 0	0.07 .40 .96 1.74 2.75 3.98 5.43 7.11 9.00 11.13 13.47 16.04 18.83 21.85 25.09	0. 85 2. 75 4. 87 7. 22 9. 79 12. 58 15. 59 18. 83	88. 8 335. 0 754. 0 1,340. 5 2,094. 5 3,015. 5 5,362. 0 6,786. 3 8,378. 0 10,138. 5 12,064. 3 14,158. 2 16,420. 0 18,850. 0	0. 17 1. 00 2. 40 4. 36 6. 87 9. 95 13. 58 17. 76 22. 51 27. 82 33. 68 40. 10 47. 08 54. 63 62. 73	2. 13 6. 88 12. 18 18. 05 24. 48 31. 45 38. 98 47. 08	167. 5 670. 0 1, 508. 0 2, 681. 0 4, 189. 0 6, 031. 0 8, 211. 0 10, 724. 0 13, 572. 5 16, 756. 0 20, 279. 0 24, 128. 5 28, 316. 5 32, 840. 0 37, 700. 0	0. 34 2. 01 4. 80 8. 71 13. 74 19. 90 27. 15 35. 52 45. 02 55. 63 67. 35 80. 20 94. 15 109. 25 125. 45	4. 25 13. 75 24. 35 36. 10 48. 95 62. 90 77. 95 94. 15	

The average acreage yield in pounds or the acreage coefficient varies with the locality. As market roads are usually located through farming country, the weight of crops per acre of farm land is a good indication of the tonnage originating on market roads. The report of the 1910 Census shows an approximate average product of 332 pounds per acre of farm land. The average yield per acre on *improved* farm land in crops was 1,674 pounds. The average weight per acre of forest products on unimproved farm land was 122 pounds.

It is found that usually 20 per cent of the roads in any county carry nearly all the traffic—possibly 90 per cent of the total. In the United States 20 per cent of the total mileage of roads is about 440,000 miles. There is an average of about 2,000 acres of farm land to each mile of such road, which should represent about 65 per cent 4

¹ There is a considerable return haul of fertilizer, fuel, kerosene, supplies, wire fence, etc., which can be partially determined by thorough inquiry of dealers.

 $^{^2}$ A careful computation of the weight per acre of all marketed crops in Tompkins County, N. Y., based on the data of Bulletin No. 295 of the Cornell Agricultural Experiment Station, gave 0.51 ton per acre of land in cultivation, which was 70 per cent of the total farm area and 63 per cent of the total area. The acre yield for the entire area was, therefore, 0.35 ton.

³ These figures are derived by determining the weight and acreage of each crop reported and by making reasonable assumptions as to distribution in the case of fruits, etc., where acreage was not given. (See Table 2.)

⁴ The average per cent of lands in farms in 39 States which reported more than 20 per cent of their areas in farms in 1910 was 65.16.

of the adjacent land. On each of the six radial market roads which have been assumed for the calculations above there would be a traffic area of 4,021 acres and a farm area of 2,614 acres per mile.

COST OF HIGHWAY CONSTRUCTION.

The cost of a given type of highway varies, but the range of variation has become comparatively well defined for each type within a given region. The standard of construction for any given type is now also generally understood and adhered to in the best practice. As this standard becomes more generally adopted, the price variation for similar local conditions will become less. In Table 5 there are given examples of cost per mile for three types of modern State highways. These averages are taken from lists of State construction jobs which are tabulated in Appendix C.¹ The standard which present specifications represent is a necessary standard evolved as the result of 20 years of modern road building. When these standards are ignored. it is usually at the expense of good work.

Table 5.—Cost elements of three types of highways.1

Туре.	Drainage and grading.	Surfacing.	Total.	Drainage and grading.	Surfacing.
Gravel (20 feet wide) Ordinary or water-bound macadam (15 feet wide) Bituminous macadam (15 feet wide) ²		\$2,599 5,815 7,533	\$4,416 9,215 10,298	Per cent. 41. 15 36. 90 26. 85	Per cent, 58.85 63.10 73.15

¹ These cost elements were obtained from 87 gravel jobs and 104 macadam jobs in Maine and New Jersey, and from 53 bituminous-macadam jobs in Maine, Massachusetts, and New Jersey. The averages were computed by weighing each job with its relative length and reducing all costs by simple proportion to equivalent average widths of 20 feet and 15 feet respectively. The complete tables of cost elements on the 244 jobs are given in Appendix C.

² Includes eight jobs of bituminous resurfacing. (See footnotes, Appendix C.)

The cost of highway construction may be subdivided into (a) cost of enduring features and (b) cost of perishable features. are built with accepted standards of grade, alignment, drainage structures, and foundations, the cost of such elements may be charged for enduring features. Whether roads so built result in the maximum percentage of permanent investment depends in part upon the cost and nature of the wearing surface. For example, a highway completed with all the best enduring features and then surfaced with gravel would show a higher percentage of cost for enduring features than the same road surfaced with more expensive material, as ordinary macadam or bituminous macadam. A poorly constructed gravel road, however, where enduring features had been slighted, would present a very high percentage of charge for temporary features. Macadam roads, so called, have been built with bond money by simply spreading broken stone in the mud. An example is shown in Plate I, figure 2.

¹ These examples were selected from States in which records were kept so as to permit cost analysis.

In issuing bonds for building highways the element of investment is of great importance. The allowable variations in grade and alignment are considerable, as are also the variations in the types of drainage structures. But there exists always a minimum standard below which it is uneconomical for any community to build on borrowed money.

It is manifestly poor policy to build an expensive surface or a relatively long-lived surface on defective grades with poor alignment, or where the drainage features are short-lived and temporary. Construction should be so adjusted to the service needed that its purpose is accomplished without waste. A county with impassable muddy clay roads must obtain, with a bond issue of \$100,000, a maximum mileage of improvement. If roads are constructed costing \$10,000 per mile, but 10 miles can be built. It is quite probable that the best economic result will be obtained by building 40 miles of road at a cost of \$2,500 per mile. This money should be spent largely for enduring features, such as grading, drainage, etc.

The common error, however, in county bond issues is to fix the sum to be voted upon and then to demand an exorbitant mileage for that sum. There is presented in Table 5 and in Appendix C the percentage of the cost of drainage and grading, exclusive of surfacing, and the percentage of cost of the surfacing on a considerable mileage

of road from several States.

Not all the surfacing need be a perishable feature. It is becoming more and more common to construct roads with surfaces built in two courses, the lower of which is regarded as a permanent feature of construction. This is particularly true of those types of road that are built with concrete foundations for bituminous-macadam, brick, or asphalt surfaces. Most hard roads are now seldom allowed to wear into the foundation course of the surfacing. It is probably conservative to regard 40 per cent of the surfacing cost of macadam or more enduring pavements as a cost for permanent features. Well-built macadam roads, from the recorded costs in Table 5, would therefore indicate a cost of 62 per cent of the total cost for permanent features and bituminous-macadam roads about 56 per cent. This method of estimating can not be applied to gravel or any natural soil road. Under most existing systems of maintenance the entire surfacing of such roads steadily deteriorates. It is generally accepted that roads built with surfaces entirely of concrete or with a brick pavement and a concrete foundation are permanent. It is not, however, yet known how long the best concrete surface will wear and it is certain that serious failures of concrete surfaces have resulted from poor construction. The best vitrified brick surfaces may have a life of 30 years or more, but repairs will usually be required and sufficiently extensive data on the life of modern vitrified brick roads grouted with cement mortar are still lacking to fix the average life period.¹

The danger of building roads with little attention to anything but the surface, with no provision for repair and maintenance, and with bonds of excessive term is, however, very serious. Complete returns of highway mileage built with local bond issues are not available, but there is given in Appendix B (Tables 25 and 26) a list of bond issues and mileage constructed with the proceeds where the reports are complete.

COST OF HIGHWAY MAINTENANCE.

Highways constructed with borrowed money should be strictly maintained.² Maintenance is necessary in order to insure to the community the maximum economic service by the road and also to preserve the investment. The cost of maintenance and repairs must, therefore, be studied at the outset. Unfortunately public records do not yet present complete data on the cost of either repair or maintenance, except in certain States which have highway departments.

Well-constructed gravel roads will sometimes sustain several years of traffic without showing marked deterioration, even when there has been no maintenance. Such roads sometimes even improve during the second season; more frequently, however, they show ruts or the formation of chuck holes. It can not be expected that the average life of a gravel surface will be greater than that of a macadam surface. The average interval for resurfacing macadam roads is between six and seven years. If a sum equal to two-thirds of the original cost of the gravel surface itself is provided for renewals at six-year intervals, it should be estimated at from \$150 to \$250 per mile per year. If \$30 is then allowed for annual dragging and small repairs, the total annual cost of repair and maintenance of gravel roads would be from \$180 to \$280 per mile. The annual cost of strict maintenance is sometimes below \$30. In Bennington County, Vt., during 1912, 175 miles of gravel roads were maintained at a cost of \$20.70 per mile. The annual cost of maintenance and repair on sand-clay roads, including all necessary resurfacing at periodic intervals, should not be fixed at less than 10 per cent of the original cost.

The cost of repair and maintenance of water-bound macadam roads has been determined with considerable exactness from Massachusetts figures and checked by resurfacing charges in other States and in Germany. From \$100 to \$125 per year ordinarily pays for necessary small repairs, such as patching, cleaning culverts, etc.,

¹ For further information as to the life of roads, see Bulletin No. 48 of the Office of Public Roads, U. S. Department of Agriculture, "Repair and Maintenance of Highways," and Bulletin No. 23 of the U. S. Department of Agriculture, "Vitrified Brick as a Paving Material for Country Roads." These bulletins may be obtained from the U. S. Department of Agriculture.

² See Bulletin 48, Office of Public Roads, U. S. Department of Agriculture.

and from \$400 to \$425 per year is the necessary annual charge for resurfacing at periods varying from six to seven years. (See footnote 1, p. 12.) The sum of \$525 per mile, on an average, should therefore absolutely maintain macadam roads if changes and increases of traffic are not excessive. It must be understood, however, that in many instances where macadam sufficed for the volume and character of traffic prior to 1906, it will not withstand the action of the motor vehicle traffic which has developed since that time.

Many miles of ordinary or water-bound macadam road have been resurfaced with bituminous materials and many miles of new bituminous-macadam road have been constructed. The logical maintenance of such highways is a surface treatment with bituminous material and rock screenings, clean gravel, or sharp sand. The cost of such surface treatment is from 4 to 12 cents per square yard, and it may be expected to last from one to three years, according to the density of traffic and the success of the application. Theoretically, perfect surface treatment would constitute absolute maintenance for a bituminous-macadam road. Such maintenance is seldom or never realized and bituminous-macadam roads doubtless require resurfacing at intervals. The cost of such resurfacing is not yet known. The average cost for repair and maintenance of 7,300 miles of highway in Connecticut, Massachusetts, New York, New Jersey, and Rhode Island for the year 1912 was about \$800 per mile. A large part of this money was expended for bituminous resurfacing and bituminous surface treatment. There is some question whether the expenditure correctly measures the average cost of repairing and maintaining bituminous-macadam roads. In the State of New York, however, for the years 1911 and 1912 the average cost for repair and maintenance was \$724 per mile upon a total average of 2,861 miles. The annual cost of repair and maintenance on Massachusetts State roads for the years 1910, 1911, and 1912 was, respectively, \$642, \$647, and \$676 per mile for about 850 miles. For the most part these figures for New York and Massachusetts represent the cost per mile of resurfacing with bituminous material and of maintaining bituminous-macadam and water-bound macadam roads by surface treatment with bituminous material. It is clear, therefore, that \$700 per mile is not an excessive estimate at present for the annual cost of all repair and maintenance of bituminousmacadam roads.

The cost of maintaining concrete roads is not yet known. It is known, however, that great care must be exercised in constructing such roads to insure their success. There have been cases where such roads began to disintegrate along the wheel tracks in less than a year, owing to defective concrete. Sometimes such roads have cracked so badly that it was necessary to remove the surface entirely. In other instances the necessary repairs have been very expensive.

Instances are also known where concrete road surfaces have shown a very high percentage of annual wear. In other cases there is apparently no measurable wear. If the road surface is built with the proper mix of concrete and carefully placed, it apparently should last indefinitely and not rut. Some cleaning of the surface and patching of joints and small depressions will be necessary at all times, so that the maintenance can not be entirely neglected.

The cost of repair and maintenance upon brick highways is very low. In most instances, where the construction is as nearly perfect as possible, almost no maintenance charges have resulted. Perfect construction, however, is seldom obtained. It is not unusual to find depressions and points of wear in brick roads, but it is less common than formerly. Brick roads are now usually constructed on a concrete foundation, with very carefully selected vitrified brick, and with the joints filled with cement mortar. Their annual maintenance costs, although low, are not on record with sufficient continuity to

supply accurate data.

It has not been customary for officials to face frankly the cost of maintenance and repair on bond-built highways at the time the bonds are issued and before construction begins. In fact, in the majority of cases where bonds have been issued by local authorities there has been no provision whatever for maintaining the roads when built. This is perhaps the gravest defect in the project of building highways by issuing bonds. The cost of all maintenance and repair over a series of years has ranged in the past from 6 to 10 per cent of the original cost of construction on the average and varies with the type of construction. Concrete roads and brick roads apparently are a marked exception to this rule. In future construction where the type of road is properly adapted to traffic and with careful maintenance from the outset the percentage of repair and maintenance cost should be lower.

THE BOND ISSUE.

Sinking-fund bonds.—The majority of highway bonds now outstanding have been issued as straight terminable bonds to be retired by sinking funds. Many such bonds now run for excessive terms. Although the term varies from 10 to 40 years, the average is nearly 25 years.² The fund to retire the bonds is accumulated by annual installments paid by the taxpayers and is supposed to draw interest continuously and to accumulate a sufficient amount to discharge the debt at maturity. The interest which the sinking fund draws is usually from 1 to 2 per cent less than the interest paid for the loan. Five per cent highway bonds are common with the sinking fund calculated to draw $3\frac{1}{2}$ per cent interest. Table 6 shows the annual payments to the sinking fund necessary to accumulate \$1,000

 ¹ Cf. Bulletin 23 of the U. S. Department of Agriculture.
 ² Some issues—notably New York State—run 50 years. Cf. Appendices A and B.

at 3, $3\frac{1}{2}$, and 4 per cent compounded semiannually for varying periods from 1 to 30 years.

Table 6.—Annual payments which, with interest at 3, 3½, and 4 per cent, compounded semianually, will amount to \$1,000 at the end of a term of years.

Voors	Ar	nual payme	nts.	W-0	Annual payments.			
Years.	3 per cent.	$3\frac{1}{2}$ per cent.	4 per cent.	Years.	3 per cent.	3½ per cent.	4 per cent.	
1 2 3 4 5 6 6 7 8 9 10 11 12 13 14 15	\$1,000.0000 492.5562 323.4583 238.9468 188.2699 154.5102 130.4175 112.3666 98.3436 87.1402 77.9872 70.3721 63.9399 58.4372 53.6780	\$1,000.0000 491.3266 321.8368 237.1428 186.3672 152.5508 128.4252 110.3564 96.3254 85.1208 85.1208 63.64527 68.3643 61.9427 56.4527 51.7080	\$1,000.0000 490.1000 320.2221 235.3498 184.4796 150.6104 126.4560 108.3733 94.3382 83.1366 73.9954 66.3996 59.9924 54.5191 49.7928	16 17 18 19 20 21 22 23 24 25 26 27 28 29 30	\$49, 5229 45, 8652 42, 6221 39, 7280 37, 1306 34, 7875 32, 6639 30, 7313 28, 9656 27, 3469 25, 8582 24, 4850 23, 2149 22, 0373 20, 9428	\$47. 5689 43. 9283 40. 7032 35. 2499 32. 9267 30. 8236 28. 9116 27. 1670 25. 5696 24. 1024 22. 7508 21. 5024 20. 3465 19. 2739	\$45, 6734 42, 0537 38, 8504 35, 9976 31, 1429 29, 0636 27, 1759 25, 4557 23, 8829 22, 4404 21, 1136 19, 8901 18, 7591 17, 7113	

¹ In Appendix D, page 98, Example 9 shows the method of calculating this table.

Table 7 illustrates how an annual sinking fund of \$32,345.83 accumulates for three years to \$100,000.

Table 7.—Accumulations of an annual payment of \$32,345.83 with interest at 3 per cent compounded semiannually.

Number of 6-month intervals.	Principal at beginning of 6-month intervals.	Interest during 6-month intervals.	Annual payment at end of 6-month intervals.	Total amount at end of 6-month intervals.
1	\$0.00	\$0.00	\$0.00	\$0.00
2	0.00	0.00	32,345.83	32,345.83
3	32,345.83	485.19	0.00	32,831.02
4	32,831.02	492.47	32,345.83	65,669.32
5	65,669.32	985.04	0.00	66,654.36
6	66,654.36	999.81	32,345.83	100,000.00

To obtain the necessary annual payments to produce any multiple of \$1 it is necessary merely to multiply the tabular value in Table 6 by the corresponding multiple; thus, an annual sinking fund payment to retire \$100,000 in 15 years at $3\frac{1}{2}$ per cent would be \$5,170.80. Table 33, pages 120 and 121, gives the yearly or periodic payments necessary to accumulate \$1 in a given number of years or periods at varying rates of interest.

There are objections to the sinking-fund method of retiring high-way bonds. It may not be possible to obtain continuously the requisite rate of interest on the sinking fund to discharge the debt at maturity. The existence of the sinking fund is a constant temptation to municipal officers to use it for purposes other than the purpose originally intended. If a county, for example, issues bonds for a second object, it is easy to argue that the sinking fund already accumulated may be used to purchase the new securities, and the finances

of the community are in a way to become much confused. This is particularly true since the officers in charge of such operations are frequently changing. Sinking fund tax levies may be deferred through carelessness or under pressure of other needs. The sinking fund always requires careful attention, because it does not progress automatically in most cases.¹ It has sometimes been entirely neglected. The total cost of a bond issue retired by a sinking fund will be greater in the end than the cost of the same bond issue made by either the annuity method or by the serial method.

Annuity bonds.—By the annuity method of issuing bonds both the principal and interest are discharged by constant annual or semi-annual payments. The amount of each payment or installment is determined by the rate of interest and the term of the bond. It usually is necessary to subdivide the bond issue into individual bonds of \$100,\$500, or \$1,000 each. The resulting periodic payment of principal and interest must vary slightly because of this adjustment. Tables 8 and 9 show, in detail, the schedule of principal and interest repayments upon a loan of \$100,000 for 20 years, retired by this plan at 4 and 5 per cent per annum, respectively. The necessary adjustment to the nearest \$100 bond is also shown. It will be seen that the amount of principal retired is small at first and constantly increases while the interest charge decreases. The sum of interest and principal remains constant, and this is an advantage as the tax is then uniform.

Table 8.—Repayment of a 4 per cent \$100,000 loan, including both principal and interest, by a uniform annual payment of \$7,358.175 for 20 years.²

	Adjusted to	o nearest cen	it.	A	djusted to	\$100 bonds	3.
Years.	Principal owing at beginning of year.	Interest for year.	Principal repaid at end of year.	Principal owing at beginning of year.	Interest for year.	Princi- pal repaid at end of year.	Total.
1	\$100,000.00 96,641.82 93,149.82 93,149.82 93,177.11 85,739.62 81,811.03 73,476.13 69,057.01 64,461.11 59,681.38 54,710.46 49,540.71 44,164.16 38,572.56 20,757.28 26,709.40 20,419.60 20,419.60 13,878.21 7,075.16	\$4,000.00 3,865.67 3,725.97 3,580.68 3,429.59 3,272.44 3,109.01 2,939.05 2,762.28 2,578.44 2,387.49 1,981.63 1,766.57 1,542.90 1,310.29 1,068.38 816.78 816.78 283.01	\$3, 358. 18 3, 492. 50 3, 632. 21 3, 777. 49 3, 928. 59 4, 085. 73 4, 249. 17 4, 419. 12 4, 595. 90 4, 779. 73 4, 970. 92 5, 169. 75 5, 376. 55 5, 591. 60 5, 815. 28 6, 289. 80 6, 541. 39 6, 803. 05 7, 075. 16	\$100,000 96,600 93,100 89,500 85,700 81,800 77,700 69,100 64,500 59,700 44,500 59,700 44,500 32,700 44,100 32,700 20,400 7,100	\$4,000 3,864 3,724 3,580 3,428 3,272 3,108 2,940 2,764 2,580 2,188 1,980 1,764 1,540 1,068 816 556 284	\$3, 400 3, 500 3, 600 3, 800 3, 800 4, 100 4, 400 4, 400 4, 800 5, 200 5, 600 5, 800 6, 300 6, 500 7, 100	\$7,400 7,364 7,324 7,320 7,328 7,372 7,308 7,364 7,380 7,388 7,388 7,388 7,386 7,364 7,306 7,306 7,308 7,368 7,368 7,368
Totals		47, 163. 50	100,000.00		47,152	100,000	147, 152

¹ In some States there are restrictions on the nature of county investments for sinking fund purposes.

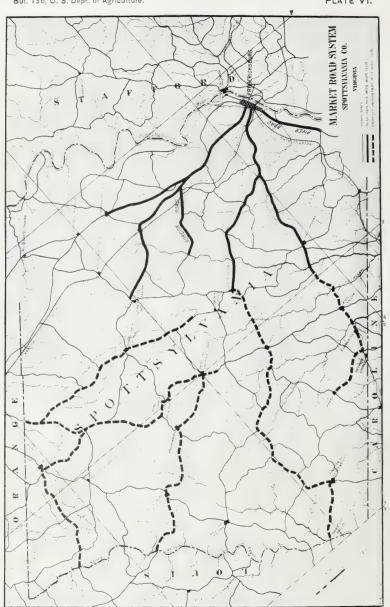
² An additional table showing the annual payments necessary to discharge a loan of \$1, with interest for varying terms and rates, is given in Table 36 on pages 126 and 127.



Fig. 1.—Dallas County, Ala. Wooden Bridge on an Unimproved Road, 1 Mile Northwest of Marion Junction.



Fig. 2.—Dalías County, Ala. New Steel Bridge with Concrete Floor Built in 1911 to Replace the Bridge in Figure 1.



MAP SHOWING MARKET ROAD SYSTEM, SPOTSYLVANIA COUNTY, VA.



Fig. 1.—Spotsylvania County, Va. Unimproved Road from Fredericksburg to Chancellorsville, March, 1910.



FIG. 2.—Spotsylvania County, Va. Chancellorsville Road Improved, March, 1911.

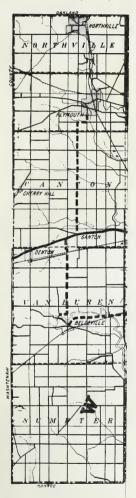


Fig. 1.—LEE COUNTY, VA. ONE AND ONE-HALF MILES FROM JONESVILLE; NEW MACADAM ROAD BUILT FROM BOND ISSUE; OLD ROAD SHOWN AT THE RIGHT FOREGROUND.



Fig. 2.—Lee County, Va. Improved Road Built Under Bond Issue of 1911 NEAR CUMBERLAND GAP; OLD ROAD IS SHOWN AT THE RIGHT.

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MAP SHOWING IMPROVED ROADS, WAYNE COUNTY, MICH.



Table 9.—Repayment of a 5 per cent \$100,000 loan, including both principal and interest, by a uniform annual payment of \$8,024,259\(^1\) for 20 years.

	Adjusted t	o nearest cen	ıt.	Adjusted to \$100 bonds.			
Years.	Principal owing at beginning of year.	Interest for year.	Principal repaid at end of year.	Principal owing at beginning of year.	Interest for year.	Princi- pal repaid at end of year.	Total.
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18	\$100,000.00 96,975.75 93,800.28 90,466.04 86,965.08 83,289.07 79,429.26 75,376.46 71,121.02 66,652.81 61,961.19 57,035.00 51,862.49 46,431.36 40,728.67 43,4740.84 28,453.62 21,852.04	\$5, 000. 00 4, 848. 79 4, 690. 02 4, 523. 30 4, 348. 25 4, 164. 35 8, 768. 82 3, 556. 05 3, 332. 64 2, 851. 75 2, 936. 43 1, 737. 04 1, 422. 68 1, 092. 60	\$3, 024, 25 3, 175, 47 3, 334, 24 3, 500, 96 3, 676, 01 4, 052, 80 4, 255, 44 4, 468, 21 4, 691, 62 4, 926, 19 5, 172, 51 5, 431, 13 5, 702, 69 5, 987, 83 6, 287, 22 6, 601, 58 6, 931, 66	\$100,000 97,000 93,800 90,500 87,000 83,300 79,400 75,300 71,000 66,500 61,800 56,900 40,600 34,600 28,300 21,700	\$5,000 4,850 4,690 4,525 4,350 4,165 3,970 3,765 3,550 3,325 3,255 3,090 2,845 2,585 2,315 2,030 1,730 1,415 1,085	\$3,000 3,200 3,300 3,500 3,700 3,900 4,100 4,500 4,700 4,900 5,200 5,400 6,000 6,300 6,900	\$8,000 8,050 7,990 8,025 8,050 8,065 8,070 8,065 8,050 8,045 7,985 8,015 8,030 8,030 8,015 7,985
19 20	14, 920. 38 7, 642. 14	746. 02 382. 12	7, 278. 24 7, 642. 14	14, 800 7, 600	740 380	7, 200 7, 600	7,940 7,980
Totals		60, 485. 18	100,000.00		60, 405	100,000	160, 405

¹Cf. Example 14, p. 101, for details of calculations.

Serial bonds.—The serial bond differs somewhat from the annuity bond, because, instead of keeping the annual payment of both principal and interest constant, the principal alone retired each year remains fixed. This type of bond has become more common for highway purposes in recent years, and during 1912 and 1913 the number of serial issues exceeded the number of issues for any other single given term. The Office of Public Roads received reports for these two years of \$15,300,819 in serial highway bonds, which is over 20 per cent of the total county and district bonds for which the period or term of issue was reported. In Tables 10 and 11 are given the necessary annual payments of interest and principal for an issue of \$100,000 for 20 years at 4 and 5 per cent, respectively, where the bonds are retired by annual payments of \$5,000 each. The first retirement is sometimes deferred for a number of years.

Table 10.—Schedule of interest and principal to retire a serial loan of \$100,000 at 4 per cent, with annual principal repayments of \$5,000.

Years.	Principal outstand- ing at beginning of year.	Interest for year.	Principal repaid at end of year.	Total.	Years.	Principal outstand- ing at beginning of year.	Interest for year.	Principal repaid at end of year.	Total.
1 2 3 4 5 6	\$100,000 95,000 90,000 85,000 80,000 75,000 70,000	\$4,000 3,800 3,600 3,400 3,200 3,000 2,800	\$5,000 5,000 5,000 5,000 5,000 5,000 5,000	\$9,000 8,800 8,600 8,400 8,200 8,000 7,800	12 13 14 15 16 17 18	\$45,000 40,000 35,000 30,000 25,000 20,000 15,900	\$1,800 1,600 1,400 1,200 1,000 800 600	\$5,000 5,000 5,000 5,000 5,000 5,000 5,000	\$6,800 6,600 6,400 6,200 6,000 5,800 5,600
8 9 10	65,000 60,000 55,000	2,600 2,400 2,200	5,000 5,000 5,000	7,600 7,400 7,200	19 20	10,000 5,000	400 200	5,000 5,000	5,400 5,200
					Totals.	5,000	42,000	100,000	142,00

Table 11.—Schedule of interest and principal to retire a serial loan of \$100,000 at 5 per cent, with annual principal repayments of \$5,000.

Years. Principal outstanding at beginning of year.	Interest	Principal repaid at end of year.	Total.	Years.	Principal outstand- ing at beginning of year,	Interest for year.	Principal repaid at end of year.	Total.
1 \$100,000 2 95,000 3 90,000 4 85,000 5 80,000 6 75,000 7 70,000 9 60,000 10 55,000 11 50,000	\$5,000 4,750 4,500 4,250 4,000 3,750 3,500 3,250 3,000 2,750 2,500	\$5,000 5,000 5,000 5,000 5,000 5,000 5,000 5,000 5,000 5,000 5,000	\$10,000 9,750 9,500 9,250 9,000 8,750 8,500 8,250 8,000 7,750 7,500	12 13 14 15 16 17 18 19 20 Totals.	\$45,000 40,000 35,000 30,000 25,000 20,000 15,000 5,000	\$2,250 2,000 1,750 1,500 1,250 1,000 750 500 250	\$5,000 5,000 5,000 5,000 5,000 5,000 5,000 	\$7,250 7,000 6,750 6,500 6,250 6,000 5,750 5,500 5,250 152,500

Comparison of serial, annuity, and sinking-fund bonds.— It will be noticed that the total expense to the community under the serial plan is somewhat less than under the annuity plan. The expense by either method is, however, considerably less than the expense under the sinking-fund plan. For the purpose of comparison the total expense to the community under each plan is assembled under Table 12.

Tables 8 to 11, inclusive, are computed with interest payable annually. Bonds with interest payable semiannually sell better. Similar tables or schedules for the annuity and serial plans of bond issues to conform to semiannual interest payments can be easily prepared. Schedules can also be prepared to show the progress of a bond loan when the bonds are bought at a premium or discount.

Table 12.—Total cost of a loan of \$100,000 for 20 years, interest compounded annually.

Annual		fund comp nnually at-	Amusita	Serial.		
on bonds.	3 per cent. 3½ per cent.		4 per cent.	Annuity.	Serial.	
$\begin{array}{c} 4 \\ 4\frac{1}{2} \\ 5 \\ 5\frac{1}{2} \\ 6 \end{array}$	\$154, 431 164, 431 174, 431 184, 431 194, 431	\$150,722 160,722 170,722 180,722 190,722	\$147, 163 157, 163 167, 163 177, 163 187, 163	\$147, 163 153, 752 160, 485 167, 359 174, 369	\$142,000 147,250 152,500 157,750 163,000	

In a bond issue by any given plan the amount, the interest, and the term may be fixed at will, but when this is done the annual repayments of principal and interest are theoretically determined. Thus, by the annuity method, if \$100,000 is to be issued at 5 per cent annually and retired in 20 years, the annual amount of interest and principal is at once determined to be approximately \$8,000.

¹ Cf. Appendix D, pages 91 to 115, for details of such schedules.

For the same bond issue under the serial plan, the total annual payment varies because the interest varies, but each yearly payment of interest and principal is nevertheless fixed.

Under the sinking-fund plan the annual payment necessary for principal and interest is theoretically constant, but it depends upon the interest realized upon the sinking fund. It is not safe, as a rule, to estimate this interest at more than 3½ per cent. Then for a \$100,000 20-year loan, with annual interest on the sinking fund, the total annual payment would be \$8,536.11. If the sinking fund could earn the rate of interest which is paid upon the loan there would be no advantage in expense to the community in the annuity or the serial bond over the sinking-fund bond. There is given in Table 13 the total mill tax on \$1 to retire a bond issue of \$100,000 by the sinking fund or the annuity plan.

Table 13.—Annual mill tax on \$1 for interest and retirement on a bond issue of \$100,000, at 5 per cent annual interest, for terms of 10 and 20 years.

	Mill tax.								
		10 ye	ears.		20 years.				
Valuation.	Sinking-fund plan,1				Sinking-fund plan,1				
	3 per cent.	3½ per cent.	4 per cent.	Annuity plan.2	3 per cent.	$\frac{3\frac{1}{2}}{\text{cent.}}$	4 per cent.	Annuity plan.2	
\$1,000,000 1,500,000 2,000,000 3,000,000 3,500,000 3,500,000 4,000,000 4,000,000 6,000,000 6,000,000 7,000,000 7,500,000 7,500,000 8,000,000 8,000,000 9,000,000 10,000,000 10,000,000 10,000,000 10,000,000 10,000,000	13. 723 9. 149 6. 861 5. 489 4. 574 3. 921 3. 431 3. 050 2. 745 2. 287 2. 111 1. 830 1. 715 1. 614 1. 525 1. 445 1. 372	13. 524 9. 016 6. 762 5. 410 4. 508 3. 864 3. 381 3. 005 2. 705 2. 459 2. 254 2. 081 1. 932 1. 803 1. 691 1. 503 1. 424 1. 352	13.329 8.886 6.665 5.332 4.443 3.808 3.332 2.962 2.666 2.423 2.222 2.051 1.777 1.666 1.568 1.481 1.403	12. 950 8. 634 6. 475 5. 180 4. 317 3. 700 3. 238 2. 878 2. 590 2. 355 2. 158 1. 992 1. 850 1. 727 1. 619 1. 524 1. 439 1. 363 1. 295	8. 722 5. 814 4. 361 3. 489 2. 907 2. 492 2. 180 1. 938 1. 744 1. 586 1. 454 1. 163 1. 1026 969 918 8. 872	8. 536 5. 691 4. 268 3. 414 2. 845 2. 439 2. 134 1. 897 1. 707 1. 552 1. 423 1. 313 1. 219 1. 138 1. 067 1. 004 948 8. 899	8.358 5.572 4.179 3.343 2.786 2.388 2.090 1.857 1.672 1.520 1.393 1.286 1.194 1.114 1.045 9.883 9.890 8.806	8. 024 5. 350 4. 012 3. 210 2. 675 2. 293 2. 006 1. 783 1. 605 1. 459 1. 337 1. 235 1. 146 6. 1. 070 1. 094 4. 892 845 802	

With interest compounded annually.
 The tax for the serial plan is slightly less, but varies from year to year.

It is quite probable that so many 30-year bonds are issued in order to take advantage of the fact that bonds of that term result in a low annual charge for interest and sinking fund. It will be seen from Table 14 that very little advantage is gained by fixing the term of a bond longer than 30 years. The annual charge decreases very slowly from that point, whereas the total charge increases rapidly.

Table 14.—Annual and total costs of a loan of \$100,000 for varying periods, with sinking fund to draw $3\frac{1}{2}$ per cent interest, compounded annually.

	Annual interest on bonds.								
	4 per	cent.	5 per cent.						
Term in years.	Total annual payment, interest, and sinking fund.	Total cost of loan.	Total annual payment, interest, and sinking fund.	Total cost of loan.					
5 10 15 20 25 30 35 40 45 50	\$22,648 12,524 9,183 7,536 6,567 5,937 5,500 5,183 4,945 4,763	\$113, 241 125, 241 137, 738 150, 722 164, 185 178, 114 192, 494 207, 309 222, 540 238, 169	\$23, 648 13, 524 10, 183 8, 536 7, 567 6, 937 6, 500 6, 183 5, 945 5, 763	\$118, 241 135, 241 152, 738 170, 722 189, 185 208, 114 227, 494 247, 309 267, 540 288, 169					

The same facts are presented in the diagram of Plate III, figure 1. The curves of annual cost of interest and retirement fall very slowly after the 30-year point.

It is an unfortunate fact that most highways do not have a life of 30 years, and it is now quite evident that the life of the highway and not the apparent economic term of the bond should determine the length of the loan. Many miles of natural soil roads are annually built by 30-year bond issues. There is usually no provision for repair and maintenance charges, and little business organization in the county road system. This practice is financially dangerous. No gravel road surface can last 30 years, and apparently the only road surfaces for which a 30-year life is recorded are surfaces of far more expensive construction than are usually built under the bond issues reported to the Office of Public Roads.

There is a further advantage in the annuity or serial bond for highway construction, because it is more likely under such a bond that the road surface will be paid for before it is entirely worn out. If an annuity or serial bond begins to mature immediately, this is not considered a serious objection among bankers. These types of bonds are particularly adapted for financing operations which by their very nature involve a wasting of the property. A highway is in part a wasting property and it is desirable to have established a margin of safety in highway financing. Railroads frequently issue serial equipment bonds for a period of 10 years with which to purchase rolling stock. The amount of bonds retired annually is carefully adjusted so that the retirement is faster than the depreciation of the rolling stock. The difference between the outstanding bonds and the value of the equipment in any year is the margin of safety.

¹ Massachusetts in 1912 reduced the term of State highway bonds from 30 to 15 years. Wisconsin passed a law, effective in 1913, providing that counties may issue 5 per cent bonds for State highways for periods not to exceed 10 years. The bonds must be serial bonds, with interest and redemption fund to be raised by direct taxation.

From the nature of the annuity or the serial form of highway bonds it is never necessary to issue new or refunding bonds at the end of the term. Both of these types of bonds have the advantage that they accomplish with one financial operation all that the sinking-fund type of bond can accomplish. The main advantage, however, of both types of bonds is that the community saves more money than under the sinking-fund plan because it avoids paying a higher rate on borrowed money than it can obtain on money that it loans.

Highway bonds are seldom sold at par. Not infrequently they command a slight premium; that is to say, they are sold at an advance over the par value. In nearly every State the law provides that municipal bonds shall not be sold at less than par. When the purchaser pays a premium for a 5 per cent highway bond it will yield less than 5 per cent. To enable investors to determine quickly the net rate of yield from a bond purchased at a premium or at a discount, tables known as bond tables have been calculated. In Appendix D is presented a short bond table of this kind (Table 37). From this table the net yield of a bond with a nominal rate of interest of from 3 to 6 per cent, payable semiannually and for varying terms, may be calculated for various prices. Thus a 5 per cent 15-year highway bond purchased at 103.20, or with a premium of 3.20 per cent, will be found to yield the purchaser 4.70 per cent on his investment.² Such tables are of more important interest to the purchaser than to the municipality offering the bonds, but they are necessary for the intelligent direction of the bond issue.

In calculating the price to be paid for serial bonds, it is customary to treat each series separately and to find the price that yields the given net rate by adding the separate prices. Some formulas will be found, however, in Appendix D which considerably shorten the labor of calculating the price to be paid for serial bonds and the labor of related calculations.

Special form of annuity bond.—In the operation of the annuity bond both interest and principal are discharged by a series of equal installments, usually semiannual. Each installment contains interest on the bonds outstanding at the beginning of the interval and the balance is applied to retire the bonds. The effect of this method is to diminish steadily the investment of the purchaser. If, however, the borrower should arrange to set aside periodically in a sinking fund a fixed sum in excess of the periodic interest on the entire issue, the effect would be to leave the total investment of the purchaser undisturbed until the sinking fund had accumulated to the amount of the loan. When the excess of the periodic installment over the required interest is arbitrarily selected and accumulates at a given rate of

¹ Massachusetts requires the premium to be deposited in the sinking fund. To avoid paying par value for the bonds, bidders frequently bid par or above par and require an allowance for attorney's fees and expenses.

² Cf. Appendix D, page 129.

interest, the term of the bond is thereby absolutely fixed. A simple way to accomplish this result is to add to the nominal interest rate which the bonds pay a percentage of the principal to be set aside in a sinking fund to retire the bonds. There is produced thus a new nominal rate. Since both interest and principal are discharged by the periodical payment of interest or dividends at the new nominal rate, an issue of this character may be described as a special form of annuity bond.

Table 15 shows the resulting terms in years of a bond issue for \$1,000,000 where from $1\frac{1}{2}$ to one-half per cent of the principal is set aside semiannually in a sinking fund which draws 3 per cent compounded semiannually. The original interest rate on the bonds is assumed to be 3 per cent, payable semiannually, and the new increased nominal rate varies then from 6 to 4 per cent. The last column shows the total cost to the borrower for the loan of \$1,000,000 under this method.

Table 15.—Necessary terms and total costs of a bond issue of \$1,000,000 at 3 per cent, payable semiannually, when retired by various arbitrary fractions of the principal set aside and compounded semiannually.

Applied semiannually to sinking fund to retire bond issue.	New increased interest rate on original 3% bonds.	Term of bonds.	Total cost to borrower.
Per cent. of loan. 11/2 13/8 11/4 11/8 1 7/8 34/4 5/8 1/2 1/2	Per cent. 6 53/4 51/2 51/4 5 43/4 41/2 41/4 4	Years. 231/2 25 261/4 281/2 31 34 37 411/2 47 50	Dollars. 1, 410, 000 1, 437, 500 1, 457, 500 1, 457, 500 1, 550, 000 1, 615, 000 1, 665, 000 1, 663, 750 1, 880, 000 2, 000, 000

The progress of the accumulation of the semiannual sinking fund under the plan here outlined is shown for varying retirement rates in Table 17. It is possible so to determine the rate of retirement that the resulting term of the bonds is integral instead of fractional. The increased nominal rates for 3 per cent bonds to retire in varying integral terms is as follows:¹

Table 16.—Equivalent nominal rates for retiring 3 per cent bonds in varying terms.

	Per cent.		Per cent.
10 years	11. 649148	30 years	5. 078686
20 years	6. 685420	40 years	4. 309664
25 years	5. 714336	50 years	3. 874114

¹ This rate per cent is determined by the formula:

Rate per cent= $3+200/S_{2n}$

where n is the number of years $S_{\overline{2n!}}$ is determined from Table 32, Appendix D, at the rate $1\frac{1}{2}\%$.

Table 17.—Accumulations at 3 per cent, convertible semiannually, of a semiannual sinking fund to extinguish a loan of \$1,000,000.

4½ per cent. 4½ per cent. 5½ per cent. 5½ per cent. 5½ per cent. 6½ per cent.	Percentage which the semiannual sinking-fund payment bears to the loan.	\$ per cent. \$ per cent. I per cent. If per cent. If per cent. If per cent. If per cent.	\$7,500.00 \$8,750.00 \$10,000.00 \$11,250.00 \$12,500.00 \$13,750.00 \$15,000.00 15,112.30 17,631.25 20,150.00 22,688.75 25,187.50 77760.25 30,225.00 22,889.19 26,615.72 30,452.5 31,528.78 38,062.31 41,871.84 45,678.88 30,881.78 35,785.40 40,990.08 120,405.62 120,405.62 133,784.02 147,162.42 160,540.83	173, 427. 50 202, 332. 09 231, 236. 67 260, 141. 25 289, 045. 84 317, 950. 42 346, 835. 01 281, 540. 11 228, 433. 46 375, 386. 81 422, 310. 17 469, 233. 52 516, 156. 87 563, 680. 22 491, 703. 10 477, 844. 07 563, 687. 14 737, 644. 66 736, 183. 54 563, 680. 22 506, 639. 55 591, 079. 48 675, 519. 40 759, 959. 33 844, 389. 25 928, 839. 18 1, 013, 279. 10	537, 065, 23 626, 576, 10 716, 086, 98 805, 597, 85 895, 108, 72 984, 619, 59 552, 621, 21 644, 724, 75 736, 882, 28 889, 331, 82 921, 035, 35 1, 013, 138, 89 584, 366, 69 681, 812, 80 779, 384, 382 876, 635, 03 974, 061, 14 600, 703, 24 700, 820, 44 807, 975, 43 976, 472, 36 1, 001, 172, 06	668, 246, 30 779, 620, 68 890, 995. 06 1, 002, 369. 44 728, 520 841, 878, 20 962, 146, 52 739, 934, 04 863, 256, 38 986, 578, 738, 533. 05 884, 955. 22 1, 0.11, 377, 40 855, 797. 52 998, 430. 44	876.134.48 1,022,156.90 917,728.15 982,487.67 1,004,724.98		
4½ per cent. 4½ per cent.	Percentage w	g per cent.	86, 250, 00 87, 500, 00 12, 593, 75 15, 112, 50 19, 082, 65 22, 839, 19 25, 568, 15 80, 80, 270, 41	144,522.92 173,427.50 234,616.76 281,540.11 339,174.34 407,608.20 400,802.59 491,763.10 422,199.63 506,639.55	447, 554.36 537, 065, 23 460, 517, 68 552, 621, 21 487, 908.57 584, 436, 69 500, 586.03 600, 708. 24 542, 484, 64 650, 981, 57	556, 871.91 668, 246, 30 601, 341.57 721, 609.89 616, 611.70 739, 931.04 623, 110.87 758, 533.05 713, 164.60 855, 797.52	730, 112. 07 764, 773. 46 818, 779. 72 818, 739. 72 982, 487. 67 964, 442. 83	1,017,072.88	8 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9
4 per cent.		½ per cent.	\$5,000.00 10,075.00 15,226.13 20,454.52 53,513.61	115, 618. 34 187, 693. 41 271, 339. 47 327, 842. 07 337, 759. 70	358, 043, 49 368, 414, 14 389, 624, 46 400, 468, 82 433, 987, 71	445, 497, 53 481, 073, 26 493, 289, 36 505, 688, 70 570, 531, 68	584, 089. 65 611, 818. 76 654, 991. 78 669, 816. 65 763, 554. 26	796, 707. 69 813, 658.31 939, 649.50 997, 797. 29 1, 017, 764. 25	1,144,015.22
New increased nominal rate on original	5% bonds.	Years.	0.5 1.0 2.0 5.0	10.0 15.0 20.0 23.0 23.5	24.5. 25.0. 26.0. 26.5. 28.0.	28. 5. 30. 0. 31. 0. 31. 0.	34.0 35.0 36.5 37.0 40.0	41.0 41.5 65.0 65.0 46.5 47.0	50.0

The details of advertising and selling highway bonds are frequently prescribed by law. Bids from bond houses are always made conditioned on an investigation of the validity of all proceedings leading to the issue. The attorneys for the bidders will require from the municipality certified copies of all papers concerning the transaction. There frequently is much variation in the form of the bids for a single issue. The items of denomination of the bonds, options on delivery, portion of the issue bid for, deposit of the money in stipulated banks, and items of less importance are often written into the bids.

TOTAL COST OF HIGHWAYS.

Charges included in total cost.—The first cost of construction is not the total cost of a highway. It is becoming customary to consider the cost of highways for a period of years.¹ This view of highway costs is important in the construction of highways with borrowed money. Municipal or county bonds are invariably issued for a definite term or period, and it is desirable, therefore, to know the total cost to a community during the life of the bond. Undoubtedly the best financial policy is to restrict the term of the highway bond to the probable useful life of the original type of road under actual conditions.

There is considerable difference of opinion among engineers and highway officials as to what constitutes the total cost of a highway during a given period of years. Questions arise over the interest charge on the original cost, the annual payments to amortize or retire the loan, the depreciation charge, and the repair and maintenance charge. Evidently if a repair and maintenance charge is made sufficient to maintain the road absolutely for an indefinite period, a depreciation charge has no place in the estimate of total annual cost. It is also apparent that total and annual costs for the loan can be made to vary at will by changing the period of the loan, i. e., the term of the bond. To make the problem more definite, it is desirable to assume, first, that the highway loan is a terminable loan and for a period not greater than the period for which the road will continue to serve with the original type of surface, grade, and alignment; and, second, that there is charged as the total cost of the road for that period all money paid by the community for that road in the form of taxes.

Although the cost of resurfacing a road or extraordinary repairs is a cost which occurs only at intervals, it is a safe and conservative plan to make an annual charge for all such work. As an example, if a water-bound macadam road is built at a cost of \$8,000 per mile

¹ Cf., for example, the report of the Cambridge (Mass.) Paving Commission, June, 1911, and the 1909 Report of Public Work in Cuyahoga County, Ohio, p. 21.

with money borrowed at 5 per cent for 15 years and retired by a sinking fund, there would result the following annual expense to the taxpayers for each mile for 15 years: Interest on \$8,000 at 5 per cent, \$400; annual sinking fund to retire \$8,000 in 15 years, at 3½ per cent interest compounded semiannually, \$413.66;¹ cost of annual maintenance, \$125; annual cost of periodic² resurfacing, \$400—making a total annual cost of \$1,338.66. By the annuity bond plan, the expenses would be: Annual repayments of interest and principal,³ \$770.74; cost of annual maintenance, \$125; annual cost of periodic² resurfacing, \$400—making a total annual cost of \$1,295.74.

At the end of 15 years the interest and redemption charges cease, and if resurfacing is carried out as planned the surface is but two years old and the community has a property the permanent value of which represents at least 62 per cent of the original cost, or \$4,960, exclusive of the surface, and an accumulation of \$800 toward resurfacing. If the road is to continue in its original form, the annual charge for repairs and maintenance will probably increase because of increased traffic. If the annual payment of principal is reduced by extending the period of the loan, there is danger that a new loan will be necessary for more expensive construction to meet the increasing traffic before the original loan is retired. Moreover, the decrease in annual payments of interest and principal is not inversely as the increase in the period of the loan. A 30-year 5 per cent annuity bond would require an annual payment of \$520.41 per mile on the \$8,000 macadam road above cited. (See Table 36 and Pl. III, fig. 1.)

If the same method of estimating the annual cost is used for each type of road considered, the relative total cost of the various types may be computed fairly and without confusion. If a highway were built from cash in the public treasury it would theoretically still be necessary to include in the annual cost of such a highway the interest on the first cost of construction at a rate which the municipality or county could obtain by investment of its funds. The question of how long such interest should run has never been determined.⁴

In estimating the total cost of a highway for a series of years the cost of repair and maintenance is the item most frequently neglected.⁵ The cost of the sinking fund or the charge for bond redemption is also sometimes forgotten. There are now outstanding bonds for highway construction where no provision has been made to retire them, although the bonds have been issued for a definite term.

¹ Use Table 6, p. 15.

² At intervals of 6.5 years, at \$2,600 per mile, or 29.5 cents per square yard for a 15-foot road; no allowance of interest is made; for discussion of this point, see p. 13.

³ See Table 36, Appendix D.

⁴ Theoretically interest would run until improved road had paid for itself by saving to community.

⁵ In one county of Virginia, after public highways had been constructed from the proceeds of a bond issue, the county established tollgates upon the highways in order to raise revenue for their maintenance.

Financing maintenance.—It is undoubtedly necessary, in general, to establish a direct tax for annual repair and maintenance for bond-built highways.¹ When highway bonds are issued it should be distinctly understood that there will be (besides the tax for interest and retirement) within a few years an additional tax for repair and maintenance, if the regular road tax within the county, as is most often likely, is not already sufficient to repair and maintain the new roads. This repair and maintenance charge is inevitable and, since the earning power of the road in reducing hauling costs tends to increase with the degree of maintenance, it is sound business to face the repair and maintenance charges in the beginning.

Comparisons of total costs.—When the more expensive types of highways are to be built by the proceeds of a bond issue, especially under increasing traffic, a question may fairly arise as to the relative portions of the total cost for a series of years, which should be devoted to repair and maintenance and to first construction and interest. As Table 5 shows, the cost of the hard highway surface constitutes, for standard types of construction, the largest percentage of total costs.

Up to a certain point, when the cost of the surface is increased, the cost per mile of maintenance correspondingly increases, but not usually the cost per unit of traffic. It costs more per mile to repair and maintain an ordinary macadam road, for example, than it does to repair and maintain a gravel road, and the cost per mile of repair and maintenance for bituminous-macadam roads is greater than for ordinary macadam roads. The costs of repair and maintenance of the best-built brick and concrete roads are apparently very low, and would, therefore, not follow the above rule.

The total necessary cost of a highway for a series of years can be determined only approximately and only after a study of the character and volume of traffic and a comparison of the total probable costs for the kinds of surface adapted to the traffic. It may not be economy to build a road of cheap first cost and high maintenance charges. If exact figures were available, accurate comparisons of different surfaces would be simple, but many items are still lacking. It is not known how long a concrete road will wear or what it will cost to renew it, especially if it has to be broken up and removed. The life of bituminous-macadam roads has not yet been fully determined, nor has the life of the best modern vitrified brick pavement. Absolute maintenance 2 on most pavements can seldom be continuous. Repairs or resurfacing operations will be needed at intervals which are as yet imperfectly determined.

¹ Cf. Act of September, 1913, by Legislature of Tennessee, which establishes a maintenance tax of 2 per cent of all highway bonds.
² See Bulletin No. 48 of the Office of Public Roads, p. 8.

If it is assumed that a 15-foot bituminous-macadam road costs \$10,500 a mile, and the corresponding 15-foot brick road \$18,500 a mile, with annual (absolute) maintenance for the bituminous road at \$600 per year and strict maintenance 1 for the brick road \$300 per year, the necessary items for the total cost for 20 years may be stated as follows:

Bituminous-macadam:

Br

Cost of construction (\$10,500) under 5 per cent serial bond with inter-	
est for 20 years ²	\$16, 012. 50
Cost of annual repair and maintenance (\$600) for 20 years	12, 000. 00
Total cost for 20 years	28, 012. 50
rick:	
Cost of construction (\$18,500) under 5 per cent serial bond with inter-	
est for 20 years ²	\$28, 212. 50
Cost of annual repair and maintenance (\$300) for 20 years	6, 000. 00
Total cost for 20 years	34, 212. 50

On the assumption made there is not as much difference in the total costs of the two road surfaces as would appear from the first costs. It is not known that \$600 per mile per year will absolutely maintain a bituminous-macadam road nor that \$300 per mile per year will strictly maintain a brick road, and the relative value of the two road surfaces at the end of the 20-year term is still to be determined.

The above analysis indicates a method of estimating the total cost of roads and of required bond issues. The total cost of a 15-foot concrete road, for example, may be compared with the above total costs, assuming a construction cost of about \$1.35 per square yard or \$11,880 a mile and an equivalent annual repair and maintenance charge between that of brick and bituminous-macadam.

EXPEDIENCY OF ISSUING HIGHWAY BONDS.

Legal restrictions on bond issues.—Nearly all States restrict the total amount of municipal bonds which may be issued to a fixed percentage of the assessed valuation. In other cases there are legal restrictions governing the amount of taxes which may be raised for highway purposes. These are examples of legal restrictions which must be clearly understood before the issue is made. The question frequently arises regarding the authority of the districts of a county to issue bonds. In a number of States the law allows the creation of highway districts or the issuance of bonds by the legal subdivisions of a county. Care must be exercised to determine to what officers the authority for such issues belongs. Instances have arisen where district road boards have undertaken the issue of bonds legally voted, but where the law provided that the county authorities and not the district authorities must issue the bonds.

In nearly all States county bonds or district bonds of any kind must be authorized by a majority, or a twe-thirds vote, of either the entire county or of the district.

Advantage of bond issues.—The issuance of highway bonds is essentially a method of capitalizing the resources of a community for the purpose of creating improved highways. The fundamental advantage of the bond plan is the construction of a good system of roads at once, but there are secondary advantages in building roads in long stretches and in the planning of the maintenance of such roads.

The question is not merely whether a community shall incur a debt; it is also a question as to whether the maximum economic efficiency and the full development of the public wealth will be best promoted by using public credit.

There is shown in Plate III, figure 2 the relation between the volume of traffic in ton-miles, reduction in hauling cost in cents per ton-mile, and the annual cost per \$1,000 of a 20-year bond under the annuity plan. A mile of road sustaining 3,000 tons of travel per year, for example, would pay interest and retirement on \$1,000 in 4 per cent bonds if the cost of hauling were reduced about 2.4 cents per ton-mile.

Emphasis has been placed in this publication on the strictly measurable economic benefits to a community from road improvement. There are many additional economic benefits and very great social benefits which are not readily measured. Increased school and church attendance is shown in repeated instances to be an immediate consequence of better roads. The general stimulus to business is difficult to evaluate. It is evident, however, that business and professional men of all classes are among the first to be benefited. This is especially true of physicians. The cost of upkeep of automobiles, particularly of tires, is becoming yearly a large item and the road condition is a most serious factor for the automobilist and the users of motor trucks.

It should be understood at the outset that the question of debt itself is relatively less important than the question of sound planning and good management of the loan. The very presence of the improved road system increases the value of the county property and therefore the resources supporting the loan. It is a well-established business principle that extension of credit within safe limits is necessary for maximum results. The financing of all private enterprises by bond issues has increased very greatly. In 1908 statistics show that, during the preceding decade, bonds were issued as a method of capitalizing public and private enterprises at the rate of \$583,000,000 annually.

¹ Cf. Farmers' Bulletin No. 505, "The Benefits of Improved Roads." This bulletin may be obtained from the Secretary of the U.S. Department of Agriculture.

Failure of bond issues.—Instances are not lacking where bond issues for highway purposes have proved failures. These instances are invariably due to mismanagement rather than to defective principle. Where counties have issued highway bonds the proceeds of which have been spent to construct temporary road surfaces on unimproved grades and without proper drainage, failure has necessarily resulted. There are on record in the Office of Public Roads instances where so-called macadam roads have been built with bond money by simply dumping broken stone at the wrong time of the year on muddy road surfaces without grades or alignments and without rolling or binding. (Cf. Pl. I, fig. 2.)

A typical method of mismanagement is to distribute the funds equally on all the roads in the county or district issuing the bonds. Recently in a southern State \$40,000 was distributed equally over nearly 90 miles of highway in a certain district. After deducting necessary overhead expenses this sum was equivalent to about \$400 per mile. Obviously no permanent results could be obtained from such a distribution. In another county, where heavy rains and severe winters could not fail to make the roads nearly impassable with the superficial construction adopted, bonds were issued to the amount of \$300,000. The money was devoted to light grading on an excessive mileage without any attempt at surfacing.

Through a misunderstanding of the essential principles underlying the establishment of a proper county road system, conflicts of interest sometimes arise which cause the failure of the bond issue plan. The location of the roads to be improved should not be determined by argument, but upon sound engineering and economic principles. Before a community votes to issue bonds for highways it is necessary to understand thoroughly what roads are to be improved and the approximate cost of their construction and maintenance. Too fre-

quently ill-advised locations are adopted.

Need for highway engineers.—Highway plans for bond issues require expert skill and professional service. Before the amount of bonds is determined, a thorough study of the needs of the county should be made and careful maps of the proposed highway system should be prepared. The sum to be issued should not be fixed until it is reasonably known what it will accomplish. It is customary for many counties to appoint a commission of business men under whose jurisdiction the bond money is expended. In other cases the county supervisor or county commissioner has the direction of expenditures. The best results have always followed where such commissions or county boards have secured the services of a highway engineer.

Guided by the costly experience of many communities, it is now becoming common for counties to adopt this plan. In all engineering construction it is customary to allow a certain percentage of the cost for engineering and supervision. There is no reason why highway building should be made an exception to this rule. At least 5 per cent of the bond issue may well be set aside for engineering and supervision alone. Money spent to hire a competent engineer ¹ to make preliminary investigations before bonds are issued and to plan and supervise construction will be well spent. It is not uncommon to find counties that will repeatedly postpone the sale of bonds in order to obtain an increase of 1 per cent in a bid for \$100,000 or less and then proceed to construct the roads in a most haphazard and ill-planned manner.

Benefit to nonabutting property owners.—In planning the highway system or the main market roads, as mentioned above, it will be found necessary to omit many roads the improvement of which is greatly desired by abutting landowners. The fact that such property holders must pay a tax for the bond issue is only an apparent injustice, for if the highway system is well planned the entire county will feel the benefits of the improvement. As a rule, main market roads reach the majority of producing areas, and when they are improved all land values tend to increase.

The fact that cities and larger towns are frequently taxed for bond issues to build highways outside of their own limits is sometimes made a point of debate in bond elections. It is argued that because a large part of the county wealth is within the corporate limit of such cities and towns, highway bond money should also be used to construct their streets. It is even urged that the expenditure should be made proportionate to the assessed valuation within the city limits. the proceeds of highway bond issues were distributed in this way their purpose in many cases would be defeated. The primary object of the county highway bond issue is to build county market roads and not to improve city streets, although a high percentage of the assessed valuation may be city property.² It is now known that the expenditure of city taxes on country roads is a sound principle and that it is one of the best features of State aid for highways. In Massachusetts the city of Boston pays possibly 40 per cent of the total State highway fund, but not a mile of State-aid highway has been built within its limits. New York City also pays about 60 per cent of the cost of the State highway bonds. Some State laws prohibit the expenditure of proceeds of State highway bonds within corporate limits of cities or towns. The improvement of market roads results in improved marketing conditions which benefit the city. Most cities are essentially dependent upon the surrounding country for their prosperity and development. The development of suburban property for resi-

¹In the general bond act of September, 1913, by the State of Tennessee the employment of an engineer by the county commissioner is made mandatory. In Virginia the law provides that counties building roads under a bond issue shall employ an engineer either appointed or approved by the State highway commissioner.

² For arguments concerning the benefits of good roads cf. Farmers' Bulletin No. 505.

dence purposes is also dependent upon highway conditions and it is becoming evident yearly that whatever makes for an increase in rural population must be encouraged. Since the introduction of motor traffic, country highways have been used to an increasing extent by city residents. In fact, the cost of maintaining many country highways has been greatly increased by the presence of city-owned motor vehicles. The general advance in facilities for doing country business from town headquarters when roads are improved is no inconsiderable factor in the commercial life of the community.

Examples of county bond-built roads.—The Office of Public Roads during the past four years has undertaken a detailed study of economic conditions in several counties which have issued bonds for highway construction. These studies have involved field work each year for from three to five years in the several counties. The detailed results of these studies are embodied in reports which are now on file in the office. Sufficient data have been gathered to emphasize and illustrate many points brought out by the discussion in the present bulletin.

The locations of the studies were Dinwiddie, Lee, Spotsylvania, and Wise Counties, Va.; Dallas County, Ala.; Lauderdale County, Miss.; Manatee County, Fla.; and Franklin County, N. Y. Although no special field studies were made in Wayne County, Mich., statistics for that county have also been compiled.

Table 18.—Financial items.

County and State.	Highway bonds.	Term in years.	Nominal interest.	Valuation year of issue.	Per cent of valuation in highway bonds.
Dinwiddie, Va. Lee, Va. Spotsylvania, Va. Wise, Va. Manatee, Fla Dallas, Ala Lauderdale, Miss. Franklin, N. Y Wayne, Mich	440,000 183,000 960,000 250,000 410,000 350,000	20 and 30 Serial. 30 30 30 30 30 60 Serial.	$5 \text{ and } 6$ $5 \text{ and } 5\frac{1}{2}$ 5 5 5 5 $5 \text{ and } 5\frac{1}{2}$ $4\frac{1}{2} \text{ and } 5$	\$3,661,897 3,014,405 11,962,956 11,011,780 2,450,000 13,330,355 16,443,301 12,293,434 467,400,635	2.84 14.59 9.32 8.71 10.20 3.08 2.13 4.07 .43

¹ 1913.

The total amount of bonds issued by these counties during the years 1900 to 1913, inclusive, was \$5,188,000, and with the exception of Lee and Wayne Counties, where the bonds were issued under the serial plan, and Franklin County, N. Y., where they are to run for 60 years, they are straight terminable bonds for 30 years. Table 18 summarizes the financial items for each county.

In some instances no preparation has been made for establishing a sinking fund to retire bonds at maturity. In several of these counties there is no provision whatever for systematic maintenance. In Virginia the State law provides that State aid allotted to counties may be used for the redemption of bond issues where the roads are built

in accordance with the requirements of the State highway commissioner and under the supervision of his engineers. In four counties in Virginia the roads are built under this plan. In Dallas County, Ala., the construction of bond-built roads was in charge of the four district commissioners and the probate judge. In Manatee County, Fla., the roads were built under the supervision of the five district county commissioners. In Lauderdale County, Miss., the county supervisors appointed a road commission of three members to construct the roads under the bond issue, and a highway engineer was employed and all work done by contract. In Franklin County, N. Y., the roads were constructed by the county road commissioners and the county superintendent of roads. In Wayne County, Mich., the roads were built by the board of county road commissioners, appointed by the county board of supervisors.

The following table shows the mileage and cost of roads constructed in each county:

Table 19.—Mileage and cost of roads in nine counties where bonds were issued.

County and State.	Miles built.	Per cent of total mileage in county.	Kind.	Average cost per mile.
Dallas, Ala	197	19.0	Gravel	\$3,700
Manatee, Fla	64	12.8	Sand-clay Macadam	4, 250
Lauderdale, Miss	84	10.5	Shell Macadam ¹	0,500
Spotsylvania, Va	41	10, 0	Sand-clay Gravel and sand-clay	1,900 2,200
Dinwiddie, Va	125 124	25. 0	Gravel and top soil	1,689
Franklin, N. Y		9. 0	Gravel Macadam	3,250
Lee, Va	84	18. 2	Earth graded	7,400
Wise, Va	131	43.7	Macadam	8,000
Wayne, Mich	83. 5	5.8	Earth graded	5,300 13,200

¹ Surface treated with petroleum asphalt,

In no one of these counties, with the exception of Detroit, in Wayne County, Mich., were there any large cities. The roads were, for the most part, constructed as market roads radiating from the main market towns in the county, as may be seen from the maps of Plates IV, VI, and IX. The economic benefits accruing to the several counties from the improvement of the roads are already apparent, and in several instances have been extraordinary. (Cf. Pls. V, VII, and VIII.)

In Dallas County, Ala., and Lauderdale County, Miss., cotton is the principal crop, although in the latter county lumber is also an important commodity. Lumber and ties form, also, the principal commodity hauled in Spotsylvania County, Va. In Dinwiddie County the principal commodities are tobacco, peanuts, and hay; in Lee County farm and dairy products, hardwood, lumber, and coal; and in Franklin County, N. Y., milk and miscellaneous farm products.

² Eighty miles.

In Manatee County, Fla., the principal crops are citrous fruits and early vegetables, which are shipped north. In Wayne County, Mich., the city of Detroit is the center of the road system and attracts a very large volume of miscellaneous traffic. The estimated annual tonnage hauled over the bond-built highways in almost every instance is sufficiently large to produce, by an assumed reduction of a few cents per ton-mile in cost, a sufficient operating income to cancel the annual interest and retirement fund required by the bonds. The relation of these items is summarized in the following table:

Table 20.—Summary of relation between bond requirements and reduced cost of hauling.

County and State.	Total annual ton-miles estimated at minimum.	Approximate cost of annual inter- est and redemption on highway bonds.	Equivalent necessary reduction (cents per ton-mile).
Dallas, Ala. Manatee, Fla Lauderdale, Miss. Spotsylvania, Va Dinwiddie, Va Franklin, N. Y Wayne, Mich	600,000	\$28,333	4.7
	1 200,000	17,342	8.7
	720,000	24,530	3.4
	574,720	12,695	2.2
	212,500	8,633	4.1
	201,544	25,544	12.6
	4,353,966	2179,882	4.1

¹ Rough estimate.

The increases in the value of land adjacent to the improved roads are especially noteworthy. In Manatee County, Fla., land increased in value \$20 per acre from 1911 to 1912, and a mile away from the road the increase was \$10 per acre. In Spotsylvania County, Va., land which formerly sold at an average of \$24.74 per acre changed hands within three years at an average of \$44.74. In Dinwiddie County, land between 5 and 10 miles from Petersburg advanced on an average from \$15.25 to \$30 in about 15 instances, and land 10 miles from town increased, on an average in 16 instances, \$16.32 an acre. On eight pieces of land in Franklin County, selected at random, there was an increase in value of 27.8 per cent after the improved roads were built, and in Lee County, Va., land advanced 25 per cent.

The construction of the bond-built highways in several of the counties herein mentioned has been of decided benefit to school attendance. In Spotsylvania County one consolidated school replaces three one-room schools, and another consolidated school is planned. In Dinwiddie County school attendance increased 17½ per cent in one year on the improved roads, and several school wagons carrying 24 pupils each have been put in service. In Lee County school attendance along the improved roads shows an average of 71 per cent against 62 per cent along other roads. In Wise County several successful school consolidations have been effected since 1909. The Pole Bridge School in this county on the road from Coburn to Wise replaces four one-room schools.

² Equivalent for annuity bond.

APPENDIX A.

STATE HIGHWAY BONDS.

Table 21.—Complete list of State highway bonds.

		Amount (by years).	Rate		
State.	Year.	Voted.	Issued.	(per cent).	Term (years).	How redeemed.
California	1910	1\$18,000,000		4	50	\$400,000 annually after July 1,
	1912 1913		\$2,000,000 3,390,000	4 4	50 50	1917.
Total		18,000,000	5,390,000			
Connecticut		² 4, 500, 000	1,500,000	31/2	22	\$205,000 annually.
	1909 1911 1913	33,000,000 33,000,000	1,500,000 2,000,000 2,000,000	4 4	25 25	\$120,000 annually. Do.
Total		10,500,000	47,000,000			
Idaho ⁵	1905 1907 1909 1911 1912 1913	50,000 18,000 22,000 136,000 29,000 250,000	50,000 18,000 22,000 136,000 29,000 250,000	4 4 4 4, 4½, 5 4½ and 5	30 20 10 and 20 5, 6, 10, 20 20 20	Sinking fund. Do. Do. Do. Do. Do. Do. Do. Do.
Total		505,000	505,000			
Maine 6	1912 1913	2,000,000	300,000	4	40	\$7,500 annually.
Total		2,000,000	300,000			
Maryland 7	1908 1909 1910 1911 1912 1913	5,000,000 81,000,000 93,170,000	500,000 1,000,000 1,000,000 1,250,000 2,250,000 2,646,000	$3\frac{1}{2}$ $3\frac{1}{2}$ $3\frac{1}{2}$ and 4 $3\frac{1}{2}$ and 4 (9)	15 15 15 15	Sinking fund. Do. Do. Do. Do. Do.
Total		9,170,000	8,646,000			
Massachusetts	1894 1895 1896 1897 1898 1899 1900 1901 1902 1903 1904 1905 1906	300,000 400,000 600,000 800,000 400,000 500,000 500,000 500,000 500,000 2,250,000	300,000 400,000 600,000 700,000 300,000 400,000 350,000 375,000 400,000 300,000 250,000	31 31 32 52 52	24 30 30 30 30 30 30 30 30 30 28 28	Do.

¹ California.—Proceeds of bond issue to be expended on a continuous and connected State highway system running north and south through the State, traversing the Sacramento and San Joaquin Valleys and along the Pacific coast, by the most direct and practicable routes, connecting the county seats of the several counties through which it passes, together with such branch roads as may be necessary to connect therewith the several county seats lying east and west of such State highway. No limitation on convenience of the several county seats lying east and west of such State highway.

4 For trunk-line roads only.
5 Idaho.—For various roads and bridges specified in the act authorizing each bond issue, except \$200,000

⁶ Idaho.—For various roads and bridges specified in the act authorizing each bond issue, except \$20,000 in 1913, which is expended under State highway commission.
⁶ Maint.—Not to exceed \$2,000,000 shall be outstanding at any one time. To be expended in the construction of State highways, the whole cost to be paid by State, except where a town may desire the joint State-aid fund to be applied on State highway.
⁷ Maryland.—For State roads.
⁸ Not to exceed \$250,000 to be issued in any one year, beginning Jan. 1, 1911.
⁹ To be issued in amounts of not less than \$500,000 at a time upon request of the State roads commission. Rate of interest to be fixed by the governor, the comptroller of the treasury, and the State treasurer.

nect therewith the several county seats lying east and west of such State highway. No limitation on annual expenditure.

² Connecticut.—To be expended during the six fiscal years ending Sept. 30, 1913. Bonds to be paid in 22 annual installments by appropriation from general fund.

³ \$1,000,000 for improvement of public roads; \$2,000,000 for improvement of trunk-line roads. The 1911 and 1913 bond issues mature in 1936, but may be redeemed by the State treasurer whenever and in such manner as he deems to be for the best interest of the State. They are not specifically known as road bonds; but the 1911 highway appropriation was specifically designated by the legislature to be from the proceeds of the \$6,000,000 State issue of bonds. The 1913 appropriation is made from the treasurer is, in a special act, authorized and instructed to issue \$4,000,000 additional bonds to meet the needs of the State.

⁴ For trunk-line roads only.

Table 21.—Complete list of State highway bonds—Continued.

State.	Year.	Amount (by years). Issued.	Rate (per cent).	Term (years).	How redeemed.
Massachusetts	1907 1908 1909	\$2,500,000	\$360,000 495,000 380,000	$\frac{3\frac{1}{2}}{3\frac{1}{2}}$ 3 and $3\frac{1}{2}$	30 30 10–30	\$12,000 annually. \$16,500 annually. \$220,000 deferred serial, 1920-
	1910		285,000	3^{1}_{2}	10-30	1939. \$180,000 deferred serial, 1920–
	1911		310,000	31/2	10-30	1939. \$200,000 deferred serial, 1921–
,	1912 1913	5,000,000 1 115,000	435,000 1,110,000	$\frac{3\frac{1}{2}}{3\frac{7}{2}}$	10-30	1940. All bu t \$175,000 deferred serial. Serial.
Total		14,365,000	8,450,000			
New Hampshire	1909 1910 1911 1912 1913	² 1,000,000 ³ 300,000	250,000 250,000 250,000 4 250,000	31/2		Deferred serial, 1914–1917. Deferred serial, 1917–1921. Deferred serial, 1921–1924.
Total		1,300,000	1,000,000			
New Mexico 5	1912	500,000		4		
Total		500,000	(6)			
New York	1906 1907 1908 1909 1910 1911 1912 1913	⁷ 50,000,000 8 50,000,000	1,000,000 5,000,000 5,000,000 5,000,000 10,000,000 8,000,000 (16,000,000 5,000,000	$\begin{array}{c} 3 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4 \\ 4\frac{4_2}{4_2} \end{array}$	50 50 50 50 50 50 50 50 50	Sinking fund. Do. Do. Do. Do. Do. Do. Do. Lo. Do. Do. Loted Sept. 1, 1913; sold Jan.
Total		100,000,000	55,000,000			
Rhode Island	1906 1909 1912	9 600,000 600,000 10 600,000		3 3½ 4	30 30 30	Sinking fund. Do. Do.
Total		1,800,000	1,800,000			
Utah	1911	11 260,000		4	23	Deferred serial, 1922–1934.
Total		260,000	260,000			
Washington 12	1911	190,000	125,000	4	12	Paid from State highway fund.
Total		190,000	125,000			
Totals		158, 590, 000	88, 476, 000			

council.

for the construction and maintenance of a system of State highways.

8 Bonds not sold Dec. 31, 1913.

7 New York.—These bonds were to be issued in two classes, to be known as A and B. Class A is coupon or registered, and redeemable from a State sinking fund, while Class B bonds were to be registered and redeemable from a redemption fund provided by the counties and towns wherein the proceeds thereof should be applied to the improvement of highways.

8 The act of the legislature authorizing this issue of bonds was ratified and rendered operative by vote of the people at the general election, November, 1912. Of the proceeds, \$20,000,000 shall be devoted to State highways, to be built at sole cost of the State, and \$30,000,000 to county highways, to be built at joint expense of State and county.

9 Rode | Right |

⁹ Rhode Island.—\$200.000 to be issued before Jan. 1, 1907, and the balance on or before Jan. 1, 1908; the proceeds to be used in building a system of State roads under the direction of the State board of public

roads.

¹⁰ To be used for construction, reconstruction, and maintenance.

11 Utah.—The proceeds to be divided equally among the counties of the State, exclusive of Salt Lake County, to be used in the construction and maintenance of State roads and bridges therein. Bonds dated July 1, 1911. 12 Washington.—For purchase of bridge across the Columbia River at Wenatchee.

¹ Massachusetts.—Authorized for special State roads by legislature, 1913.
² New Hampshire.—Not to exceed \$250,000 to be issued in any one year, and the proceeds to be used exclusively for State aid in the construction of the three trunk lines to be designated by the governor and council from the Massachusetts State line in a northerly direction.

To be used for State aid in constructing trunk-line highway to be designated by the governor and

⁴ Not sold Dec. 1, 1913.
5 New Mexico.—These bonds shall be in denominations of \$1,000, numbered 1 to 500, the first 20 of which shall be payable on Jan. 1, 1919, and 20 of said bonds, in consecutive numerical order, shall be due and payable on July 1 annually thereafter until and including July 1, 1942. The proceeds are to be expended for the construction and maintenance of a system of State highways.

STATE BOND ISSUES DEFEATED.

Colorado.—The proposition to issue \$10,000,000 in State bonds for roads was submitted to the people of Colorado at the general election in November, 1912, and was defeated. The proposition can not be again submitted to the people within a few years.

Ohio.—At the general election in November, 1912, there was submitted to a vote of the people of Ohio a proposition to issue \$50,000,000 in State bonds to construct a system of intercounty highways. The vote on this proposition numbered about three-quarters of a million, and the bond issue was defeated by 2,017. One remarkable fact in connection with this vote was that the cities of the State gave substantial majorities for the bond issue, while the rural vote was substantially against it, and to such an extent as to overcome the city majority, although about 80 per cent of the taxes which would have been levied to take care of the interest and sinking fund of the bonds would have been paid by the cities.

Rhode Island.—On June 3, 1913, a special election was held in the State of Rhode Island on the issuance of \$700,000 of State bonds for the purpose of completing a system of State roads. At this election only about 14 per cent of the voters of the State attended the polls, and the proposition was overwhelmingly defeated.

Pennsylvania.—On November 3, 1913, at a general election a proposed issue of \$50,000,000 in highway bonds was defeated, although the proposition carried in Philadelphia and Pittsburgh.

APPENDIX B.

APPROXIMATE LISTS OF COUNTY AND DISTRICT HIGHWAY AND BRIDGE BONDS; TOWNSHIP HIGHWAY AND BRIDGE BONDS; COUNTY, DISTRICT, AND TOWNSHIP HIGHWAY AND BRIDGE BONDS VOTED IN 1912 AND 1913; COUNTIES, DISTRICTS, BEATS, AND TOWNSHIPS GIVING COMPLETE MILEAGE RETURNS OF ROADS BUILT UNDER BOND ISSUES: TOWNSHIPS AND TOWNS GIVING COMPLETE MILEAGE RETURNS OF ROADS BUILT UNDER BOND ISSUES; SUMMARY OF ALL HIGHWAY AND BRIDGE BONDS VOTED TO JANUARY 1, 1914.

Table 22.—County and district highway and bridge bonds.1

ALABAMA.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total Amount voted to Jan. 1, 1914.	Term of years.	Inter- est rate.
Aufauga Blount Bullock Buller Colbert Conecuh Crenshaw Dallas² Elmore Escambia³ Hale Jackson Jefferson Lawrence Lee	\$65,000 150,000 160,000 155,000 200,000 200,000 125,000 410,000 38,000 100,000 250,000 200,000 253,000 255,000	30 30 30 30 30 30 30 30 30	Per ct. 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	Limestone Madison. Marion. Marshall Mobile Montgomery. Morgan Perry. Pike Russell. St. Clair. Sumter.	\$135,000 172,500 100,000 130,000 500,000 850,000 240,000 192,000 192,000 100,000 5,121,500	30 30 20 30 30 30 30 20	Per ct. 4½ 5 5 5 4½ 5 5 4½ 5 5 5 4½ 5 5 5 5 5

ARIZONA.

$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	Maricopa: Phoenix (city) ⁵ Mesa (city) ⁵ Special road district 1 Special road dis-
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ARKANSAS.

Benton. Crawford³. Jefferson. Lee.	45,500	12	6	Montgomery Sebastian: Ft. Smith ³ Woodruff: District 1	\$10,000 600,000 30,000	20 6
Lonoke				Total	1,218,315	

In 21 States highway and bridge bonds have also been issued by townships. See list following.

² Includes \$60,000 of bridge bonds.

³ Bridge bonds only.

⁴ Bridge.
5 To cover partial cost of improvement of Phoenix to Roosevelt Dam road.

Table 22.—County and district highway and bridge bonds—Continued. CALIFORNIA.

Counties	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Alpine 1. Contra Costa. Fresno 1. Glenn. Humboldt Kern. Lake. Los Angeles. Orange. Plumas.	\$4,800 300,000 80,000 450,000 15,000 2,500,000 20,000 3,500,000 1,370,000	(2) 20 25 40 10–25	Per ct. 5 6 5 7-9 5 5 41 2 5 4	Riverside Sacramento ³ San Diego. San Joaquin. San Mateo. Santa Barbara. Tehama. Ventura ¹ .	\$1,500,000 825,000 1,250,000 1,850,000 1,850,000 290,000 3,000 275,000 15,630,800	2 40 40 40 7-10-40 20	Per ct. 4\frac{1}{2} 5 5 6 6 5

COLORADO.

Counties.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Delta. Garfield San Miguel Total	\$71,700 28,000 35,000 134,700		Per ct. 5 6 6

DELAWARE.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Kent New Castle Sussex ¹	\$30,000 4 1,285,000 30,000	20 20–51 5–24	Per ct. 5 4-4½-5 4½	Districts 1–10	\$50,000 1,395,000	5–11	Per ct.

FLORIDA.

Alachua. Bradford: Hampton. Clay Columbia. Dade. De Soto. Duval. Franklin. Hernando. Hillsborough. Holmes: 1 district. Jackson.	\$40,000 25,000 150,000 40,000 250,000 250,000 1,050,000 20,000 300,000 1,400,000 40,000 300,000	20	5 4 ¹ / ₂ 5 6 4	Nassau. Orange. Palm Beach. Pasco Pinellas Polk: Winterhaven. Putnam St. John St. Lucie. Seminole. Walton.	70, 000 200, 000 200, 000 70, 000	30 30 30 30 30	6
Holmes: 1 district	40,000	30	6			20	6

GEORGIA

		0101	. VOLIZE		
Ben Hill Bleckley Clarke Colquitt Gordon Hancock Laurens Marion	8,000 100,000 400,000 8,000 51,000 202,000	 4 5 5	Miller Spalding Towns Troup. Trurner.	10,000 4,000 200,000 20,000	

¹ Bridge bonds only.
² Serial.

<sup>Bridge bonds, \$225,000.
Of this amount \$275,000 was for bridges.</sup>

Table 22.—County and district highway and bridge bonds—Continued. IDAHO.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Ada Bear Lake Boise Canyon. Custer ² Fremont: District 1 Gooding.	\$234, 484 45,000 70,000 1 198, 782 15,000 120,000 160,000	10-20 4 20 10-20 10-20	Per ct. 4½-5 5½ 4-5 6 6	Kootenai Lincoln. Oneida: Districts 1-3. Twin Falls Washington ² .	\$83,071 130,000 59,000 3 100,000 6,500 1,221,837	10-20	Per ct. 6 5 5 2 6
			ILLI	NOIS.			
Edwards: District 3	\$3,000	2 1–20	6	Wabash	\$12,000	5 5	5
Jackson 4 Peoria 4 St. Clair: Centerville District	36,320 320,000 49,000	5 20	5	Total	420, 320		
			INDI	ANA.			
Adams. Allen Bartholomew Boone. Carroll ⁶ Cass. Districts 1–3.	\$151,550 53,840 365,572 223,260 80,000 569,258 112,425	10 10 10 10 10	4½ 4½ 4½ 4½-5 4½-4-6	Marshall Martin Miami Monroe Montgomery Morgan Newton	\$86,400 189,881 636,656 315,000 1,795,723 341,200 67,021	15 10–20 10	41 41 41 42 42
Clark Clay Crawford Daviess Dearborn	90, 000 232, 272	10 10 1-20	4½ 4½ 4½ 4½ 4½ 4½	Ohio. Owen. Parke. Porter: Districts 1–3. Posey: Districts 1–3.	74,000 199,693 390,996 1,055,880 648,244	10 20 10–20	5 4½ 4½-5 4½-6
Decatur Delaware Dubois Fayette Fountain Franklin Frulton 6 Gibson Greene Hancock	7 63, 880 100, 000 196, 949 53, 610 137, 950 111, 000 50, 000 77, 300 42, 499 8 273, 500	10-15 10-20 10 10 10 10 10 1-10	4½ 4½ 4½ 4½ 3½-5 4½ 4½ 4½ 4½ 4½ 4½ 4½	Putnam Districts 1–3. Randolph Ripley Rush. St. Joseph 6 Shelby 6 Spencer Starke. Sullivan Switzerland	105, 000 41, 000 80, 982	10-20 10 20 10 10 10	$\begin{array}{c} 4\frac{1}{2} \\ 5 \\ 4\frac{1}{2} \\ \end{array}$
Harrison Henry Huntington Jackson Jasper Jay Jefferson Jemnings Knox Kosciusko Laporte Lavrence Madison	43, 220 41, 269 341, 932 9 29, 640 127, 500 50, 370 113, 525 69, 300 189, 360 1, 440 949, 640 93, 000 45, 000	10 10 10 20 10 10 20 10 10	4½ 4½ 4½ 4½ 4½ 4½ 4½ 4½ 4½ 4½	Switzerland Tippecanoe 6 Tipton: Districts 1-3. Union Vanderburg Vermilion Vigo Wabash Wayne Wells. White Whitley	55, 652 260, 000 673, 140 60, 000 266, 196 462, 800 305, 000 145, 320 8, 200 11 477, 791 513, 000 8, 369	10 10 10 10 10 10	4 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1
Marion		10-20	31-41-5	Total	18, 072, 049		

<sup>Bridge bonds \$151,162.
Bridge bonds.
\$50,000 for bridges.</sup>

⁴ Bridge. ⁵ Serial.

⁶ Bridge bonds only.

<sup>Bridge bonds \$30,000.
Bridge bonds \$25,000.
Bridge bonds \$15,000.
Bridge bonds \$200,000.
Outstanding.</sup>

Table 22.—County and district highway and bridge bonds—Continued. IOWA.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rațe.
Adams Allamakee ¹ Audubon ¹ Blackhawk Boone Buchanan Buena Vista Calhoun ¹ Carroll Cass ¹ Cedar ¹	42,000 3 14,226 60,450 3 15,087 3 16,797 40,000 40,000 4 162,066	12	4½	Iowa ¹ Jackson ¹ Kossuth ¹ Lue ¹ Lucas Madison ¹ Mahaska Marion ¹ Mills Palo Alto Plymouth	7 137,738 50,000	3–17 10–20	$\begin{array}{c} 4\frac{1}{2} \\ 4\frac{1}{2} - 5 \\ 4\frac{1}{2} - 5 \\ 4-4\frac{1}{2} \end{array}$
Cherokee Clarke Clinton 1 Crawford Dallas. Davis 1 Decatur. Delaware Des Moines. Dickinson 1	25,000 19,000 57,000 50,000 67,000 47,500 19,000 8 3,126 70,000		4½ 4½ 4½ 4½ 4½	Polk Pottawattamie Sac¹ Shelby¹ Union Van Buren Wapello¹ Warren¹ Winneshiek Woodbury¹	1,219,900 3 37,290 25,000 23,092 96,000 109,000 91,000 163,000 8 160,000 9 63,748	20	3½-5 4-4½-5 4½ 4
Dubuque. Fayette ¹ . Floyd. Fremont ¹ .	5 55, 352		4½		10 149, 452 11 4,006,314		4½-5

KANSAS.

KENTUCKY.

Bath Boyle Bullitt Carroll Christian Clark Franklin Gallatin Garrard Grant	4,000 50,000 40,672 202,000 60,000 23,000 38,500 33,000	4-5-6 4-5-6 4-6-4 4-41-6	Mason. Montgomery. Nicholas: Districts 1-4. Ohio. Owen. Pendleton. Robertson.	60,000 29,000 40,000 30,000 170,000 175,000 10,400	5–8	4 4 5 4 ¹ / ₂ -5-6 5
Christian	202,000		1-4			4
Clark	60,000		Ohio			
			Owen	170,000		5
Gallatin	38,500	4-6	Pendleton	175,000		43-5-6
Garrard	33,000	4	Robertson			
Grant	90,000	41-6	Scott	196,000		4-5
Harrison	37,500		Trimble	120,000		
Kenton	197, 100		Woodford	17,500		
Lewis	6,200		· ·			
Lincoln			Total	1,759,872		

Bridge bonds only.
 Includes \$16,298 outstanding warrants.
 Outstanding bridge warrants.
 Includes \$4,060 outstanding bridge warrants.
 Includes \$5,352 outstanding bridge warrants.
 Includes \$8,806 outstanding bridge warrants.
 Includes \$60,738 outstanding bridge warrants.
 Includes \$60,000 outstanding bridge warrants.
 Includes \$20,748 outstanding bridge warrants.
 Includes \$20,748 outstanding bridge warrants.
 Includes \$24,452 outstanding bridge warrants.
 Include officials may issue bonds to pay accur

¹⁰ County officials may issue bonds to pay accumulated outstanding warrants and the above list for the most part represents such funded warrants, all for bridges. It is customary to pay, in most instances, interest at 4, 45, and 5 per cent.

12 Bridge bonds \$100,000.

Table 22.—County and district highway and bridge bonds—Continued.

			LOUIS	IANA.			
Parishes ¹ and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Parishes and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Assumption. Bossier. Calcasieu De Soto. East Baton Rouge District 1. Franklin. Iberia. Iberville: Districts 1, 5, and 6.	\$86,000 175,000 900,000 60,000 22,000 15,000 16,914 70,000	10 1-40 25 10 10 20 10 1-10	Per ct. 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	Jefferson Lafayette Plaquemines	\$200,000 75,000 60,000 75,000 47,000 116,597 1,932,840	25 30 2-4	Per ct. 5
			MARY	LAND.			
Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Allegany Anne Arundel Calvert ² Caroline Cecil Charles Dorchester Frederick	\$10,000 37,000 3,000 50,000 100,000 10,000 43,000 127,000	2½ 20 15–30	Per ct. 5 5 5 5 5 4 4 4 2	Kent ² . Montgomery. Prince Georges. Queen Annes Talbot ² . Worcester. Total.	\$10,000 144,500 16,000 63,000 37,000 100,000	25 30 25	Per ct. 5 4½ 5
		7	IASSACE	IUSETTS.			
Barnstable 2 Berkshire Bristol Essex Nantucket	\$14,000 5,000 7,000 661,000 56,000	1-2 1-3	41/4 41/2 31/2 4 41/2 4	Norfolk ² Plymouth ² Total	\$50,000 20,000 813,000	(3)	4.92
			MICH	IGAN.		-	
Alger Alpena Baraga Bay Berrien Delta Emmet Genesee Gogebic Houghton Ingham Jonia Liron Kent	\$150,000 100,000 40,000 255,000 162,500 225,000 700,000 150,000 30,000 63,652 20,000 160,000 735,000	20 15 10–20 10	5 6 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	Mackinae Manistee 2 Mason Menominee Midland Muskegon 2 Ontonagon Ottawa Schoolcraft Wayne Wexford Total	\$100,000 32,000 100,000 56,000 25,000 38,000 600,000 40,000 2,000,000 50,000	10–26 15 15 10 15	5 4½ 5 4
			MINNE	ESOTA.			
Aitkin ² Anoka ² . Beltrami. Cook. Crow Wing ² . Hennepin. Itasca ² .	\$16,000 40,000 631,350 60,000 50,000 110,000 31,000	20 30 20	6 4 4 6 4 ¹ / ₂ 5	Lake. Mahnomen. Ramsey ² . St. Louis. Winona. Total	\$20,000 5,000 75,000 300,000 50,000 1,388,350	20 30 5-7	6 4 4½ 5

¹ Parishes are equivalent to counties.

² Bridge bonds only.

³ Nine months.

Table 22.—County and district highway and bridge bonds—Continued. MISSISSIPPI,

Counties, beats, and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties, beats, and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Adams. Alcorn Attala. Benton Benton Bolivar. Calhoun: Beat 1. Chickasaw: Beat 3. Claiborne. Clay: Beats 1-3 Coahoma. Copiah. Beat 2. Covington. De Soto: Beats 1, 2, 3, and 5. Frorrest. Beats 1 and 3. Franklin². George. Grenada Hancock. Hinds. Beats 1 and 5. Issaquena. Itawamba. Jackson. Jasper. Jefferson Davis. Jones. Beat 2. Lafayette Lamar Lauderdale: Beats 1 and 5.	\$150,000 95,000 50,000 6,000 392,000 125,000 221,000 221,000 225,000 305,000 50,000 250,000 120,000 30,000 52,000 30,000 52,000 30,000 52,000 30,000 50,000	25 20 20 10-25 25 30 1-10 20 25 25 40 20 20 25 25 30	Per ct. 5 5 6 6 5 5 6 6 5 5	Leflore Lincoln Lowndes: Beat 2 Marshall Monroe Montgomery. Neshoba Noxubee Beats 2, 3, and 5 Oktibbeha Panola Perry Pike Pontotoc Prentiss Beat 1 Quitman Rankin Brandon Starkey Simpson Beats 1 and 2 Sharkey Simpson Beats 1 and 5 Tallahatchie Beats 1 and 5 Tishomingo Tunica Union Warren Washington Warren Washington Wikinson 2 Yalobusha Beats 2 and 4 Yazoo: Four beats	\$300,000 200,000 200,000 20,000 40,000 380,000 377,500 50,000 20,000 20,000 20,000 20,000 20,000 20,000 40,000 40,000 40,000 40,000 40,000 40,000 50,000 40,000 50,000 60,		6 5 4-4½ 5
Lawrence Lee Beats 1 and 2	25,000 25,000 250,000 80,000	25	51-6	Total	8,710,872		

MISSOURI.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Boone 2 Callaway. Cedar. Christian. Clinton. Clay: Two districts. Cooper. Dade. Franklin. Greene. Grundy. Howell. Jefferson. Laclede.	100, 000 19, 000 6, 000 4, 000 3, 000 77, 000 325, 000 238, 000 5, 000	10-20	6 5 6 4 6 6 6 6	Lafayette Lawrence: Mt.Vernon Mississippi. New Madrid: King's Highway Malden Risco. Newton: Neosho Nodaway Pettis. Stone. Taney.	\$125,000 50,000 7,000 93,000 20,000 30,000 15,000 200,000 10,000 7,500		6

¹ Counties are subdivided into beats.
2 Bridge bonds only.
3 Twelve miles of levee.
4 Of this amount \$150,000 includes bridges, sewers, and culverts.
5 Bridge bonds, \$20,000.
6 Of this amount \$110,400 was issued for building bridges.

Table 22.—County and district highway and bridge bonds—Continued. MONTANA.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.			
Blaine Broadwater Carbon Cascade 20 districts LOster Dawson Flathead Lewis and Clark Lincoln Meagher Musselshell	\$40,000 102,000 90,000 45,000 320,000 100,000 177,500 105,000 125,000 30,000 2 130,000	20 20 20 20 20 20 20 20 20	Per ct. 5 5 5 4½ 4½ 5 4½ 5 5 4½ 5 5 5 5 6 6 6 6 6 7 6 7 7 7 8 7 8 8 8 8 8 8 8 8	Ravalli Rosebud Sanders 20 districts Sweet Grass Teton 33 districts Yalley ¹ Yellowstone ¹ Total	\$72,106 3 328,000 130,000 15,000 35,000 100,000 4 100,000 65,000 70,000 2,239,606	5-20	Per ct. 4½-6 5 5 4½ 5 5 4½ 5			
NEBRASKA.										
Blaine. Dawson ¹ Douglas. Garfield ¹ Keith ¹ Keyapaha ¹	\$5,000 6,000 5 308,000 4,000 49,000 30,000		6 4½ 5 4–6 3½–5	Lincoln. Morrill ¹ . Nance ¹ . Scotts Bluff. Total.	\$15,000 17,000 82,500 37,000 553,500		4½-5 3-7 5-6			
NEVADA.										
Churchill Douglas. Ormsby.	\$23,000 15,000 40,000	2–11	4 ³ / ₄ -5 5	Washoe 1	\$97,000		5-6-8			
			NEW J	ERSEY.						
Atlantic. Bergen. Burlington. Camden. Cape May. Cumberland. Essex. Gloucester. Hudson. Hunterdon. Mercer.	\$307,000 2,121,000 55,000 348,900 329,300 43,000 1,140,505 200,000 6,098,977 232,000 434,000	15 30 50 30 30 30	4-5 4-4½ 4-½ 4-½ 4-½ 4-½ 4-½ 4-4½ 4-4½ 4-4½ 4-4½	Middlesex Morris Ocean Passaic Salem Somerset Sussex Union Warren Total	\$781,500 400,000 35,000 941,500 45,000 75,000 154,100 30,000 14,386,782	30 14-17 5-10	3½-4½ 4 5 4-4½-5 4-4½-5 4 4-4½ 4			
			NEW M	IEXICO.						
Bernalillo 7	\$100,000	10-30	4½ 5	San Juan 1	\$18,000	20-30	6			

¹ Bridge bonds only.
2 Of this amount \$29,970 was used for building three bridges; balance for 300 miles of road.
3 Of this amount \$113,000 was for bridges.
4 Of this amount \$30,000 was for bridges.
5 Including inheritance tax.
6 Of the \$136,000 voted in 1913, \$26,000 was used for a bridge.
7 Roads and bridge bonds only.

Table 22.—County and district highway and bridge bonds—Continued. NEW YORK.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.			
Albany Cayuga. Chautauqua. Chemung. Clinton Columbia. Erie Franklin. Fulton. Greene. Herkimer Jefferson. Lewis. Livingston. Montgomery. Nassau Niagara. Oneida	\$749,000 29,777 160,000 99,670 15,000 56,000 1,297,000 70,000 408,000 130,000 25,244 77,106 201,000 2,007,749 4,000 150,000	1–20 60 4 6–20	Per ct. 4½-5 3½-4½-5 3½-4½-4½-4½-4½-4¾-5-6 4½-4½-4½-5-6 4.7-5 5	Ontario. Orange. Orleans. Otsego Putnam. Rensselaer St. Lawrence. Saratoga. Seneca Steuben Suffolk. Tompkins Ulster. Warren Westchester Wyoming	\$176,000 689,000 156,000 60,000 38,000 465,000 150,000 62,217 60,000 110,000 73,000 269,000 215,000 9,097,923	30 10-15 15 15 6 5-14 10 13½ 20-25	Per ct. 3\(\frac{1}{2}\) 4\(\frac{1}{4}\) 5\(\frac{1}{2}\) 4\(\frac{1}{4}\) 5\(\frac{1}{2}\) 4\(\frac{1}{4}\)			
	NORTH CAROLINA.									
			}	1		í	1			

Alamance	\$400,000		5	Iredell	\$400,000		. 5
Anson	100,000			Jones 1	10,000		
Beaufort 1	² 125,000			Lee	100,000	40	5
Bertie	20,000		5	Lincoln	200,000	40	5
Brunswick	40,000			McDowell	9, 273	5-10	6
Buncombe	50,000		5-6	Madison	300,000		
Cabarrus	³ 145,000	30	1	Mecklenburg	300,000		
Cherokee: Marble	,			Nash and Edgecombe	,		
District	187,000			Rocky Mt. District.	30,000	30	6
Cleveland	60,000	40	. 6	New Hanover	550,000	. 25	4-41-5
Cumberland 1	40,000		5	Orange	250,000		
Davie	175,000			Pasquotank	10,000		
Edgecombe	16,000		6	Polk	4 100,000	30	5
Districts 1-5, 8-11	200,000	55	5	Rutherford	250,000	40	5
Gaston	300,000		4	Sampson	150,000	10-20	5
Granville	160,000	20	41-5	Stokes 1	35,000	30	6
Guilford	300,000		~ 5	Vance	220,000	20-40	5
Haywood	60,000			Yancey	150,000		
Henderson	49,000						
Hoke	50,000		5	Total	5,541,273		

NORTH DAKOTA.

			Stutsman	\$36,500	 6
	6,500	 	Total	63,000	

¹ Bridge bonds only.

<sup>Bridge bonds only.
By act of legislature, county commissioners have authority to sell bridge bonds without vote of people.
Also 10 steel bridges.
By act of legislature.</sup>

Table 22.—County and district highway and bridge bonds—Continued.

Counties and districts.	Total amount voted to Jan. 1, 1914.	. Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Adams Ashland Ashland Ashland Ashland Athens Auglaize Belmont Butler Champaign Clark Clermont Columbiana Coshocton Crawford District I. Cuyahoga Darke Defiance Defiance Delaware Erie ⁷ Fayette Franklin Fulton Gallia Geauga Greene ⁷ Hamilton Hancock Harrison Henry Highland Hocking Huron Jackson Jefferson Knox Lake Lawrence Lawrence Licking Logan Lorain District I.	\$181,300 1 258,500 2 309,500 3 00,000 9 4,800 9 6,000 2 3,750 2 57,662 110,200 3 00,000 4 150,000 5 191,000	(6) 2-20 (6)	$\begin{array}{c} 4\frac{1}{2} - 5 \\ 4 - 6 \\ 4 - 4\frac{1}{2} - 5 \\ 4 - 4\frac{1}{2} \\ 4 - 4\frac{1}{2} - 5 - 6 \\ 4 - 4\frac{1}{2} \\ 4 - 4\frac{1}{2} - 5 \\ 4 - 4\frac{1}{2} - 5 \\ 4\frac{1}{2} - 5 \\ 4\frac{1}{2} - 5 \\ 4 - 4\frac{1}{2} -$	Lucas Madison Madison Mahoning District 1 Marion Mercer Miami Montgomery Morgan Morrow Muskingum Noble Ottawa Paulding Perry Pickaway¹ Pike Portage Preble Putnam Richland Ross Sandusky Scioto Seneca Sandusky Scioto Seneca Shelby¹ Stark Summit Trumbull Trumbull Truscarawas Union Van Wert Warren¹ Warren¹ Wayne¹ Warne¹ Wayne¹ Williams¹ Wood Wyandot 13 Districts	7,200	(6) 10 25 3-10 3-10 3-10 1-3 12-21 1-30 1-22 5 10	$\begin{array}{c} Per\ ct. \\ 4-1\frac{1}{5} \\ 5-1\frac{1}{4} \\ 4-1\frac{1}{5} \\ $
			j	1			

OKLAHOMA.

Carter 7. Choctaw Coal 7. Creek 7. Delaware Grady 7. Johnston 7. Muskogee	200,000	10-25	5	Nowata Okłuskee 7 Osage. Pottawatomie Tulsa Wagoner Total	75, 000 75, 000	5-5½ 5

OREGON.

-					1		
Clatsop	\$400,000 500,000	20 10-30	5	Multnomah	\$1,250,000	1-30	5
Ouchsoll	500,000	10-30	J	Total	2, 150, 000		

Of this amount \$114,000 bridge bonds.
Of this amount \$75,000 flood bonds were issued without a vote.
Of this amount \$70,000 for bridges.
Emergency road and bridge bonds.

⁵ Of this amount \$65,000 used for bridges.

⁶ Serial.

⁷ Bridge bonds only.

8 Of this amount \$9,000 used for bridges.

^{9 \$60,000} issued under emergency act of 1913 for

bridges.

1º Of this amount \$775.000 used for bridges.

11 Of this amount \$440,000 were 5 per cent flood emergency bonds.

12 Bridge \$250,000.

13 Bridge \$250,000.

14 Emergency bonds.

15 Bridge, \$6,000 emergency.

Table 22.—County and district highway and bridge bonds—Continued.

PENNSYLVANIA.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Allegheny. Beaver 2. Bedford. Berks. Butler Cameron. Clinton 2. Columbia Forest. Indiana Lackawanna Lebanon Lehigh.	1\$15,900,000 555,000 9,500 475,000 20,000 1,000 50,000 202,500 86,000 10,500 35,800 450,000 29,850 325,000	30 2-12 2-12 5	Per ct. 3\frac{1}{4} 4\frac{1}{4}\frac{1}{4} 3\frac{1}{2} 4 3\frac{1}{2} 4 4 3\frac{1}{2} 4 5 4-4\frac{1}{2}	Luzerne Lycoming. Mifflin. Montgomery. Northampton Potter. Susquehanna. Venango ² . Washington. Westmoreland. Wyoming ² . York. Total.	3 \$2,690,000 382,900 55,000 725,000 300,000 25,000 15,000 17,000 250,000 72,000 72,000 250,000 24,839,050	5-20 20	Per ct. 4½ 3-3½-4 4 3½-4 3½-4 5 5 5 4¾-2 3½-4
		S	оитн с	AROLINA.			
Dillon. Horry Kershaw ² . Laurens. Marion.	4 \$100,000 10,000 40,000 50,000 40,000	30	5 4½ 4½ 4½	Oconee. Richland ² Sumter. Total	\$45,000 75,000 50,000 410,000		
		8	SOUTH	DAKOTA.			
Pennington 2	\$44,000			Stanley 5	\$33,300		
			TENN:	ESSEE.			
Anderson Benton. Blount. Bradley. Campbell 6. Districts 1-5. Carter. Elizabeth Claiborne. Cooke. Coffee. Cumberland. Davidson Dickson. Grainger Greene. Hamilton. Hawkins. Hickman Jackson. Jefferson. 9 districts Knox. Loudon. 5 districts.	65,000 220,000 80,000 250,000 150,000 395,000 255,000 150,000	30 30 30 40 65 1-12½ 30 25	55 55 4½-55 5-6 5-6 5 5-6 5-6 5-2 4½-5	McMinn Madison Marion Maury Monroe Montgomery Morgan Perry 6 Polk Putnam Roane Robertson Sevier Shelby Sullivan Sumner Union Washington Wayne 6 White Total	250,000 365,000 450,000 2,45,500 2,792,000 530,000 50,000 168,000 47,700 90,000	30 7 15-30 30 20-30 15 12 20-30 30	4½-5 5 5 6 4½ 45 5 4½ 45 5 4½ 5 4½ 6

<sup>Of this amount \$550,000 bridge bonds.
Bridge bonds only.
Bridge \$100,000 payable serially, last 10 years of term.
Concrete bridge, \$17,500.
Certain townships only.
Bridge bonds.</sup>

Table 22.—County and district highway and bridge bonds—Continued.

TEXAS.

	Total			1	Total		
Counties and	amount	Term	Interest	Counties and	Total	Term	Total
Counties and districts.	voted to	of	rate.	districts.	amount	of	Interest
districts.	Jan. 1, 1914.	years.	1200.	districts.	Jan. 1, 1914.	years.	rate.
	Jan. 1, 1011.				3411. 1, 1314.		
			Per ct.				Per ct.
Anderson	\$150,000	20	5	Jim Wells	\$125,000	10	5
Atascosa	20,000		3	Johnson	136, 200	10	
Austin Districts 1 2	20,000 175,000	5-40	5	Johnson Jones ¹ Karnes	7,000	20	5
Bastrop: Districts 1 and 2 Baylor Bee Bell 2 districts Beyer				Karnes	7,000 42,000 10,000		
and 2	180,000	20-40	5	Kent 1	10,000		
Baylor	100,000	40	5	Kerr	40,000		
Bee	49,922	20	5	King	5,000		
Bell	100,000 49,922 19,960		5	Kinney	5,000 80,000		
2 districts	200 000	40	51/2	Knox 1	18,500		31-5
	1,250,000			Kent 1 Kerr King Kinney Knox 1 Lamar: Justice Pre-			
Borden	1,250,000 7,900 40,000		4-5		300,000 $45,500$	10-40	5
Bosque: District 7	40,000	40	5	Lampasas 1	45,500		4-5
Bowie	250,000 450,000 45,000	34	5	Lavaca	25,000		
BrazoriaBrooks	450,000	40	4–5 5	Leon: Districts 1, 2, 4, 5, and 6	134,000		
Brown: District 1	150,000	40	5	Liberty: Districts 1	134,000		
	150,000 47,000 240,000		J	and 4	425,000		5
Burnet	240,000			Limestone: District 4	300,000	10-40	5
Calhoun: Districts 1	210,000			Live Oak	16, 990	10-40	4-5
and 2	235,000	40	5	Llano .1	425,000 300,000 16,990 25,000		
Callahan	1,276		4	Llano 1 McCulloch McLennan	118,000	40	4–5
Callahan	1,276 20,000 35,000			McLennan	118,000 150,000	40	3-5
	35,000	40	5	McMullen	4,000		5
Chambers	168,000	20	5	Matagorda	560,000		
Childress	25,000 25,000		4-6	Maverick. Medina. Menard.	42, 602 60, 000 20, 000		5
Coke	25,000			Medina	60,000	40	4
Colorado	60,000	40	4	Menard	20,000		
Coke Colorado Collingsworth	14,888	5-40	4-6	Midland	50,000		
Collin	14,888 450,000 153,000		-:-::-:-	Midland	57, 872 200, 000		
Comal	155,000	40	4-41-5	Willed	200,000	40	
Coneno 1	15,000		4-6	Mills ¹ Mitchell: District 1	5, 400 30, 000	40	5
District 1	100 000	40	5	Montgomery: District 1	50,000	40	Ð
Collingsworth Collin Comal Concho¹ Cooke District 1 Culberson Dallas Denton: District 1.	1,990 100,000 50,000 1,390,000	40	5	trict 1	250,000	40	5
Dallac	1.390.000	40	$\frac{4^{1}}{2}$	Motley	25,000	10	
Denton: District 1	75,000	40	5	Motley Navarro: Districts 1			
Dewitt Dewitt Dickens. Dimmit Ellis Ells Fals.	75,000 31,998 11,500			and 3	475,000 100,000	40	5
Dickens	11,500	20-40	5	and 3 Nolan	100,000	40	5
Dimmit	30 000			Nueces. Orange. Palo Pinto.	175,591		
Ellis	800,000 617,000 100,000			Orange	200,000	1	5
El Paso	617,000	40	4	Palo Pinto	9,750 25,000		
Falls	100,000		3	Parker	25,000	4	4
Fannin Fayette Fisher Foard	1,900		4	Polk Potter Reeves	40,000 20,000 12,000	4	5
Fayette	69,500 19,900 83,000		5	Potter	20,000		5
Fisher	19,900		4	Polygie: Districts 1	12,000		9
Foat Dand	420,000		3½-5 4-5	and 2	50,000		4
Fort Bend	420,000 500	2-50	4-5 4½	Refugio: Districts 1 and 2. Robertson Runnels.	500,000		4
Freestone: District 1.	50,000	2-30	5	Runnels	500,000 57,094		5
Frio	86,953	40	5.	San Jacinto	3.000		5
Galveston	1,500,000	40	5	San Patricio	148,000		4-5
Garza	50,000	40	4	San Saba	38, 750		4
Gonzales: District 1	50,000 160,000		5	San Jacinto San Patricio San Saba Shackleford	148,000 38,750 12,500	40	4-5
Gonzales: District 1 Grayson: Districts 1				Sherman	7 (101)		
and 9	685,000	2-50	41/2	Smith	405,000	40	5
Gregg Grimes Guadalupe Hall. Hamilton	50,000 134,000 239,500 65,000 22,994 43,500			Smith Somervell Stephens Sterling Stonewall Sutton	405,000 16,950 18,000	20	5
Grimes	134,000	20.40	4-5	Sterling	18,000	40	
Hall	239, 500	30-40	4-41-5	Stonewall	10,000 50,000 12,000	40	4
Hamilton	22,004	5-20	4-6	Sutton	12,000		31
	43 500	0-20	4-0	Tarrant	1,834,000	20-25	4-5
Hardin	169,000		5	Taylor: District 1	150,000	20-20	5
Hardin Harris. Haskell ¹	169,000 1,508,000 16,000			Throckmorton	2,000		
Haskell 1	16,000			Tom Green 1 Travis Trinity: Districts 1 and 2	2,000 96,000	10-40	5-6
Hays: District 1	87,000		5	Travis	482,000		4
Hemphill	10,000 100,000		6	Trinity: Districts 1	, , , , , , , , , , , , , , , , , , ,		
Hidalgo	100,000			and 2	160,000	40	5
Hays: District 1. Hemphill Hidalgo Hill	102,000	40-45		Upsnur	149,000		
Precinct 1. Hood. Hopkins. Houston: Districts 1	250,000	40	5	vaiverde	6,000 200,000 25,000		
Hood	36, 499 5, 963	10	4-5	Victoria: District 2 Waller	200,000		5
Houston: District	5,963	40	6	Waller	25,000	40	4-5
and 3	174 000		5	Walker	15,000	40	0
and 3. Howard	100,000		5	Ward	150,000		
Irion	174,000 100,000 20,000	40	51	Webb	5,000 10,000		6
Jackson	124, 500		4-51-6	Waller Walker Ward Webb. Wharton Wheeler ¹	320,000		3-41-5
Jackson Jefferson	124,500 809,500	40	$\begin{array}{c c} 4-5\frac{1}{2}-6 \\ 4\frac{1}{2}-5-6 \end{array}$	Wheeler 1	15,000		4

¹ Bridge bonds only.

Table 22.—County and district highway and bridge bonds—Continued.

TEXAS—Continued.

Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interes
Wichita Wilbarger Williamson	\$15,000 75,500 300,000		Per ct.	YoungZavalla 1	\$83,996 44,999	40	Per ct. 4-5
Williamson Wood	150,000		4½-5 5	Total	24, 960, 837		
			UT.	AH.			,
Boxelder	\$175,000	20	4½	San Juan	\$14,500	20	
Cache	45,000		4	Uinta Weber	8,000 120,000	20	5
Carbon 1	. 30,000	20	5 5-6	Weber	120,000	20	4-5
Carbon ¹ Emery	45,000 30,000 39,500 8,500	20	5	Total	440, 500		
	1	1	VIRG	INIA.	1)
Accomae: Atlantic,				Northampton: 1 dis-		:	
and Lee	\$100,000		5-51/2	triet	\$50,000	30	43-
Alleghany ¹ Amherst	40,000			Orange	175,000		
Amherst	215,000	20-30	4½-5 5	Page 1	26,000		
Augusta: South River Botetourt 1	250, 000 10, 000 84, 000 100, 000	30	9	River	100,000	34	
Brunswick	84,000			Pulaski:	100,000	01	
Brunswick Charlotte	100,000		41/2	Dublin	100,000		1
Clarke 1	90,000		$4\frac{\tilde{1}}{2}$	Pulaski	70,000	34	
Culpeper:	120,000	34	5	Rappahannock: Wakefield	30,000		
Catalpa Stevensburg	45,000	34	5	Hampton	36,000		
Dickenson:	′		0	Piedmont	28,000		
Clintwood	54,000	2-30	5	Rockingham: Plains .	36,000 28,000 30,000 575,000	10	
Kenady	32,000	2–30 1–30 20–30		Russell	575,000		
Dinwiddie Elizabeth City	54,000 32,000 105,000 30,000	20-30	5-6 5-6	Scott: Esterville	100,000	20-30	
Fairfax: Mt. Vernon	90,000			Fulkerson	33, 800	20-50	
Fauquier: Centre	75,000			Johnson Smyth: Marion, Rich	33,800 33,300	20-30	
Fluvanna	1,300			Smyth: Marion, Rich			
Giles 1	30,000 80,000			Valley, and St. Clair	325,000		5-
King George	10,000			Spotsylvania:	525,000		0-
Lee:	,			Courtland a n d			
Jonesville and 7				Chancellor	100,000	30	
districts Lunenburg:	440,000	6-36	$5-5\frac{1}{2}$	Berkeley and Liv- ingston.	100,000	30	
Plymouth	40,000		51-6	Stafford	100,000	30	
Rehoboth	24,000		$5\frac{1}{2}-6$	Tazewell	625 000		
Browns Store	40,000		$5\frac{1}{2}$ -6	Warren: 3 districts	90, 000 200, 000 25, 000 960, 000		
Mecklenburg: 7 dis-	350,000		5	Washington Westmoreland	25,000		
tricts Montgomery	30,000			Wise	960,000	30	
Nelson	35,000		7				
Norfolk	200,000		$4\frac{1}{2}$	Total	6,632,400		
			WASHI	NGTON.			
	000			0.7	01-01-	-	1
Asotin	\$35,000		41 6 7	Okanogan	\$15,000		
Chillem	401,000		41-6-7	Carl arish	100,000	20	
Clallam	500,000	1					
Clallam Clarke ¹	500,000 69,262			Delta	75,000		
Clallam	500,000 69,262 133,000		$\frac{5\frac{1}{2}}{}$	Pacific Snohomish Delta Total	\$15,000 100,000 80,000 75,000 4,408,262	20	

¹ Bridge bonds only.

Table 22.—County and district highway and bridge bonds—Continued.

WEST VIRGINIA.

		,					
Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and districts.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Barbour Cabell Hancock: Baxter and Grant. Butler Harrison Logan ¹ Marion: Fairmont Mannington	\$40,000 300,000 225,000 125,000 110,000 60,000 400,000 300,000	20 30 30	Per ct. 4 4½ 5 5 5 5	Marshall Monongalia Pleasants: St. Marys. Tyler: Ellsworth Lincoln Wetzel: Grant Wood: Parkersburg.	\$150,000 75,000 60,000 125,000 200,000 150,000 180,000 2,500,000	10-34 10-34 34 30	6 6 6 4 ¹ / ₂
			WISCO	ONSIN.			
Ashland	\$50,000 20,000 38,000 35,000 11,000	20 10 6	4 4 5 4	Sauk ¹ Vilas Total	\$40,000 60,000 254,000	20 20	41/2

¹ Bridge bonds only.

Table 23.—Township highway and bridge bonds.

CONNECTICUT.

Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Fairfield: Easton. New Canaan. Stamford ' Wilton. Hartford: Plainville West Hartford Windsor Litchfield: Barkhamsted North Canaan.	\$25,000 14,000 96,000 35,000 20,000 45,000 40,000 16,000 23,000	40 30 20	Per ct. 3\frac{1}{2} 4 4 4 3\frac{1}{2} 3\frac{1}{2} 3\frac{1}{2}	Middlesex: Chatham. East Haddam. New Haven: Derby. New London: Mont- ville. Windham: Brooklyn. Plainfield. Total.	\$70,000 44,000 60,500 30,000 28,000 30,000 576,500	20	Per ct. 4 3½ 3½ 4 4 4

ILLINOIS.

Counties and town- ships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and town-ships.	Total amount voted to Jan. 1, 1914.	Term of years.	Intorest rate.
Adams: Melrose Bond: Central Bureau: Greenville. Ohio. Carroll: Fairhaven Woodland Wysox Champaign: Colfax. Christian: Mount Auburn Clark: Anderson. Westfield 1.	\$8,000 6,000 2,700 17,500 2,000 23,954 38,500 4,400 6,000 3,000 2,250	10 1-5 4-6	Per ct. 5 5 5 5 41 2 5 41 2 5 6	Clay: Stanford	\$900 5,000 3,105 200 15,000 60,000 12,000 58,479 43,100 95,000 2,500	10 8 5 20–25 20–25 20–25	Per ct. 5 4½ 4 5 5 5 5 5
York	3,000		5	Dekalb: Malta	8,500	2	5

¹ Bridge bonds only.

² Of this amount, \$1,200 for bridges.

Table 23.—Township highway and bridge bonds—Continued. ILLINOIS-Continued.

		11.	LINOIS-	-Continued.			
Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Douglas:			Per ct.	Lee-Continued.			Per ct.
Boudre	\$35,000	1 13	5	Hamilton	\$12,800		5-6
Sargent. Dupage: Naperville	35,000	2-7	5	Harmon	⁸ 9, 125		5
Edger:	2,300			Viola	13,000	1-13	5½ 6
Edgar: Elbridge	2,500		6	McLean: Martin Macoupin: Bird Madison: Godfrey	2, 200 8, 000		
Emparrass	35 000	10	5	Madison: Godfrey	1, 200		
Hunter ²	1.500		5	Montgomery:			
Paris. Effingham: Mason	1,500 35,000 10,000		5	Montgomery: Hillsboro	16,000	1 5-8	
Ford: Button	2,500		6-10	Witt Moultrie:	2,200		6
Franklin:			0	East Nelson	3,500		- 5
Browning	4,500 350		6	Lovington 2	7,375		6
Northern. Fulton: Orion ²	350		4	Ogle:			_
Gallatin:	7,000		5	Maryland	4,500	13	5 5
Bowlesville	1,000	1-2	4	Pine Rock Rockvale	2,000 9,000	10	5
Equality	4,000		6	Woosung	15,000		
Snawnee	7,000	1–5	4	Peoria:			
Greene: Woodville	250		4	Jubilee	2,000 7,000	8	5
Grundy: Goose Lake	2,500		5	Timber 2	1,500	8	5 6
Maine 2	5,500		5	Pike:	1,000		. 0
Maine 2 Wauponsee 2	3,300		5	Derry 2	3,075		51/2
Hancock:	1			r an mount,	300		
Appanoose	1,835		5	Hadley Hardin	525		
Hancock	6,550		5-51	Kinderhook	1,200 700		
Alha 2	3,500	6	5	Kinderhook Pleasant Hill	1,200		
Atkinson Geneseo ² Loraine ² Phenix	5,900	10	5 5	Richland: German	1,798		6
Geneseo 2	15, 450	3-19	5	Rock Island: Black			
Loraine 2	2,100 4,250		5 5	Hawk St. Clair:	5,500		, 6
Yorktown	2,500		5	Centerville	2,500		
Troquois:				Centerville Fayetteville	2,000 7,400 8,000		
Belmont. Chebanse ² . Milford ² .	6,000 4,000		5 5	Freeburg. New Athens 2 O'Fallon. St. Clair 2 Shiloh Valley.	7,400	10	
Chebanse 2	4,000		5	New Athens 2	8,000	12	4-5
Pigeon Grove	10,000	10	6	St Clair 2	6,000 3,200	4	5 5
Sheldon	5,000 37,500		5	Shiloh Valley	9,550	15	4-5
Jackson:				Saline:			
Carbondale	35,000	3-5	5	Brushy	1,500		5
De Soto	7,325 1,250		6 5	Galatia	1,694	3	6
Sand Ridge	3,900		41	Harrisburg 2	1,400 6,215 800		
Jasper:	1		~	Galatia Harrisburg ² . Independence ² . Mountain	800		6
Grove	500			Mountain	2,372 2,000		6
Wade Jefferson:	478			Raleigh Stonefort Sangamon: Salis- bury ²	5,000		6
Blissville 2	1,000			Sangamon: Salis-	0,000		
Blissville 2 Farrington 2	1,000			bury 2	6,000	5	5
Jo Daviess:	1 500			Stephenson: Jefferson	2 000		5
Derinda	1,500 2,500			Waddams	3,000 6,000		
ElizabethPleasant Valley	2,500 10,000		5-6	Tazewell:	0,000		
Kankakee:				Hopedale 2	1,142	4	
Ganeer	35,000			Mackinaw 2	9,000		51
Momence. Yellowhead. Knox: Haw Creek	35,000 35,000 2,500			Tremont Vermilion:	6,500		5
Knox: Haw Creek	2,500		5½	Cront	15,777		
La Salle:				Jamaica. Middlefork. Washington: Bolo	6,500		
Deer Park	22,000		51-6	Middlefork	5,000		
Farm Ridge	1 - 2,000			Washington: Bolo	240		
Mission Utica	3,750 26,500		5	Wayne: Big Mound	11,600		6
Lake:	20,000		51/2	Leech 2	4,000	5	6
Antioch	4,000		5	Massilon	4,000 46,125	5	6
Newport	9,325	28	4-51	White:			1 0
Lawrence:		1	2	Burnt Prairie Emma	11,000 25,000		6 5
Bond Denison	6,150		6	Hawthorne	27,500		5
Demson	35,000	6	5	Mill Shoals	25,000 27,500 5,000	1-10	
Lee:	1	00	_	Whiteside:		1-	
Ashton China East Grove ²	44,000 25,000	20	5	Newton	5,820 15,000	11 16	
China							

¹ Serial. ² Bridge bonds only.

Of this amount, \$3,000 bridge bonds.
 Of this amount, \$3,125 for bridges.

Table 23.—Township highway and bridge bonds—Continued.

ILLINOIS—Continued.

Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Will: Channahon Crete Custer. Dupage. Winnebago: Cherry Valley. New Milford.	\$5,500 35,000 3,000 1,500 12,325 17,725	13 3	Per ct. 5 5 5 5 5 5 5 5 5 6 6 6 2	Winnebago—Contd. Roscoe. Woodford: Patridge. Spring Bay Total.	\$35,000 1,300 2,700 1,618,634	5	Per ct. 5 6 5

INDIANA

			INDI	ANA.			
4.2	e1 000 201	(9)	41	Wasting Massachine	67.40.070	1 10	
Adams: Townships	\$1,026,321	(2) 1-20	$\frac{4\frac{1}{2}}{4\frac{1}{2}}$	Martin: Townships	\$148,870	1-12	
Allen: Townships	134, 132	1-20	42	Miami: Townships Monroe: Townships	504, 530	10-20	41-5
Bartholomew: Town-	780, 180	10	41	Montgomery: Town-	599, 465		$3\frac{1}{2}$
ships Blackford: Town-	100,100	10	42	shine	849,820		47 6
	1 249,063	10	41	ships Morgan: Townships	393, 689		41-6
ships Benton: Townships	723, 560	10	41-6	Newton: Townships.	456, 125		$\frac{4\frac{1}{2}}{4\frac{1}{2}-6}$
Boone: Townships	127, 150	10	41	Ohio: Townships	20,078		42-0
Carroll: Townships	1,016,686	3 10	41	Orange: Townships	1 170, 541		
Cass: Townships	1 692, 158	10	12	Owen: Townships	394, 089	40	41-5
Clark: Townships	1 213, 138	3 10	41	Parke: Townships	893, 367	10	41/2
Clay: Townships	1,004,354	10	41-6	Perry: Townships	73,000	20	41/2
Clinton: Townships	850,000	10	41	Pike: Townships	152, 296	20	42
Crawford: Townships:	71,806	1	41-5	Porter: Townships	1 725, 516		
Daviess: Townships	934, 988	3 1-20	41	Posey: Townships	1 473, 231		
Dearborn: Town-			-3	Pulaski: Townships.	1 270, 229		
ships	219,330	1-20	43	Putnam: Townships.	757,005		$4\frac{1}{2}$
Decatur: Townships.	779,583	10	41	Randolph: Town-	101,000		12
Delaware: Townships	850,000	10	4-5	ship	1 517, 176		$4\frac{1}{2}$
Dubois: Townships	216, 400		41-6	Ripley: Townships	1 259, 366		-2
Favette: Townships	1 39, 609		43	Rush: Townships	625, 742		43-53
Fountain: Townships	425,000	10	41-6	Saint Joseph: Town-	,		-2 -2
Franklin: Townships.	173,820	10	31-6	ships	1 23, 500		
Gibson: Townships	808, 770	10	$4\frac{5}{2}-5\frac{1}{2}$	Scott: Townships	108, 856	10	41/2
Grant: Townships	760, 702	10	43	Shelby: Townships	166, 805	20	43-6
·Greene: Townships	861,062		41	Spencer: Townships.	1 37, 300		41-6
Hamilton: Townships	525, 836			Sullivan: Townships.	1, 215, 564		$4\frac{1}{2}-5$
Hancock: Townships.	255, 065		41-5	Starke: Township	1 254, 429		
Harrison: Townships.	202, 887		41-5	Switzerland: Town-	<i>'</i>		
Hendricks: Town-				ships	160,019		$4\frac{1}{2}-5$
ships	315, 846		41/2	Tippecanoe: Town-			
Henry: Townships	47,408		$4\frac{1}{2}$	ships	1 273, 930		$4\frac{1}{2}$ -6
Howard: Townships.	736,000	10	$4\frac{1}{2}$	Tipton: Townships	1 76, 372		
Huntington: Town-				Union: Townships	79, 711		$4\frac{1}{2}$
ships	1 301, 289	10	$4\frac{1}{2}$	Vanderburg: Town-	1 107 000		
Jackson: Townships.	1 230,000			ships	1 137,600		$4\frac{1}{2}$
Jasper: Townships	1 237, 195	10	41	Vermilion: Town-	1 292, 132		
Jay: Townships	310, 828	10	41 5	ships	601, 222		
Jefferson: Townships	135, 119	20	41-5	Vigo: Townships	784, 220	1-20	41
Jennings: Townships Johnson: Townships.	417, 210	10	41-5	Wabash: Townships. Warren: Townships.	1 402, 270	1-20	$4\frac{1}{2}$
Knox: Townships	127,025	10	$\frac{4\frac{1}{2}}{4\frac{1}{2}}$	Warrick: Townships .	78, 163		41
Kosciusko: Townships	1 824, 496	10	42	Washington: Town-	10, 100		$4\frac{1}{2}$
ships	1,440			ship	1 232, 799	10	$4\frac{1}{2}$
Lake: Townships	1 1, 766, 211			Wayne: Townships	410, 940	10	41
Laporte: Townships.	1 654, 320	3 20	41	Wells: Townships	1 473, 660	10	42
Lawrence: Townships.	- 004, 020	20	*2	White: Townships	1 385, 680		
ships	1 384, 630	10	41/2	Whitley: Townships.	1 8, 369		
Madison: Townships.	849,820	10	12	" Hittey: Townships.	0,000		
Marion: Townships.	1 40, 735			Total	35, 837, 348		
Marshall: Bourbon	1 28,500	15	43	200021111111111111111111111111111111111	25,001,010		
The state of the s	20,000		-2				

¹ Outstanding Jan. 1, 1913.

² Six months.

³ Serial.

Table 23.—Township highway and bridge bonds—Continued.

KANSAS.

Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Allen: Iola	\$33,000		Per ct.	Mitchell: Pittsburg 1. Neosho: Mission	\$26,000 32,000		Per ct.
Barton: Lakin 1	20,000		6	Ottawa: Center	9,500		7
Liberty 1. Butler: Douglass	6,000 9,000 150,000		4-41	Pottawatomie: St. Mary's	40,000		41/2
Cherokee: Shawnee		10.00	0.10	Womego Riley: Manhattan Rush: Belle Prairie	40,000 35,000 12,200		6
Lincoln ¹ Shirley	18,700 1,565	10-30	6-10	Sedgwick: Payne	5,000		6 5
Comanche: Township	1,565 2,000 54,000			Wabaunsee: Kaw Wilson:	9,000		5
Douglas: Grant. Finney: Garden City.	2,500 16,000 2,500 89,600		6	Center Clifton	7,000 2,100		6
Franklin: Cutler 1 Geary: Junction City.	2,500 89,600	9-10	5-6	Clifton Fall River Guilford	2,100 4,900 10,000		
Kingman: Bennett	18,000	30	$\frac{5}{5\frac{1}{2}}$	Neodesha Wyandotte: Town- ship	12,000		
Kiowa: Glick 1 McPherson: Town-	5,000				5,000		
ship Marshall: St Bridget	6,000 15,000		5	Total	677,065		
			MAI	NE.			
Kennebec; Benton	\$1,500	5	4	Waldo: Frankfort 1	\$1,000		5
Knox: Vinal Haven Oxford: Norway 3	2,500 35,000 12,000	35	4	Washington: Jones- port	1,000	6 mos.	6
Penobscot: Orono 1 Piscataquis: Foxcroft ¹	12, 000 25, 000	2-3-4 1-25	4 4	Total	78,000		
		1	MASSACE	IUSETTS.			
Barnstable:	\$40,500		4	Franklin—Con. Northfield ¹	\$30,000		31/2
Brewster	15,000 63,400		51/2	Sunderland Hampden:	2,500		4
Harwich ¹ Mashpee	400		4	Russell	14,000	10	4
WellfleetBristol:	24,000	42	31-4	Westfield	100,000 50,000		4 4
Fairhaven ¹ North Attleboro	42,000 6,000	1-6	5	Nantucket: Nan-		10	4-41/2
Somerset 1 Swansea	8,000 4,000		4	tucket Norfolk: Millis 1 Plymouth:	36,000 5,856	10	4
Amesbury	16,000		4	East Bridgewater	5,000 100,517		4
Marblehead Franklin:		10	4	Plymouth Worcester: Grafton	3,800		4-41/2
Conway Gill Monroe ¹	15,000 4,500 1,000	10	4-4½ 4	Total	650, 473		
			MICH	IGAN.	1		
					-	1	
Alcona: Mikado Allegan:	\$2,000		5	Benzie: Crystal Lake. Berrien: 3 townships.	\$20,000 89,000	5	
Gunplain Saugatuck	20,000 18,000		$\frac{4\frac{1}{2}}{4\frac{1}{2}}$	Branch: Union Charlevoix: Hudson ¹ Cheboygan:	10,000 1,100	5	5 7
Antrim: Banks	20,000	20	5	Benton	10,000		5
Central Lake Arenac: Au Gres	20,000 1,550			Walker	7,000 5,000		6 5
Baraga: Arven	10,000			Chippewa: Sugar Isle	2,000		6
Covington	10 000			Tront Tales	10,000		
L'Anse	25,000		6	Trout Lake Clare: Redding	3,000		5

Table 23.—Township highway and bridge bonds—Continued.

MICHIGAN-Continued.

Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Crawford: 2 town-			Per ct.	Midland—Continued.			Per ct.
ships	\$16,000		2 07 00.	Larkin	\$1,413		
Delta: Bark River	12,300	10	5	Mount Haley	1,000		5
Escanaba	5,000	5	5	Butterfield	4,000		6
Ford River	3,000 10,000		5 5	Clam Union ¹ Pioneer	800 6,000	3-9	5
Dickinson: Norway	8,000		5	West Branch	3,000		
Genesee: Davison	8,300		$5\frac{1}{2}$	Monroe: Bedford.	39,000	13	5
Forest. Montrose Thetford.	10,000 7,000	6	4 5	E110	40,000 30,000	20	5
Thetford	10,000	10	5	IdaWhiteford	60,000		5
Vienna	10,000 3,500		5	Montcalm: Eureka	725	10	5
Gladwin: Bourret Gogebic: Marenisco	20,000	20	5 7	Montcalm	1,045		
Grand Traverse:	30,000			Reynolds Newaygo:	10,000		5
mulewater	24,000			Engley	1,200		5
Green Lake Hillsdale: Fayette	18,000 3,450	1	5	Grant	7,500 20,000		5
Houghton: Chassell	3,000		6	Four townships	39,000		
Huron: Bingham	2,000			Oceana: Elbridge	20,000	21	5
Bingham Bloomfiel Brookfield Colfax Oliver Sebewaing Windsor	2,000		6	Golden. Greenwood ¹ . Hart.	19 500		5
Colfax	20,000		5	Hart	1,267	3	6
Oliver	12,000 75,000		5	Pentwater Shelby Weare	20,000	20	6
Windsor	50,000	10	$\frac{4^{\frac{1}{2}}}{4^{\frac{1}{2}}}$	Weare	3,000		5 5 5
Ionia:	12,000		5	Ogemaw: Cumming	5,000	20	5
Ionia Lyons ¹ Isabella: Vernon	12,000		5	Ontonagon: Ontonagon	10,000		
Isabella: Vernon Iron:	6,000			Carr Lake McMillan	20,000 9,500		
Crystal Falls	15,000		5	Rockland	28, 500		
Mastadon Kalkaska:	20,000			Osceola: Burdell	10,000		
Clearwater	6,000			Evart. Hartwick.	14,000 8,000	20	5
Cold Springs Springfield	5,000 9,000			Hartwick	8,000 6,000		5 5
Lake:	1			Hersey ¹ Lincoln Marion	5,000		5555555757
Ellworth Newkirk	6,000 6,000		5 5	Marion Osceola	12,000 25,000	15	5
Leelanau:				Osceola Otsego: Hayes	600 8,000		7
Empire Leelanau	11,000		5	Ottawa: Robinson Presque Isle: Allis	2,800	16	5
Townships (3) Mackinac:	26,000			Roscommon:			5
Garfield	8,903		5	Gerrish Richfield	15,000 18,500	25	5
Hudson Newton	4,000 5,000		5	Sagmaw: Blumfield	10,000		4
Macomb:	1			Bridgeport	20,000		
Lake Warren	50,000 36,000			Bridgeport	10,000 20,000		$\frac{4\frac{1}{2}}{4\frac{1}{2}}$
manistee:	1			St. Charles	10,000		5
Maple Grove ¹ Springdale	1,100 10,000		7	Spalding St. Clair:	5,000		-
Springdale Stronach Meropette:	500		5	East China 1	3,000 25,000		5 4
Marquette: Powell	30,000			Kimball Sanilac:			
Wells	0.000		5	Forrester	5,000 5,000	10	5 5
Mason:		1 '		Schoolcraft:			
Custer Free Soils	20,000 15,000			Hiawatha 1	4,000 6,000	9	6 5
Riverton. Menominee: Stephen-	20,000			Tuscola:			
Menominee: Stephen-	11,000			Ellington	3,832 20,000		6
son	0,000			Fairgrove Wellington	4, 500		
Edenville ¹ . Greendale ¹ . Ingersoll Jerome.	9,000		5 4½	Van Buren: Covert	25,000	5	5
Ingersoll	10,000	11	5	Covert	25,000	5 5	5
Joi Oine	6,500	'		" Washiellaw: Salem	5,000	1	

¹ Bridge bonds only.

Table 23.—Township highway and bridge bonds—Continued.

MICHIGAN-Continued.

Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Wayne: Redford Wexford: Antioch Cherry Grove Greenwood	\$50,000 2,000 5,000 5,000	20-30	Per ct. 4½ 5	Wexford—Contd. Henderson. South Branch. Total.	\$2,000 2,000 1,926,135		Per ct.

MINNESOTA.

Aitkin:				Goodhue:			
Cornish	\$6,000		4	Central Point 2	\$500		5
Fleming	1,200		4	Vasa 2	4,800		5 5
Haugen	7,000		4-6	Houston: Yucatan 2	2,500	5	5
Hebron	3,500		6	Hubbard:	2,000		,
Jevne	4,000	20	4	Alice	3,000	1 10	4
Jewett	3,500		6	Badoura	200	- 10	4
Pequadna	3,000		- 6	Farden	1,200	10	4
Pliny	4,000	19	4	Guthrie	1,000	6-10	4
Verdon	1,000		6	Hart Lake	1,000		4
Wagoner	5,000		4	White Oak	3,000	5-20	4
Wealthwood	7,300		6	Isanti: Stanford 2	500		
Williams	7,000		4	Itasca:			
Workman	5,000		6	Alvwood	2,000	5	4
Becker: Spring Creek.	1,500		4	Ardenhurst	3,500		4
Beltrami:	9,000	6	4	Balsam	20,000		6
Eland Kelliher	2,000 7,000	0	6	Bass Brook	15,000	4-15	$5\frac{1}{2}$
Wabanica.	3,500		4	Bigfork	8,000	20	6
Benton:	5,000		4	Deer River	12,000		6
Alberta	1,100			Feeley	3,000	20	6
Longola	3,000	1 18	4	Grand Rapids	10,650		5
Watab	1,500		6	Marcell	10,000	20	6
Bigstone: Otrey	2,150	5	6	Trout Lake	8,500	3-21	6
Brown: Prairieville 2.	2,000		6	Jackson:			
Carlton:	,			Enterprise 2	3,000		4
Barnum	2,200	15	5	Sioux Valley	3,600		4
Beseman	8,000		6	Kanabec:			
Blackhoof	3,000	15	4	Kroschel	3,400		4
Carona	1,500			Pomrey	4,100	11	4
Eagle	3,000		4	South Fork	1,500		4
Holyoke	10,000	15	6	Hillman	3,000	10	4
Kalavala	3,000	15	4 7	Kandiyohi: Lake			
Knife Falls	3,000	10-15 20	6	Elizabeth	550		
Lakeview	9,603 3,000	20	4	Davis	1 000	10	6
Red Clover	3,500	13	4	Hallock	1,000 $12,300$		4-7-10
Split Rock.	3,000	13	4	Percy	3,500		43
Chippewa:	0,000	10	-	Red River	1,100	10	72
Crate	5,000	5-20	4	St. Vincent	3,000	1	4
CrateLone Tree 2	3,000	20	3	Spring Brook	1,400	5-11	4
Chisago:	-,			Svea	1,000		4
Rushseba ²	600	7	6	Teien 2	6,090		4
Sunrise 2	5,000	6	4	Thompson 2	7,800		4
Clay:				Koochiching:			
Felton	6,500		4	Bannock	3,000	10	. 4
Flowing	1,000		6	Cingmare	12,000		6
Morken	4,500	19	10-7	Dinner Creek	3,000		4
Cook:	10.000			Englewood	2,000	1 1-20	4
Colvill	12,000 15,000		6	Forest Grove	2,000	6-16	4 6
Hovland	20,000	(1)	6	Jameson	1,500 10,000	20	6
Maple Hill	15,000	(-)	6	Koochiching	15,000	20	6
Schroeder	8,000	14	7	Lindford 2	3,000	12	4
Cottonwood: Rose	5,000	1.4	'	Lindford 2 Meding	7,000	10	4
Hill?	2,000		4	Pine Top	5,000	10	6
Crow Wing: Little-	-, -, -			Reedy	6,000	10	4
pine	3,000	5	4	Sturgeon River	3,000		6
Dakota:	,			Wildwood	8,000	4-11	6
Randolph 2	2,360		5-6	Lac Qui Parle:	., 500		
Waterford 2	2,500	4	5	Mehurin	2,400		4
Dodge: Ashland	2,650	1	6	Ten Mile Lake	50, 400		4
Douglas: Belle River.	2,300		5-7	Lake:	0.500		
Fillmore: Pilot	F 500		0	Two Harbors	2,500		
Mound	7,500	1	6	Waldo	3,500	1	4

¹ Serial.

² Bridge bonds only.

Table 23.—Township highway and bridge bonds—Continued.

MINNESOTA—Continued.

		22221	1120011				
Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Lincoln: Diamond			Per ct.			4	Per ct.
Lake	\$500		reret.	Pope: New Prairie 1.	\$800		
Lyon: Eidsvold 1	1,025			Ramsey: White Bear.	12,500		
McLeod:				Red Lake:			
Collins	3,000 1,000		4 6	Lake Pleasant Terrebonne	1,000 1,700		5
Mahnomen:	1,000		U	Redwood:	1,700		
Beaulien	1,000		4	Brookville	3,000	5-10	
Bejou Heier Townships	1,500	20		Sundown. Renville: Crooks	4,000		7
Townshins	1,000 6,600		4	Rice:	2,500		5
Marshall:				Bridgewater 1	3,000	5	5
Alma	1,200	5-9	4	Flora	2,000	5	4
Big Woods Donnelly	1,400	5 10	8 7	Rock:	1,600		6
Lincoln	1,000 6,000	20	6	Denver Kanaranzi	3,500		6
Vega	1,300		4	Luverne	2,500		6
Vega	1,000	20	4	Luverne. Springwater 1	8,000		6-8
Millelacs: Bogus Brook 1	2 200		4	Roseau; Cedarbend	1 700		4
East Side	2, 200 1, 500		4	Deer	4,000	20	6
East Side Kathio	12,000	20	4	Dieter. Grimsted.	1,700 4,000 9,500 6,000		6
Onamia	4,000		4	Jadis	6,000 6,000		
Page South Harbor	3,000	(2)	4 4	Lind	1 600		6
Morrison:		()		Malung. Mickinock.	1,000		6
Hillman	4,000	14	4	Mickinock	6,600		6
Rosing 1. Murray: Des Moines	800	€-13	6	Moose. Pohlitz	8,600 5,000		6-7
River	1,200		4	Ross	10,000	10	6
River Nicollet: Belgrade Nobles: Townships	4,000	10	6	Spruce	5,000		. 6
Nobles. Townships	5,700	10	4	Ross. Spruce. Stafford. Stokes. St. Louis:	5,900	5	4-6
Norman: Anthony 1	500		4	St. Louis:	9, 500	20	6
Good Hope. Hegne. Olmsted: Rochester	3,000		6	Ault	0,000		6
Hegne.	800	5-10	10	Beatty	3,000		4
Olmsted: Rochester Ottertail:	1,769		41/2	Canosia	10,000 3,000	10-15	10
Buse 1	1,058		6	Mesaba	15,000		51/2
Buse 1. Eagle Lake. Maine.	400			Mesaba Scott: Belleplaine	1,500	3	5
Maine	2,000 1,000			Sherburne: Elk River	= 000		6
PaddockPennington;	1,000			Livonia	5,000 1,000		
High Landing	3,000		6	Talmer. Sibley: Dryden	2, 400 1, 000		5
Rocksbury	1,500	10	10	Sibley: Dryden Stearns:	1,000		
Pine: Arna.	2,000		5	Brackway	1,500		4
Brooknark	5 540		4	Grove	1,800		6
Bruno. Chengwatana ¹ Danforth.	14,000		51-6	Grove. Paynesville. Steele: Lemond.	3,000		41/2
Unengwatana 1	3,000 4,000		4 4	Stevens: Baker	1,400		6
Fleming	10,000	13	6	Todd: Little Elk	5,000	7-16	4
Fleming Kettle River	3,600			Wadena.			
Mission Creek	5 (100)		6	Bullard. Huntersville	1,500	(2)	4
Partridge Pine City ¹ Pokegama Rockcreek	2, 400	6-13	4	Orton	2,500 3,000	1	4
Pokegama	2, 400 1, 700 1, 600	10	4	Orton. Wing River 1. Washington: New-	1,900	9	
Rockcreek	1,600		4	Washington: New-	00 000		-
Wilma Pipestone: Sweet	2,500 2,500		4	port Watonwan; Adrian	20,000 3,000	2 5	5 5
Polk:	,			Wilkin: Andrea Wright: Townships	2,000		5
Fairfax	3,500	5-15	4	Wright: Townships	3,000		4
Gentilly	12,000 1,000	5	4 4	Yellow Medicine:	4,000		4
Nesbit.	5,000	20	6	Oshkosh ¹ Wright	3,000		4
Farrax Farley Gentilly Nesbit Sandsville Sullivan Tabor	1,000 14,000	10	10				
Sullivan Tabor	14,000 1,300		4-10	Total	982, 805		
2.4.001	1,500						

¹ Bridge bonds only.

Table 23.—Township highway and bridge bonds—Continued. MISSOURI.

·			
Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Nodaway: Polk	\$50,000		Per cent.
Union	15,000	(1)	6
Total	65,000		

NEBRASKA.

Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Dawson: Lexington Keith: Ogallala. Lincoln: Bostwick Hershey Merrick: Loup Morrill: Township Nance: Genoa Township Platte: Columbus	\$6,000 26,670 4,000 20,000 3,000 14,000 82,500 14,000	20	Per ct.	Platte—Continued. Loup Oconee 2. Scotts Bluff: Castle Rock and Highland Gering. Winter Creek. Total.	\$3,000 6,000 12,000 10,000 15,000 246,170	15 15	Per ct. 6 6

NEW HAMPSHIRE.

Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Grafton: Bristol	\$15,000 25,000 40,000	20	Per cent.

NEW JERSEY.

Interest rate.	Term of years.	Total amount voted to Jan. 1, 1914.	Counties and townships.	Interest rate.	Term of years.	Total amount voted to Jan. 1, 1914.	Counties and townships.
Per ct.		\$7,000	Camden: Delaware	Per ct.	8–13	\$95,000	Atlantic: Egg Habor
• 5		6,000	Gloucester	42	8-13	97,000	Hamilton
5		2,900	Haddon			91,000	Bergen:
5		2,500	Voorhees	4		75,000	Franklin
5		5,000	Cape May: Lower	5	5	45,000	Hillsdale
4		87,000	Essex: Belleville	41-5			Hohokus
			Gloucester:	5		30,000	Midland
5		500	Monroe	5 5		7,000	Orvil
5		3,900	Wollwich	5		75,500	Overpeck
(1		4 000	Hunterdon: West	5	31	25,000	Riverdale
41 5					30		Washington
$4\frac{1}{2}-5$		25,000		6.		14,500	
ă		900		41		40.000	
5					30		
			Cilibia Cidillordi		00		Pemberton
		760,600	Total	41	30	15,000	Southampton
		4,900 23,000 8,600 760,600	Amwell Monmouth: Neptune. Salem: Upper Pitts- grove Union: Cranford Total	4 5 4½ 4 4½ 4½ 4½	30	42,500 14,500 40,000 15,000 10,000 15,000	Union Washington Burlington: Chester Northampton Pemberton Southampton

¹ Serial bonds.

² Bridge.

³ Bridge bonds.

Table 23.—Township highway and bridge bonds—Continued. NEW YORK.

Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
4.33			D	Jefferson—Contd.			D at
Allegany: Angelica	\$9,000		Per ct.	Philadelphia.	\$8,000		Per ct.
Scio				Rutland 1	6,000		
Chautauqua:	. 0,000			Lewis:	0,000		
French Creek	3,000	3	41	Denmark	6,000	6	5
Kiontone	4,000	4		Lowville 1	9,000		
Westfield	28,000		4	Oneida:			
Chemung:	·			Augusta	10,000		
Big Flats	40,645		41/2	Kirkland	11,500		
Chemung	20,000		41	Paris	5,000		
Elmira Cortland:	3,408		$4\frac{1}{2}$	Vernon Otsego:	20,000		
Cortlandville	14,000			Maryland	3,000		
Homer	4,000			Unadilla	5,500		
Marathon	4,800			Westford	2,500		
Delaware:	,			Putnam: Putnam			
Middletown	6,000			Valley	25,000	12	44
Sidney	1,400			Schenectady: Prince-	4 000		
Essex: Chesterfield	1 500			town 1 Seneca: Lodi	1,200	1-4	6
Keene	1,500 5,500			Steuben:	1,200		
Lewis 1	6,500			Canisteo	1,000		1
St. Armand	4,000			Corning	13,000	2-5	5
Franklin:	,			Rathbone	2,480		
Bombay	3,000			Suffolk:			
Malone	8,000			East Hampton	70,000	6-20	4
Moira	7,000	6	5	Huntington	17, 703		
Fulton: Caroga Genesee: Le Roy 1	35,000 12,000	-	9	Babylon and Southampton	80,000		
Hamilton: Long	12,000			Tompkins:	80,000		
Lake	30,000			Lansing 1	5,000	(2)	41
Herkimer:	,			Trumansburg	25,000		
Frankfort	2,765	4	5½	Westchester:			
German Flats	6,000			Bedford	5,517	6-19	4-5
Herkimer	88, 232 25, 771	11	41	Cortland	196, 393 259, 000		4-5
Manheim Newport 1	12,500	12 16	$\frac{4\frac{1}{2}}{4}$	Eastchester Greensburg	357, 500		
Russia	3,000	10	4	Harrison	310,600		
Salisbury	5,900	5	5	New Castle	145,693		
Schuyler	12,530			North Castle	4,578		
Webb	17,000	19	5	Pelham	18,000		
Jefferson:	40.0			Rye	135,000		
Clayton	18,000			Scarsdale	147,350		
Ellisburg 1 Henderson	24,000 9,000			winte Plains	218,000		
Lyme 1	25,000			Total	2,631,165		
	,00				,,,		

NORTH CAROLINA.3

Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Alleghany: Township	e=0 000		Per ct.	Catawba: Hickory	850,000		Per ct.
Anson: Wadesboro	\$50,000 2,000			Newton	\$50,000 50,000		
Ashe: Horse Creek	5,800			Cherokee:	30,000		
Bertie: Township	5,000			Murphy	50,000	20	6
Bladen: Township	10,000			Valley Town	47,000		51-6
Brunswick:	07 000		~	Cleveland:			_
Smithville Towncreek	35,000 15,000	20	5	Kings Mountain	25,000	30	5
Buncombe: Black	10,000	20		Shelby	50,000	15	5
Mountain.	20,000			Townships 6 and 7.	50,000		
Burke: Morganton	50,000			Davidson: Lexington.	100,000		
Caldwell: Lovelady	25,000			Duplin:			1
Carteret:	10,000	40	-	Calypso	5,000		
Morehead Newport	10,000	42 42	5	Faison Rosehill	15,000 20,000		
Mewbott	3,000	42	9	Rosemin	20,000]	

¹ Bridge bonds only.
² Serial.
³ By act of legislature, county commissioners have authority to sell bridge bonds without vote of people.

Table 23.—Township highway and bridge bonds—Continued.

NORTH CAROLINA—Continued.

Counties and townships.	Total amount voted to Jan.1,1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
DuplinContinued.			Per ct.	Moore-Continued.			Per ct.
Wallace	\$5,000		2 01 00.	Mineral Springs	\$10,000		1 01 00.
Warsaw	20,000			Sand Hill	10,000		6
Franklin:	20,000			Nash:	10,000		
Franklinton	140,000	30	5-53	4 townships	40,000		,
Louisburg	70,000		$5\frac{1}{2}$	Manning	50,000		
Youngsville	55,000		6	Onslow: Jacksonville.	10,000		
Greene: 7 townships	180,000			Orange: Hillsboro	40,000		
Halifax:				Pitt: Greenville	50,000	40	5
Enfield	60,000			Polk: Tryon	12,000		
Halifax	40,000			Richmond:		Ì	
Haywood: Waynes-			_	Beaver Dam	10,000		
ville	50,000 .		5	Black Jack	5,000		
Henderson:	10.000			Marks Creek	15,000		
Edneyville Hendersonville	12,000 50,000			Mineral Springs Rockingham	5,000		
Hoopers Creek	20,000			Steeles	25,000 15,000		
Jackson:	20,000			Wolfs Pitt	25,000		
Callowhee	30,000			Scotland:	20,000		
Dillsboro	15,000			Laurel Hill	30,000	30	4
Lee	15,000			Spring Hill.	20,000		4
Sylva	30,000			Stewartsville	50,000		
McĎowell:	,			Williamson	30,000		
Marion	50,000		6	Stokes:	ĺ í		
Nebo	10,000		6	Danbury	15,000	30	6
Old Fort	20,000		6	Meadows	40,000	30	6
Macon: Franklin	100,000			Sauratown	50,000	30	- 6
Madison: 2 townships.	20,000		-,,	Surry: Mount Airy	85,000	30	
Martin: Robersonville	FO 000			Warren: Warrenton	50, 000		
Williamston	50,000 40,000			Wayne: Brogden	40,000		}
Moore:	40,000			Goldsboro	100,000		
Carthage	8,000		6	Wilson: Wilson	100,000		
Deep River	12,500		U U	77113011, 77113011	100,000		
Greenwood	10,000			Total	2,751,300		
McNeills	14,000	10-30	5-51		5,102,000		

OHIO.

Adams: Wayne	\$7,000		4	Cuyahoga-Contd.			
Ashland:	Φ1,000		-2	Warrensville	10,000		
Montgomery	1 98,000			West Park	5,000		
Sullivan	25,000	10-18	5	Erie: Groton.	25,000		
Troy.	70,000	10-18	5	Fulton: 12 townships.	392, 200		4½ 5
Athens:	10,000	10-10	0	Geauga: Hambden	3,000	6	4
	1,000	2-4	5	Hamilton: Springfield	17,500	0	41
Canaan Trimble 2	20,000	2-4		Harrison:	11,500		42
Belmont:	20,000			Short Creek	9,000		5
Colerain	25 000			Stock	2,700		4-6
Pease.	25,000		5	Henry: Ridgeville	2,500		6
	88,000		9	Huron:	∠,500		0
Pultney	25, 000 33, 000			Bronson	15,500	(3)	5
Warren	40,000			Greenfield		3	. 6
Washington	40,000	16	5	Greenwich	4,800 64,000	3	43
York	32,000	10	0			(3) (3) (3) (3)	41 5
	95 000	(0)	ا ج	Lynne	28,000	1 (°)	42-0
Perry	25,000	(3)	5 5		50,000	9	4½ 4½
	20,000	23	9	New London	40,000		42
Crawford: Town-	955 500	0.00	4.0	Norwalk	25,000		4-5
ships	355,500	8-20	4-6	Norwich	46,000	(2)	
Cuyahoga:	00 500		F 01	Peru	15,000	(3)	$\frac{4\frac{1}{2}}{6}$
Bedford	33,500		5-81	Richmond	31,000		5
Brecksville	19,000	15	$\frac{4\frac{1}{2}}{5}$	Ridgefield	35,000		5
Brooklyn	7,000	10	5 41	Sherman	40,000	10	4 41
Dover	35, 829		4½ 4½	Wakeman	27,500	29	4-42
	32, 161	24	41 22	Jefferson: Springfield.	25,000	29	4-4½ 4½
Independence	5,000		41-5	Knox: Hillar	10,000		
MayfieldOlmsted	8,500		41/2	Lake:	H F00		0
	30,500		41	Painesville	7,500		6
Orange	32,600		$4\frac{\tilde{1}}{2}$	Willoughby	38,000		41/2
Parma	16,000		$4\frac{1}{2}$	Lorain:	41.000		
Rocky River	30,900	8-16	4-41-5	Brighton	14,000		5
Royalton	19,725		$4\frac{7}{2}-5$	Columbia	24,000		41
Solon	14,000		$\frac{41}{2}$	Grafton			5
South Newburgh	35,500		5	Huntington	11,500		5
Strongsville	10,500	1-8	41/2	Rochester	20,000		41/2

¹ Flood bonds issued without vote.

² Bridge bonds.

³ Serial.

Table 23.—Township highway and bridge bonds—Continued.

OHIO.

			ОН	10.			
Counties and townships.	Total amount voted to Jan. 1,1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Lucas:			Per ct.				Per ct.
Monclova. Springfield	\$8,000 2,000	2	5	Scioto: Porter Seneca:	,	9-19	41/2
Mahoning:		_		Adams	10,000 60,500 72,500 66,000 38,000 11,000 27,000 47,000	10	5
Canfield. Ellsworth	100,000	25	4½-5	Big SpringBloom.	60,500	10	42
Poland	100,000 18,500 115,000 100,000		$\begin{array}{c} 4\frac{1}{2} \\ 4\frac{1}{2} \\ 4\frac{1}{2} \end{array}$	Eden Hopewell London	66,000	13	4½ 4½ 4½ 4½ 4½
Smith Springfield	90,000		41/2	Hopewell	38,000		41/2
Marion: Tully	40,000			Scipio	27,000		
Medina: Brunswick	22,500		5	Seneca	47,000		4
Guilford	64,000		43	Canton	26,000		5
Hinckley Liverpool	20,600	20 12	5	Lexington	10,000		4
Medina	19,000 127,500	12	41/2	Sugar Creek Washington	14,000 4,000		
Miami:	1		-	Summit:			
Brown	1,200 7,000	(1).	5	Coventry	10,000		41/2
Newberry	2,000		5	Hudson	5,000		5
Montgomery: Clay	30,000	5	5	Stowe Twinsburg	8,000 7,000		
Van Buren	10,000		5	Trumbut!:			_
Noble: Caldwell	6 000	15-19	6	Bristol	3,000 10,000 100,000		6 5
Noble Olive	6,000 20,000	10-19	4-5	Liberty	100,000		5
Olive	20,000		5	Liberty Lordstown	100,000	3	4
Ottawa: Allen	37,000			Newton Vienna	100,000 47,500 25,000		5
Bay	37,000 24,450			Tuscarawas:		_	
Catawba	20,000 25,200		5 5	Mill Perry	10,000 1,200	5 3	5 5
Erie	22,000	7-15	5	Van Wert:			
Harris Perry: Coal	45, 200 19, 000	25	5	Harrison Jennings	125,000 21,000	25	4-41/2
Pickaway:				Liberty	144,000		4-41
Derby	17,000 18,000			Pleasant Ridge	131,000 125,000		4-4½ 4-5
Portage:				Tully	75,500 140,000	23	4-5
Aurora	4,000			Willshire	140,000		4
Brunfield Ravenna	6,900 9,000	2-10	4	York Vinton: Vinton	540		
Richland:				Vinton: Vinton Williams: Brady	35,000		41
Cass Plymouth	35,000 61,000		4½-5 5	Wood: Liberty Wyandot: Tymoch-	50,000	5	4-5-6
Sharon	50,000		5-6	tee	46,000	10	41-5
Weller	42,000		4-5	Total	5, 283, 805		
Ballville	12,000		4	10000	0,200,000		
Madison	3,100		41/2				
			OKLA	нома.			
04				D			
Carter: Berwyn	\$15,000	15	6	Rogers: Catoosa	\$3,000	25	6
Morgan	40,000			Verdigris	14, 288	25	6
Wilson Creek: Sapulpa	10,000 50,000	20	5	Stephens: King Tulsa: Red Fork	27,500 50,000	15	6
Kay: Miller	18,000	20		Wagoner: Stonebluff	4,500		
Osage: Bigheart	50,000			Total	382,288		
Big Hill	50,000						
Strike Ax	50,000						1

¹ S erial.

Table 23.—Township highway and bridge bonds—Continued.

PENNSYLVANIA.

			EMMSI	LVANIA.			
Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Allegheny: Mifflin Reserve Scott	\$18,000 21,000 10,000	20	Per ct. 5 4½-5	Clinton—Contd. Leidy. Logan. Columbia: Mount	\$12,500 150	10	Per ct. 5 412
Stowe	20,000 13,000	8	41/2 41/2 5	Pleasant	250		4
Armstrong: East Franklin	4,300	17	5 4½	Oil Creek Wenango Cumberland: Lower	1,700 1,960	5 6	5 5-6
Kiskiminetos Manor Beaver:	5,500	20	5 5	Allen Dauphin: Jefferson Delaware:	2,350 583		5 5
Big BeaverChippewaDoughertyWhite.	5,000 1,850 5,412 1,000	9	5 6 6	Ashton	12,000 3,500 11,000		4 5
Bediord:	l .	4	6	Edgemont	13,000		4½ 4 6
BloomfieldLibertySouth WoodburyBerks:	4,000 400 9,500	5 4–10	4 4 4–5	Tinnicum Upper Chichester Upper Darby	32,000 3,400 99,800	20	5-6 5½ 4½-5
Alsace	1	1	5	Elk: Benzinger Ridgway. Franklin: Lurgan	3,450 29,000 1,000		5 6
GreenfieldLoganTaylorBradford:	5,800 35,000 4,500	20	$\begin{array}{c c} & 4\frac{1}{2} \\ & 5 \\ & 4\frac{1}{2} \end{array}$	Huntingdon: Spring-	5,000		5 5-6
Armenia Terry	385 450	3	5-6	field Indiana: Conemaugh			5
Warren Bucks: Bristol	38,333	1	4	Conemaugh Pine White Juniata: Greenwood. Lackawanna:	9,000 200		6 5 5
Middletown Southampton Butler:	38, 333 50, 000 50, 000	6	4 4 5	Covington	1,500 1,100 65,000	20	6 6 4
Adams. Butler Cambria: Middle Tay- lor	3,000 5,500 1,250	15	$\frac{4_{1}^{1}}{6}$	Hunlock	2,300	15	
Cameron:	1 600	8 3	6 5–6	Plains Plymouth Wilkes-Barre Lycoming:	2,300 45,000 15,000 40,000		6 5 5 5
Lumber 1. Shippen. Carbon: Penn Forest. Center:		10	6 5–6	HepburnLewesNippenose	3,000 600 2,380		5 5 6
College Gregg Haines	2,000 900 500		5 5 5	McKean:	2 200		6 5 5
Half Moon Chester: East Brandywine	700		4½-5 4-5	Ceres. Eldred. Foster. Hamlin.	1,600 6,300 4,108	2	5 6
East Coventry East Goshen New Garden New London	7,200	30	4½ 4 5	Mifflin; Derry Monroe:	10,000		6 4
New London Penn Pennsburg Tredyffrin Valley	2,000 3,000 11,000		5 5 5	Jackson Middle Smithfield Paradise	2,000 2,000 2,000	5	
Valley West Brandywine West Calm	2.1881	9	$\begin{array}{c} 4\frac{1}{2} \\ 5 \\ 4\frac{1}{2} \end{array}$	Paradise Pocono Polk¹ Smithfield Stroud	2,785 500 7,000		4-5 4 5
West Calm. West Goshen Willistown. Clarion: Licking	2,500		5 41 42 4	A hington	290 000		4-4½-5 3-4
Clearfield:	5 000		6 5	Cheltenham. E. Norriton Horsham	155,000 4,500 25,000 16,000		5
Burnside. Cooper Decatur Ferguson	2,000 1,000 5,000	5	5 6 5	Lower Gwynedd. Montgomery. Springfield. Upper Publin. Upper Providence. W. Norriton. Worgester	16,000 8,000 20,000 85,000	10	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
Jordan	750			Upper Providence W. Norriton	85,000 9,000 12,500 22,500	3 20	4½ 4–4½
Lawrence	2,000		5½ 5	Worcester. Perry: Jackson Toboyne	22,500		4-4½ 5 5
Julius Calulot	1, 100		0	. торой петет	200		

¹ Bridge bonds only.

Table 23.—Township highway and bridge bonds—Continued. PENNSYLVANIA--Continued.

Connties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Pike: Greene. Lehman. Palmyra. Potter: Bingham. Clara. Eulalia. Hector. Oswego. Pike. Portage Stewardson. W. Branch. Schuylkill: Delano. E. Brunswick. N. Manheim. Rush. Sullivan: Colley. Forks. Susquehanna: Apolacon.	\$3,500 1,700 1,200 704 973 4,752 2,500 1,300 8,774 1,500		Per ct. 5 6 5 5 6 6 5 5 5 6 6 6 5 5 5 6 6 6 4 4 6 6 6 6	Tioga—Continued. Deerfield. Morris. Nelson. Shippen. Tioga. Union: Hartley. Venango: Allegheny. Warren: Conewango. Corydon! South West. Spring Creek. Washington: Hanover. Independence. Wayne: Cherry Ridge. Dreher. Lehigh. Westmoreland: Ligonier. N. Huntingdon. Wyoming: Northum-	\$5,100 3,357 4,410 3,332 3,014 11,275 1,200 6,600 20,000 600 3,636 20,000 4,000 1,600 4,000 1,600 8,000 1,500 1,200	5 7	Per ct. 5 6 5-6 5-6 6 3-4 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6 6
Auburn Brooklyn Forest Lake	400 6,000 1,500		5	berland. Windham. York: Fawn.	550 6,000		5 5
Jackson Tioga: Brookfield	3,769	4	5 5	Total	2,333,609		

RHODE ISLAND.

Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Washington: South Kingston. Total.	\$265,000 265,000		Per cent.

SOUTH DAKOTA.

Counties and townships.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Stanley: Ashcreek	\$3,500 3,500	5	Per cent.

VERMONT.

Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Addison: Middlebury Bennington: Bennington Center Franklin: Berkshire. Sheldon.	\$1,500 10,000 771 1,050	1–13	Per cent.

¹ Bridge bonds only.

$\begin{tabular}{lll} \textbf{Table 23.--} Township highway and bridge bonds--- Continued.} \\ \textbf{VERMONT--} Continued. \\ \end{tabular}$

Counties and towns.	Total amount voted to Jan. 1, 1914.	Term of years.	Interest rate.
Grand Isle: Grand Isle. Isle La Motte. North Hero.	\$1,000 2,000 1,000		Per cent.
Total.	17, 321		

WISCONSIN.

Counties and townships.	Total amount yoted to Jan. 1, 1914.	Term of years.	Interest rate.
La Crosse: Onalaska	\$11,000 16,000 27,000	10	Per cent.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913.

ALABAMA.

		1912		1913			
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Blount			Per cent.	\$150,000 125,000		Per cent.	
DallasHale	\$100,000 100,000	30	5				
Lawrence Marion Marshall	123,000	30	6	100,000 130,000	20 30		
Perry	$110,000 \\ 100,000$	30 30	5 5				
Total	533,000			505,000			

ARKANSAS.

Benton Montgomery Woodruff: District 1	 	 \$2,815 10,000 30,000	12	6
Total	 	 42,815		

CALIFORNIA.

Kern		 	\$2,500,000	25	5
Orange		5			
Riverside		 	1,500,000		
San Mateo Santa Barbara: Carpinteria		6	1,250,000	40	5
Total		 	5 950 000		
10ta1	1,520,000	 	5,250,000		

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

DELAWARE.

	DELA	WARE.				
		1912			1913	
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Kent New Castle Sussex	\$105,000		Per cent.	\$30,000 1 475,000 30,000	20 20–51 5–24	Per cent. 5 4½ 4½ 4½
Total	105,000			535,000		
	FLO	RIDA.				
Bradford: Hampton	\$250,000			\$25,000	20	6
De Soto Franklin Hernando Hillsborough	20,000	20	41/2	250,000 100,000 1,000,000	30 30	5 5
Holmes: 1 district. Lake. Orange. Palm Beach	200,000			1,000,000 40,000 500,000 600,000	30 2 15–30 30	6 6 5 ₂
Pasco Pinellas Polk: Winterhaven	370,000 130,000	30	5	150,000	30	5
Walton Total	70,000			2,665,000		
-	GEO	ORGIA.	1		1	
Bleckley				\$8,000	30	5
Total				408,000		
	ID	AHO.		1		1
Ada	\$45,000	20	$5\frac{1}{2}$	\$200,000	10-20	5
Boise Canyon Fremont: District 1 Gooding	70,000 47,620	10	5	120,000 160,000	10-20	6
Lincoln: Shoshone Richfield	80,000	10-20	6	50,000	10-20	6
Twin Falls				3 100,000	10-20	$5\frac{1}{2}$

¹ Bridges, \$250,000.

630,000

² Serial.

⁸ Bridges, \$50,000.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

ILLINOIS.

			1912			1913	
Counties and districts.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
				Per ct.			Per ct.
Carroll	Woodland I Wysox				\$1,200 3,500	1-5	5 5
Crawford	Honey Creek	\$25,000			35,000	20-25	5
	Lamott	20,000			35,000	20-25	5 5
	Oblong				35,000	20-25	5
Dekalb	Robinson Malta	25,000 8,500	2	5			
Douglas.	Boudre	35,000	13				
ŭ	Sargent	35,000	2-7	5			
Edgar	Elbridge	2,500	10	6			
Edwards:	Emparrass	35,000	10	i i			
District 3					3,000	2	6
Fulton	Orion	7,000		5			
Gallatin	Bowlesville	1,000 7,000	1-2 1-5	4 4			
Jackson	Carbondale	35,000	3-5	5			
Jefferson	Blissville 1	500			500		
T	Farrington 1 Ganeer				500		
Kankakee	Momence	35,000 35,000					
	Yellowhead	35,000					
La Salle	Farm Ridge				2,000		5
Lawrence	Dennison Ashton	22,000	20	5	35,000 22,000	3 20	5 5
1/66	China		20	3	22,000	20	9
	Harmon				3,000		
To 11	Viola				13,000	1-13	
Pike	Derry Hadlev	3, 075 525		5½			
	Hardin	1,200					
	Kinderhook	700					
St. Clair	Pleasant Hill Centerville	1,200 2,500					
St. Clair	Fayetteville	2,000					
Sangamon	Salisbury	6,000	5	5			
Stephenson	Jefferson				4.000		
Wayne	Leech ¹ Massilon ¹				4,000 3,125	5 5	6
Whiteside	Sterling				0,120		
Will	Crete				35,000	13	5
	Custer				3,000	3	5
Total		424,700			233, 825		

INDIANA.

Adams					\$151,550	10-	43
	Blue Creek				15, 120	(2)	41
					5,280	(2)	43
	Hartford				8, 240	(3)	41
	Kirkland				10,160	(2)	43
	Monroe				25, 440	(2)	45
	Preble				6,560	(2)	41
	Root					(2)	4.
	St. Marys				6,400	(2)	45
	Wabash				32,940	(2)	41
	Washington				69,740	(2)	$\frac{4\frac{7}{2}}{4\frac{1}{2}}$
Allen					53, 840	10	41
	Jackson	\$36,320	1-20	41			
	Lafayette	22,800	1-20	43			
	Madison	35, 930	1-20	41			
	Maumee		1-20	41			
•	Monroe	8, 240	1-20	41			
Bartholomew	Townships				79,216	3 10-20	43
	Clifty		10	45			
	Flat Rock		10	45			
	Haw Creek	16,500	10	41			

¹ Bridge bonds only.

² Six months,

³ Serial.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

INDIANA—Continued.

			1912			1913	
Counties and districts.	Townships.	Amount voted.	Term of years.	Inter- est rate.	Amount voted.	Term of years.	Inter- est rate.
Benton	Grant Hickory Grove Richland			Per ct.	\$111,560 11,156 2,926 1,643	10 10 10	$Per\ ct. \ \frac{4\frac{1}{2}}{4\frac{1}{2}} \ \frac{4\frac{1}{2}}{4\frac{1}{2}}$
Boone	Perry Sugar Creek. Townships	\$14,040 6,000 2,400	10 10	$\frac{4\frac{1}{2}}{4\frac{1}{2}}$	9,378 42,400	10	$4\frac{1}{2}$
Carroll. Cass: Districts 1-3. Clark.	Townships. Bethlehem. Carr Charlestown. Jeffersonville Monroe. Union. Washington.	9,440 13,700 43,400 38,100 29,506 14,316 17,948 9,010	10 10 10 10 10 10 10	5555555	112, 425	10	$4\frac{1}{2}$
Clay	WoodPerryOhio	9,010 9,000 6,824	10	5 	73,800	10	41/2
Daviess	Madison Reeve Center	66,063			90,000 56,738 21,000 40,000 40,000	10 10-20 1-20 1-20 20	$\begin{array}{c} 4\frac{1}{2}\\ 4\frac{1}{2}\\ 4\frac{1}{2}\\ 4\frac{1}{2}\\ 4\frac{1}{2}\\ 4\frac{1}{2}\\ 4\frac{1}{2}\\ \end{array}$
Decatur Delaware Fayette	Harrison. Miller.	11,320	1–20	41/2	50,000 1 63,880 100,000 24 000	10-20 10-15 10-20 10	4½ 4½ 4½ 4½ 4½ 4½ 4½ 4½ 4½
FountainGibson	Center Montgomery Patoka. Union	122,750			15, 200 77, 300 5, 600 26, 400 18, 000 27, 300	10 10 10 10 10 10	$4\frac{1}{2}$ $4\frac{1}{2}$ $4\frac{1}{2}$ $4\frac{1}{2}$ $4\frac{1}{2}$ $5\frac{1}{2}$
Grant Greene Hamilton	Townships	550,000	10	4½	42, 499	10	$4\frac{1}{2}$
Harrison	HarrisonTaylor	7,100 9,200 10,200		412	² 35, 500 43, 220	1-10 20	4½-6 4½
Henry	FranklinUnion.	9, 200		$\begin{array}{c} 4\frac{1}{2} \\ 4\frac{1}{2} \end{array}$	215,000 39,653	10	41/2
Huntington Jackson Jasper	Jackson	52,988	10	4½ 	39, 653 22, 425 3 29, 640	10 10 10	$4\frac{1}{2}$ $4\frac{1}{2}$ $4\frac{1}{2}$
Jay Jefferson Jennings	Keener Townships Township	18,000	10	4½	68, 910 50, 370 3, 000 14, 300 93, 400 189, 360	10 10 20 10	4-6½ 4½ 4½ 4½ 4½
Johnson Knox Kosciusko Laporte	Townships. Vincennes.	1,440	10	$4\frac{1}{2}$	93,400 189,360 208,000	10 10 20	$\begin{array}{c} 4\frac{1}{2} \\ 4\frac{1}{2} \\ 4\frac{1}{2} \end{array}$
Madison. 3 districts. Marion	Fall Creek	99, 380	10	4½	76, 120 6, 240 5 228, 000 57, 000	4 10 20 10-20	4½ 4½ 4½ 4½ 4½
Marshall Martin	BourbonBaker.	28, 500 30, 000 5, 092	15	4½	4,300	15	41/2
Miami Monroe Morgan Ohio		5,092 32,550 96,319 21,000	10-20	$\frac{4\frac{1}{2}}{4\frac{1}{2}}$	70,880 48,200 9,000	10-20 10 10	4½-5 4½ 5

¹ Bridge bonds, \$30,000. ² Bridges, \$25,000.

³ Bridge, \$15,000. ⁴ Serial.

⁵ Bridge, \$200,000.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

INDIANA-Continued. .

			1912 '			1913	
Counties and districts.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Owen	MarionAdamsTroy	\$8,972 73,000	40	$\begin{array}{ c c c } Per ct. \\ \hline & 4\frac{1}{2} \\ \hline & 4\frac{1}{2} \end{array}$	\$24,159 22,658	20 10	Per ct. 4½
Pike. Putnam: Districts 1-3. Rush. St. Joseph.	Townships	39,800 60,000	16	$\frac{4^{1}_{2}}{4}$	21,000 58,689 259,000	20 10 10–20	$\begin{array}{c} 6\frac{1}{2} \\ 4\frac{1}{2} \\ 4\frac{1}{2} \\ 4\frac{1}{2} \end{array}$
Scott. Shelby ¹ .	Jennings Shelbyville Ohio	51, 940 14, 320	10	$4\frac{1}{2}$ $4\frac{1}{2}$	80,000 28,920	20 20	$\frac{4\frac{1}{2}}{4\frac{1}{2}}$
	Jackson	17, 960 22, 931	10	$\frac{4^{1}_{2}}{4^{1}_{2}}$	41,000 80,982	10 10	$\frac{4\frac{1}{2}}{4\frac{1}{2}}$
Tippecanoe ¹ . Tipton: Districts 1–3. Vanderburg. Vigo. Wabash					260,000 44,080 92,600 33,800 145,320	10 10 10 (2)	4½ 4½ 4½ 4½ 4½ 4½ 4½ 4½
Wayne	Liberty Noble				10, 960 67, 540 12, 660	10 10 10 10	42 4½ 4½ 4½ 4½
Wells	4 townships Wayne				58,660 146,000 93,000	10 10	$\begin{array}{c} 4\frac{1}{2} \\ 4\frac{1}{2} \\ 4\frac{1}{2} \end{array}$
Total		2,384,783			4, 701, 997		

IOWA,

Counties.		1912		1913			
	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Boone	\$25,450	. 12	Per cent.	3 \$67,000		Per cent.	
Fremont ¹ Jackson ¹ Madison Wright ¹				\$ 100,000 \$ 108,000 28,000 45,000	20 20 23-17 7-15	5 5 5 5	
Total	25,450			348,000			

Bridge bonds only.
 Serial.
 General funding bonds including gravel roads.

By order of Board of Supervisors.
 To fund outstanding bridge warrants.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

KANSAS.

Counties.	Townships.		1912		1913			
		Amount voted.	Term of years.	Inter- est rate.	Amount voted.	Term of years.	Inter- est rate.	
Geary	Junction CityGlick	\$86, 150 89, 600 5, 000	10 9–10 (¹)	Per ct. 6 5-6 5			Per ct.	
Marion Sedgwick. Wilson.	Center Guilford	7,000 10,000			\$6,000 1,550	5–11	5	
Wyandotte		189,000 386,750	(2)	4½	7,550			

KENTUCKY.

Counties.		1912		1913			
	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Lewis	\$8,000	5–8	Per cent.	\$800		Per cent.	
Total	8,000			800			

LOUISIANA.

		1912		1913			
Parishes ³ and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate	
Assumption				\$80,000	9	Per cent.	
Bossier				175,000 900,000	1–40 25	5 5	
East Baton Rouge: District 1	\$13,009	1–10	10	37,000	10–20	5	
Jefferson. Lafayette. Tangipahoa: District 2.	200,000		5	75,000 75,000	25 30	5	
Washington.				39, 477	2-4	5½	
Total	213,009			1, 381, 477			

MAINE.

			1912		1913		
Counties.	Towns.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Kennebec	Benton			Per ct.	\$1,500	5	Per ct.
Knox. Oxford	Vinal Haven Norway 4		1		2,500 35,000	35	4
Penobscot. Piscataquis.	Orono 5 Foxeroft	\$25,000	1-25	4	12,000	2-4	4
Waldo Washington	Frankfort 5				1,000 1,000	(6)	5 6
Total		25,000			53,000		

¹ Serial to run until 1918. ² Serial to run from 1932 to 1941.

³ Parishes are equivalent to counties. ⁴ For roads and sewers.

⁵ Bridge bonds. ⁶ Six months.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

MARYLAND.

		1912		1913				
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.		
Caroline			Per cent.	1 \$35,000	20	Per cent.		
Montgomery: 5 districtsQueen AnnesTalbot.	\$47,000 50,000			25,000 30,000	25	41/2		
Worcester				25,000	25	5		
Total	97,000			115,000				

MASSACHUSETTS.

			1912		1913		
Counties.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Barnstable ²				Per ct.	\$14,000	1.0	Per ct.
Berkshire Bristol Essex	North Attleboro	\$6,000	1-6	4	5,000 7,000 120,000	1-2 1-3	$\frac{4}{4\frac{1}{2}}$
Hampden	Russell	5,000 9,000		4			
Nantucket	Nantucket	20,000	10	5	20,000	5	4
Norfolk ²	Millis	2,400	3	4	50,000	(3)	4.92
Plymouth 2		2, 100			20,000		4
Total		42,400			236,000		

MICHIGAN.

Antrim	Central Lake		 	\$20,000 20,000		
Baraga. Benzie	Arven Crystal Lake		 	20,000		
Berrien	3 townships		 	500,000 89,000		
Delta Emmet			 4½ 4½		4 10	
Genesee Gogebic GrandTraverse		150,000	$\frac{4_{2}}{4_{2}^{1}}$	200,000		
Huron	Whitewater Sebewaing			24,000		
Ingham	Windsor	50,000				
Kalkaska	Clearwater Coldspring	6,000	 			
Kent	Springfield	9,000		265,000		
Lake. Leelanau.	Ellsworth Leelanau	20,000	 			
	3 townships		 	26,000		

Bridge built from part of this amount.
Bridge bonds only.

³ Nine months.
⁴ Serial.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

MICHIGAN-Continued.

				1912			1913	
Counties.	Tow	nships.	Amount voted.	Term of years.	Inter- est rate.	Amount voted.	Term of years.	Inter- est rate.
Mackinac.	,				Per ct.	\$100,000	10-20	Per ct.
Mackinac	Hudsor	1	\$4,000		!	\$100,000	10-20	9
	Newtor	1	5,000 50,000 36,000 10,000					
Macomb	Lake		50,000					
35	Warren		36,000					
Mason	Free So	ш	10,000			56,000	15	
Montealm	Eureka		500	10	5	30,000	10	9
Newago	Groton.					20,000		
Oceana	Golden.		3,000		5			
Ontonagon.						38,000	1 10	5
Osceola	Lincoln			20	47	5,000		
Ottawa	Fairgro	770	600,000	20	41/2	20,000		
T uscola	Welling	ton				4,500		
Van Buren	Covert.					25,000		,
	South I	Taven	25,000	5	5			
Wexford	Hender	son	2,000					
Total	.`		1,696,500			1,721,152		
-		MININ	ESOTA.			1	1	
		MIINI	ESOIA.				1	
Beltrami						\$81,000	20	4
Carlton	Blackho	oof	\$3,000	15	4			
	Corona.		1,500	15	4			
	Mahtow	7a	3,000	20	4			
	Red Clo	over	2,000 3,000	13	4			
Kittson	Thomp	ock	7,000	13	4 4			
Koochiching.	Bannoc	k	3,000	10	4			
Troots and the second s	Meding		7,000	10	4			
	Reedy.		6,000	10	4			
McLeod	Collins.		3,000	6-15	4			
Marshall	Alma	- d-	1,200 800	5-9 5	4 8			
Millelacs	Big Wo	ous	5,000	9	4			
Ramsey	White I	Bear	7,500		4			
Winona						50,000	5-7	5
Total			53,000			131,000		
						1	1	
		MISS	ISSIPPI.					
			1912			1	.913	
Counties and beats.		Amount	Term of				erm of	Interest
		voted.	years.	rate.	VO	oted.	rears.	rate.
				Per cer	nt.	.		Per cent.
Adams: Beat 1		\$150,000						
Attala		50,000	25		5			
CalhounBeat 1		\$150,000 50,000 40,000 60,000	25		6			
Chickasaw: Beat 3		50,000	25 25 25 20		5 \$1	50,000	20	5
Claiborne		50,000	20			10,000	20	5
Clay:								
Beats 1–3		141,000				00.000	10.05	
Beat 2		50.000	30		5	20,000	10-25	6
Coahoma		50,000 159,000	30		0			
Beat 2						75,000	25	6
Covington.		50,000						
De Soto: Beats 1, 2, 3, and 5		250,000	10.00		5			
Forrest Beats 1 and 3		100,000	10-25			00,000	40	
Death I and d		7 (Coriol	.;		00,000	40	9

¹ Serial.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

MISSISSIPPI-Continued.

		1912			1913	
Counties and beats. ¹	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
			Per cent.			Per cent.
George	\$30,000	30	6			
Greene	47 000			\$10,000	1-10	6
Grenada	45,000	20	5 6			
Hinds: Beats 1 and 5	100,000	20	0	50,000	20	6
Imus: Deats I and 5				200,000	25	5
Issaquena Itawamba				20,000	40	6
Jackson	65,000			65,000		
Jasper	25,000	25	5			
Jones: Beat 2	20,000	20	9	50,000	25	5
Lafayette	180,000	25	51-6	50,000	20	9
Lamar	51,000	20	02-0	20,000		
Lauderdale: Beat 5	50,000	30	5	100,000	30	5
Lee:	00,000	50	0	100,000	30	9
Beats 1 and 3	50,000	25	51/2			
Beats 1 and 2	50,000	20	02	80,000	25	51-6
Leflore.				100,000	20	5
Lowndes: Beat 2				50,000	10-20	5
Monroe: Beats 1, 4, and 5.	50,000	25	5	50,000	10-20	0
Montgomery: Beat 1	40,000	10-20	5	**********		
Neshoba	10,000	20		100,000		
Noxubee .				380,000		
Beats 1, 2, 3, and 5	377, 500	25	54	000,000		
Panola	,		-2	50,000		6
Pike				200,000		
Pontotoc.				5,000	20	
Prentiss: Beat 1	50,000	20	6	40,000	25	6
Quitman,				25,000		
Rankin: Beat 2				10,000		
Scott: Beat 1	75,000	20	6			
Simpson: Beats 1 and 2				40,000	20	$5\frac{1}{2}$
Fallahatchie.	25,000	25	6			
Beats 1-5,,,				75,000	- 25	6
Warren	65,400	20	5	300,000		
Yalobusha:						
Beats 1 and 4	25,000	25	$5\frac{1}{2}$			
Beats 2 and 4				48,000	25	$5\frac{1}{2}-6$
Yazoo: 4 beats				77,500	25	6
Total	2,403,900			2,450,500		

MISSOURI.

			1912			1913	
Counties and districts.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Inter- est rate.
Boone: Harg			10	Per ct.			Per ct.
CedarClay: 2 districts		19,000 135,000	2–15	$5\frac{1}{2}$			
Dade: 1 district Greene		30, 000 12, 000			\$78,000 5,000		
Grundy		30,000 50,000			3,000		
Lawrence: Mount Vernon Mississippi: 1 district		50,000 7,000	15	5			
New Madrid: King's High- way and Malden Risca		20,000					
Newton: Neosho Nodaway		15,000	(2)	6	30,000		6
Stone: 1 district	Polk 3	10,000	17	6	50,000		
Total		398, 000			163,000		

¹ Counties subdivided into beats and districts.

² Serial. ³ Bridge bonds only.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

MONTANA.

		1912		1913				
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.		
Blaine Cascade	\$40,000 60,000	20	Per cent.			Per cent.		
29 districts 1	170,000	20	41	\$45,000	20	5		
Lincoln	125, 000 80, 000	20 20	$\frac{4\frac{1}{2}}{5}$					
Sanders: 20 districts Teton	100,000	5-20	5	15,000	2 5-20	5		
33 districts				3 100, 000	20	5		
Total	575, 000			160,000				

NEBRASKA.

Lin	colnts Bluff; Precincts	\$10,000	20	5	\$15,000	
	Total	10,000			15,000	

NEW JERSEY.

				1912			1913	
	Counties.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Inter- est rate.
A +1c	antic		\$30,000		Per ct.			Per ct.
	gen	Egg Harbor	30,000	8–13 30	4½ 4½ 4½			
Can	adene May		57,000	5 30	4½ 4½ 4½	\$70,000	30	41
Cur	nberlandex		9,000 100,500	9	4½ 4			
Glo	ucester		130, 000 320, 666	1–13	4½ 4–13			
Hu	nterdon		45,000	25 20–30	4	84,000 14,500	30 30	4 41
Mid Oce	dlesex		48,000		4½	143, 500 35, 000	30	5
Pas Sus	saicsex						14-18	5
Wa	rren					30,000	5-10	4
	Total		892,766			513,000		

NEW MEXICO.

		1912	1	1913			
County.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Dona Ana			Per cent.	\$100,000	32	Per cent.	

¹ Bridge bonds only.

² Serial.

³ Bridges. \$30,000.

⁴ Bridge, \$26,000.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

NEW YORK.

		1			1		
			1912			1913	
Counties.	Towns.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Inter- est rate.
Cayuga				Per ct.	\$29,777	1-20	Per ct.
Chautauqua	French Creek Kiantone	\$3,000 4,000	3 4	$4\frac{1}{2}$			
Chemung	Big Flats	7,000 20,000		$\frac{4\frac{1}{2}}{4\frac{1}{2}}$			
Essex	Elmira	3,408 1,500		$\frac{12}{4\frac{1}{2}}$			
Fulton	Keene	3,000 35,000	6	5			
Greene Herkimer.	Fairfield	45,500			5,000		
	Frankfort German Flats	2,765 6,000	4	$5\frac{1}{2}$			
	Herkimer 1 Manheim	20, 732 19, 771	11 12	4½ 4½	67,500		4.6
	Newport Russia	8,000 3,000	16	4			
	Salisbury Schuyler	5,900 12,530	5	5			
Lewis	Webb	17,000 12,362	19 25	5 5			
Livingston	Lowville	9,000			12,750	4	43
Nassau Niagara	772-3-3 4	240,000	5–20	$\frac{4\frac{1}{2}}{}$	500,000 4,000		4½-4.7
Oneida Orleans	Kirkland Maryland	5,400 21,750 3,000	6	5			
Otsego	Westford	2,500			38,000	15	43
Rensselaer		150,000 125,000	4-9	4	81,000		
Schenectady Seneca	Princetown 1	120,000			1,200 20,335	10	4.7
Steuben	Corning	4,000	2-5	5	55,000	131/2	41/2
Tompkins	Lansing	23,000 5,000	(1) (1)	$\frac{4\frac{1}{2}}{4\frac{1}{2}}$			
Warren	Trumansburg	10,000 50,000	11	5			
Westchester	Eastchester	89,560 46,500		4-5	2 30,000		
	New Castle White Plains	141,500 30,000					
Total		1,186,678			844, 562		

NORTH CAROLINA.

		1912		1913			
Counties and districts.	- Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Anson Beaufort		\$50,000		Per ct.	\$50,000 3 50,000		Per ct.
Brunswick. Buncombe Burke. Cabarrus.	Morganton				40,000 50,000 50,000		5–6
Caldwell Carteret Catawba	Lovelady Morehead Newport Hickory Newton				25,000 10,000 3,000	42 42	5 5

 $^{^1}$ Serial. 2 Bridge bonds only. 3 By act of legislature county commissioners have authority to sell bridge bonds without vote of people.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

NORTH CAROLINA—Continued.

Davie Duplin Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11 Franklin Granville Greene. Halifax Haywood Henderson Iredell. Jackson	Townships. Townships Calypso Faison Rosehill Wallace. Warsaw. Franklinton. Youngsville Voted by all townships, except 3. Enfield. Halifax Waynesville Edneyville Hendersonville Hoopers Creek Cullowhee Dillsboro.	Amount voted. \$187,000 25,000 5,000 20,000 5,000 20,000 15,000 40,000 40,000	Term of years.	Interest rate. Per ct. 5 5-5½	Amount voted. \$60,000 50,000 175,000 20,000 20,000 180,000 40,000 25,000	Term of years.	Interest rate. Per ct.
Cleveland. Davie. Duplin. Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11. Franklin. Granville. Greene. Halifax. Haywood. Henderson. Iredell. Jackson.	Calypso. Faison. Rosehill Wallace. Warsaw. Franklinton. Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville. Edneyville. Hoopers Creek. Cullowhee.	25,000 5,000 15,000 20,000 5,000 20,000 15,000 40,000 50,000 40,000		5-5½	200,000 20,000 180,000 60,000 40,000		Per ct.
Cleveland. Davie. Duplin. Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11. Franklin. Granville. Greene. Halifax. Haywood. Henderson. Iredell. Jackson.	Calypso. Faison. Rosehill Wallace. Warsaw. Franklinton. Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville. Edneyville. Hoopers Creek. Cullowhee.	25,000 5,000 15,000 20,000 5,000 20,000 15,000 40,000 50,000 40,000		5-5½	200,000 20,000 180,000 60,000 40,000		
Davie Duplin Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11. Franklin Granville Granville Halifax Haywood Henderson Iredell	Calypso. Faison. Rosehill Wallace. Warsaw. Franklinton. Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville. Edneyville. Hoopers Creek. Cullowhee.	5,000 15,000 20,000 5,000 20,000 20,000 15,000 40,000 50,000 24,000		5-5½	200,000 20,000 180,000 60,000 40,000		
Duplin	Calypso Faison Rosehill Wallace Warsaw Franklinton Youngsville Voted by all town ships, except 3. Enfield Halifax Waynesville Edneyville Hendersonville Hendersonville Cullowhee.	20, 000 5, 000 20, 000 15, 000 40, 000 50, 000 24, 000	20		200,000 20,000 180,000 60,000 40,000	55	
Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11. Franklin Granville Greene	Fanson. Rosehill. Wallace. Warsaw. Franklinton. Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville Edneyville. Hoopers Creek. Cullowhee.	20, 000 5, 000 20, 000 15, 000 40, 000 50, 000 24, 000	20		20,000 180,000 60,000 40,000	55	
Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11. Franklin. Granville. Greene Halifax. Haywood Henderson Iredell. Jackson	Wallace. Warsaw. Franklinton. Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville. Edneyville. Hendersonville. Hoopers Creek. Cullowhee.	20, 000 5, 000 20, 000 15, 000 40, 000 50, 000 24, 000	20		20,000 180,000 60,000 40,000	55	
Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11. Franklin. Granville. Greene Halifax Haywood Henderson Iredell Jackson	Warsaw Franklinton Youngsville. Voted by all townships, except 3. Enfield. Halifax Waynesville Edneyville. Hendersonville. Hoopers Creek. Cullowhee.	20,000 15,000 40,000 50,000 24,000	20		20,000 180,000 60,000 40,000	55	
Edgecombe: Districts 1, 2, 3, 4, 5, 8, 9, 10, and 11. Franklin. Granville. Greene. Halifax. Haywood. Henderson Iredell. Jackson. Granville. Greene. Greene. Halifax. Haywood. Henderson Greene. Halifax. Haywood. Henderson Greene. Halifax. Haywood. Henderson Greene. Haywood.	Franklinton. Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville. Edneyville. Hendersonville. Hoopers Creek Cullowhee.	20,000 15,000 40,000 50,000 24,000	20		20,000 180,000 60,000 40,000	55	
4, 5, 8, 9, 10, and 11. Franklin Granville Greene. Halifax Haywood Henderson Iredell. Jackson.	Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville. Edneyville. Hendersonville. Hoopers Creek Cullowhee.	50,000 24,000	20		20,000 180,000 60,000 40,000	55	
Granville. Greene. Halifax Haywood. Henderson Iredell. Jackson.	Youngsville. Voted by all townships, except 3. Enfield. Halifax. Waynesville. Edneyville. Hendersonville. Hoopers Creek Cullowhee.	50,000 24,000	20		180,000 60,000 40,000		
Granville Greene. Halifax Haywood Henderson Iredell. Jackson.	Voted by all town- ships, except 3. Enfield. Halifax Waynesville. Edneyville. Hoopers Creek. Cullowhee.	50,000 24,000		5	60,000 40,000 25,000		
Halifax. Haywood. Henderson. Iredell. Jackson.	ships, except 3. Enfield	50,000 24,000		5	60,000 40,000 25,000		
Haywood. Henderson Iredell. Jackson.	Enfield. Halifax. Waynesville. Edneyville. Hendersonville. Hoopers Creek. Cullowhee.	24,000		5	25,000		
Haywood. Henderson Iredell. Jackson.	Halifax Waynesville. Edneyville. Hendersonville. Hoopers Creek.	24,000		5	25,000		
Haywood. Henderson Iredell. Jackson.	Waynesville Edneyville Hendersonville Hoopers Creek Cullowhee	24,000		5	25,000		
Iredell	Hendersonville Hoopers Creek Cullowhee				25,000		
Iredell. Jackson. C	Hendersonville Hoopers Creek Cullowhee						
Iredell. Jackson. (Hoopers Creek	400,000			12,000 50,000		
Jackson.		400,000			20,000		
					30,000		
	DIII30010				15,000		
	Sylva			5	15,000 30,000		
Lee. Lincoln.	•••••	100,000	40	5	200,000	40	
McDowell	Marion				50,000	30	(
	Nebo				10,000		(
Macon.	Old Fort Franklin				50,000 10,000 20,000 100,000 300,000		(
Madison					300,000		
	Township	10,000					
Martin	Robersonville Deep River				50,000		
	Greenwood				12,500 10,000 10,000		
Mark	Mineral Springs				10,000		
Nash	Rocky Mount Mannings	20,000			50,000		
New Hanover					50,000 1 350,000 10,000	25	
Onslow.	Jacksonville	050 000			10,000		
Orange	Greenville	250,000			50,000	40	5
Polk					2 100,000	30	
	Beaver Dam Black Jack	10,000					
1	Marks Creek	10,000 5,000 15,000					
1	Marks Creek Mineral Springs	5,000 25,000 15,000 25,000					
1.3	ROCKINGHAM	25,000 15,000			•••••		
1	Steeles	25,000					
Rutherford	***************************************				250,000	40	
Sampson. Scotland.	Stewartsville	10,000			100,000	20	
	Williamson	50,000 30,000 30,000 20,000					
1	Laurel Hill	30,000	30	4			
Stokes	Spring Hill Danbury	20,000		4	15.000	30	
	Meadows				15,000 40,000 50,000 80,000 200,000	30	(
Chromes	Sauratown			5	50,000	30	(€
Vance.	Mount Airy	5,000	30	9	200,000	20-40	
Warren	Warrenton						
Wayne	Brogden				40,000		
Yancey.	Goldsboro				40,000 100,000 150,000		
Total		1,706,000			3,642,500		

¹ Including \$250,000 for bridges.

² By act of legislature.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

OHIO.

			1912			1913	
Counties and districts.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
4.111				Per ct.	8104 000	10	Per ct.
Ashland	Sullivan				\$194,000 25,000	10 10–18	5
Ashtabula	Troy				25,000 70,000 1 75,000 2 78,000	10-18	5
AuglaizeBelmont	Washington York	\$40,000	16	5 5	2 78,000	13–26	9
Coshocton		2,003,220	1-30		³ 100,000 1,000,000	10 1–31	5 5
Defiance 4	Euclid	4,000	24	$4\frac{1}{2}$	65,000	4-65	5
ErieFavette4	Groton	25,000		41		(5)	5
FultonGallia					9,000 30,000 14,000	5 2-8	5 5
Hancock		120,500			28,750	5	<u>5</u>
Henry Highland: 2 districts Huron	Norwalk	20,000			7,850	5	5
	Ridgefield Sherman	20,000 25,000	10	5 5			
Lake Lawrence					62,000 30,000	20 4½-5	4½
Licking Lorain: District 1		210,000			6 374,000	5-25 13	5-5½ 5
Lucas	Four townships	175,000 139,535					
Madison 4 Mahoning District 1	Springfield	40,000			80,000	10	5
Mercer					150,000 54,600 60,000	25	5 5–5½
Miami Montgomery Muskingum					330,000		5
Noble	Caldwell	10,000		4-5	6,000	15-21	5 6
Ottawa	Catawba Danbury	20,000		5			
Paulding		24,000			134,300 45,000 14,000	7 10	5 5
Pike Portage	Brumfield	6,900			14,000	2-13	5
PutnamRoss		155,000	5-10	5	s 86,000	25-30	
Sandusky					9 37, 650 10 440, 000	5	5 5 5
Stark Summit ⁴		40,000			11 545,000 23,000	5–15	
Trumbull Districts 1 and 2	Vienna	60,000			12 245, 000		5
Tuscarawas: 68 districts	v ienna	25,000		5	130,000	1-3	6
Union Van Wert	Tully	15,900	23	4–5	53,600 16,600	12-21	5
Warren 4 Washington 4	1 dify	10,900	23		262,000 190,000	1-30 1-22	4-5 5-5
Wayne ⁴					20,000 5,000		
Wood. Wyandot	Tymochtee	20,000	41-5		¹³ 156,000	5	5 5
Districts	1 y mochico				7,200	10	5
Total		3, 221, 455			6, 308, 550		

¹ Flood bonds.

² Bridge \$70,000.
3 Emergency road and bridge bonds.
4 Bridge bonds only.

⁵ Nine months. 6 Bridge \$24,000.

⁷ Of this amount \$775,000 for bridges.

⁸ Bridge and refunding bonds.

Bridge S25,000.
 Flood and emergency bonds, by authority of H. B. 640.
 Bridge \$190,000.
 Bridge \$85,000.
 Bridge \$6,000.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

OKLAHOMA.

			1912		1913		
Counties.	Townships.	Amount voted.	Term of years.	Inter- est rate.	Amount voted.	Term of years.	Inter- est rate.
Carter	Berwyn	\$27,500	15	Per ct.	\$15,000 50,000 3,000 14,288	15 20 25 25	Per ct. 6 5 6 6
Wagoner. Total.		75,000 102,500			82,288		

OREGON.

		1912		1913			
Counties.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Clatsop				\$400,000 500,000 1,250,000	20 10–30 1–30	Per cent. 5 5 5	
Total				2, 150, 000			

PENNSYLVANIA.

		1912		1913			
Counties and districts.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Allegheny				Per ct.	\$1,550,000	30	Per ct.
Berks		\$475,000	2-12	$3\frac{1}{2}$			
Cameron	Lumber	600	3	5-6			
Corbon Districts (55)	Shippen	3,000	10	6			
Carbon: Districts (55) Lackawanna					50,000 200,000	5 15	4
Luzerne					2 260,000	30	4½ 4½
McKean	Ceres	1,000		5			
	Hamlin	4, 108 -					
Potter	Thenley	800			25,000		5
Washington	Forks			- 6	220,000	1-20	$\frac{4^{3}}{4}$
Westmoreland					250,000	20	41
York					35,000	20	
Total		484,508			2,590,000		

RHODE ISLAND.

				1912		1913		
	County, Town.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Inter- est rate.	
Wasi	hington	South Kingston	\$100,000		Per ct.			Per ct.

¹ Bridge bonds only.

² Bridge \$100,000.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

SOUTH CAROLINA.

		1912		1913			
Counties.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Laurens. Marion Richland. Total.	\$50,000 40,000 75,000		Per cent. 4½ 4½ 5½ 5½			Per cent.	

SOUTH DAKOTA.

		1912			1913		
Counties.	Township.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Pennington ¹	Ashcreek	\$44,000 13,500 3,500	1–10	Per ct. 5			Per ct.
Total	• • • • • • • • • • • • • • • • • • • •	61,000					

TENNESSEE.

		1912			1913	
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
Benton Bradley. Campbell Carter. Dickson Greene: 25 districts. Hamblen Hickman Jackson Jefferson Loudon Montgomery Perry Polk Roane. Sevier: 17 districts Shelby Sullivan Sumner Wayne. Wayne.	812, 944 25, 000 100, 000	40	5 4 ¹ / ₂ 4 ¹ / ₂ 4 ¹ / ₂	\$200,000 25,000 4,000 250,000 500,000 17,500 150,000 150,000 120,000 14,500 330,000 185,000 600,000 30,000	25-30 1 30 30 30 12½ 30 30 30 30 30 7 30 30 30 122 122 123 123 123 123 123 123 123 123	
Tatal	629, 144			2, 786, 000		

¹Bridge bonds only.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

TEXAS.

		1912			1913	
Counties ¹ and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
4 1	e150 000	20	Per cent.			Per cent.
Anderson	\$150,000			\$20,000		
Austin Districts 1-3	200,000	5-40	5 5			
Bastrop: Districts 1-2	200,000 100,000 100,000	20-40	5	80,000		
Bee	15,000	20	5			
Bell,	15,000 7,960			3, 980 200, 000 750, 000		
District 1				200,000	40 40	5 5
Bexar	40,000	40		150,000	40	9
Bosque: District 7	150,000 45,000	. 34	$5\frac{1}{2}$			
Brooks. Calhoun.	45,000	40	5	5 000	40	
Districts 1 and 2	100,000	40	5	135,000	40	
Cameron				5,000 135,000 20,000 35,000		
Cass: District 7	14,000			35,000	40	5
District 1	6,000	20	5			
District 1 District 4				100,000		
Collin				450,000 2 75,000	40	5
Cooke	1,190					
Crockett				40,000	40	5
Culberson	5.000	• • • • • • • • • • • • • • • • • • • •		50,000	40	5
Denton: District 1	75,000	40	5			
Ellis	173,000					
Fort Bend.	17,000			350,000 175,000		
Frio.	5,000 75,000 173,000 17,000 30,000 1,990			80,000	40	5 5
Frio				350,000 175,000 80,000 250,000 50,000	40	5
Garza. Gonzales: District 1	150,000		5	50,000	40	4
Grayson				35,000		
Grayson Districts 1 and 2	400,000	40	5			
GreggGrimes	125,000			50,000		
Utiliagailibe				1,600		
Harris: Districts 5 and 6	212,000	(3)	5	070.000	40	5
Hill: Precinct 1. Houston: Districts 1 and 3.	174,000			250,000	40	9
Howard	100,000					
Irion				20,000	40	5 5
Jim Wells. Johnson				125,000 75,000	10	
Jones			5	75,000 3,000 40,000 80,000	20	- 5
Kerr	20,000	5-40	5	40,000		
Kinney Lamar: Precinct 1 Leon:				100,000	10-40	5
Leon:	04.000					
Districts 1-6 District 7	84,000			50,000		
Liberty	225,000			50,000 200,000 150,000		
Liberty. Limestone.	170 000	10. 40	5	150,000		
District 4. Matagorda: Districts 1, 2, and 4. McLennan: District 1. Medina: District 4.	150,000	10-40	1	460,000		
McLennan: District 1	100,000	40	5			
Medina: District 4				40,000	40	5
Midland				50,000 200,000 100,000 475,000	40	
Montgomery: District 1 Navarro: Districts 1 and 3				100,000	40	-5
Navarro: Districts 1 and 3 Nolan.	15,000			475,000	40	5
Nueces				165,000		
Orange	200,000			1		
Polk	25,000			40,000 25,000	4	5
Robertson	500,000	40	5			
Robertson. Districts 1, 2, and 5.				250,000		
San Saba				1, 990 376, 250	40	5
Smith Somervell: District 1						

¹ Counties subdivided into districts and precincts. ² Issued by commissioner's court.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

TEXAS—Continued.

		1912		1913			
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Sterling. Tarrant Tom Green ¹ Trinity: District 1.				70,000 120,000	10-40	Per cent.	
Walker Waller: Waller Wharton: District 1 Wood Zavalla	300,000 120,000	(2)	5	150,000 15,000	40	5	
Total	5,748,040			6,598,819			

UTAH.

		1912		1913			
Counties.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.	
Boxelder	8,500	20 20	Per cent. 4½ 5	\$14,500	20	Per cent.	
Total	183, 500			14, 500			

VERMONT.

	Towns.	1912			1913		
Counties.		Amount voted.	Term of years.	Inter- est rate.	Amount voted.	Term of years.	Interest rate.
Addison Bennington Franklin	Middlebury Bennington Center Berkshire Sheldon				\$1,500 10,000 771 1,050	13	Per ct.
Total					13,321		

VIRGINIA.

		1912		1913				
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.		
Accomac: Atlantic	\$50,000		Per cent.	\$50,000		Per cent.		
Augusta: South River. Brunswick. Culpeper: Catalpa.	250,000 84,000 120,000	(2)	5 5 5					

¹ Bridge bonds only.

² Serial.

³ Issued by commissioner's court as emergency bonds.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

VIRGINIA-Continued.

	VIRGINIA	A-Continu	ied.			
		1912			1913	
Counties and districts.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest rate.
			Per ct.			Per ct.
Dickenson: Clintwood and Kenady	\$54,000	2-30	5	\$32,000 90,000		
Fairfax: Mount Vernon				10,000		
T 00				76,000		5
Lunenburg: 3 districts	40,000		6	64,000 35,000	32	$\frac{51}{5}$
Northampton:				35,000	34	9
Eastville	50,000					
Franktown	20,000 125,000	30				
Orange Pittsylvania: Dan River	125,000	10-20	5			
Pulaski: Dublin	100,000	10-30	5			
Rappahannock				64,000		5
Rockingham: Plains	30,000	10	6	150,000		5
Scott:				150,000		
Estillville				100,000	20-30	5
				33,800 33,300	20-30 20-30	5 5 5
				225,000	20-30	5
Spotsylvania: Berkeley and Living-						
stone	100,000			100,000	30	5
Warren	100,000			60,000		5
Westmoreland				25,000 260,000		5 5
Wise				260,000	30	5
Total	1,123,000			1,408,100		
	WASH	INGTON.	<u> </u>		1	
Asotin				\$35,000		
Clallam	\$300,000	20	5			
Clarke 1				500,000		
King. Okanogan: District 1.	3,000,000 15,000	20 10	5 10			
Snohomish: Delta	15,000	10	10	75,000		
Total	3,315,000			610,000		
	WEST	VIRGINIA	٨.			
Hancock:				-		
Butler	\$125,000	34	5			
Baxter and Grant	125,000	10-34	5			
Logan ¹				\$60,000	20	5
Fairmont				400,000	30	5
Mannington				300,000	30	5
Marshall Pleasants: St. Marys.	150,000	34	5	60,000	30	5
Wetzel: Grant				150,000	34	6
Wood: Parkersburg	180,000	30	$4\frac{1}{2}$			
Total	580,000			970,000		
r o(ar	330,000			570,000		

¹ Bridge bonds only.

Table 24.—County, district, and township highway and bridge bonds voted during 1912 and 1913—Continued.

WISCONSIN.

			1912		1913		
Counties.	Townships.	Amount voted.	Term of years.	Interest rate.	Amount voted.	Term of years.	Interest est rate.
AshlandColumbia		\$25,000 20,000	20 20	Per ct.	\$25,000	20	Per ct.
Iron La Crosse Sauk ¹	Onalaska	35,000	6	4	11,000 24,000	10 20	.5 4½
Vilas Total		140,000	20	5	60,000		

¹ Bridge bonds only.

Table 25.—Counties, districts, beats, and townships giving complete mileage returns of

			Mil	es of roa	d built a	nd plai	nned.	
State.	Counties, districts, beats, and townships.	Total amount voted to Jan. 1, 1914.	Sand- clay.	Gravel.	Mac- adam.	Bitu- mi- nous mac- ad- am.	Total.	Remarks.
Alabama	Autauga Bullock Dallas	\$65,000 160,000 410,000	95	5 137			100 100 197	Includes 16 miles
	Elmore. Jackson Marshall Mobile	170,000 250,000 130,000 500,000	35	56 32 30	76 10		111 108 75 42	About 1 mile of bituminous concrete pavement; 5 miles
Arizona	Morgan Pike Russell. St. Clair. Yuma.	240, 000 192, 000 100, 000 85, 000 500, 000	230	1 1.5 85 150	60		65 230 65 85 200	of chert gravel and 36 addi- tional miles in course of con- struction.
Arkansas California	Yuma. Woodruff: District 1. Glenn. Kern. Los Angeles. Orange. Sacramento.	30,000 450,000 2,500,000 3,500,000 1,370,000 600,000		6 160 38.1	183.4	248 107 104	29 160 339.5 248 107 104	23 miles of graded road. 118 miles graded.
	San Diego	1,250,000					450	Mostly surfaced with disinte- grated granite; 44 miles con- crete.
	San Mateo	1,298,000		20	48		112	44 miles not specified.
Delaware	New Castle	1,285,000		2.9		2.06		
Florida	Columbia Hillsborough Manatee Nassau	1,400,000			64		86 70 64 22	Brick.
	Orange	800, 000		ļ ļ			80	65 miles of brick; rest not speci- fied.
	Pasco	150,000 200,000			30		30 50	Rock 25 miles, marl 15 miles, and shell 10

miles.

Table 25.—Counties, districts, beats, and townships giving complete mileage returns of roads built from proceeds of bonds—Continued.

			Mil	es of road	l built a	nd plar	ned.	
State.	Counties, districts, beats, and townships.	Total amount voted to Jan. 1, 1914.	Sand- clay.	Gravel.	Mac- adam.	Bitu- mi- nous mac- ad- am.	Total.	Remarks.
GeorgiaIdaho	Ben Hill	\$75,000 120,000	125	60			125 60	
Indiana	trict 1. Adams	151, 550 53, 840 223, 260		104.5	36. 9 10. 34		36. 9 10. 34 105	½ mile of brick
	Cass: Districts			12	15	8	35	road.
	Daviess Delaware Gibson Hancock	100,000		27 20 76. 5	3 10 20 .5		30 30 20 77	Bridge bonds,
	Henry Jay Martin		•	21. 5 6. 5 84. 54	9	5	26. 5 15. 5 84. 54	\$25,000.
	Miami Morgan			204.38 273	9. 65 75		214. 03 348. 75	3 mile of brick road.
Kansas Kentucky	Union Vanderburg Johnson Lewis	61, 269 6, 200		14 5	6 60 13		20 60 13 5	
Louisiana	Ohio		71	46	10		10 46 71 15	
	Rouge. Iberville: Districts 1, 5, and			10.5			10.5	
Maryland Michigan	6. Cecil Prince Georges Alpena Baraga Berrien Genesee Mackinac Mason	16,000 100,000 40,000 500,000 700,000	20	141	3 100 14 3	14	17 10 40 30 100 155 35	
	MidlandOntonagonWayne	100,000 56,000 38,000 2,000,000			5 6		15 12 83.5	Includes 80 miles of concrete; rest
Minnesota Mississippi	Wexford Lake St. Louis Jackson	50,000 20,000 300,000 160,000	20	175	4		10 20 175 125	not specified.
Missouri	Jasper. Lauderdale Neshoba Prentiss: Beat 1 Yalobusha Beats 2 and 4. Callaway. Lafayette Lawrence Mount Vernon	25,000 350,000 100,000 40,000 62,000 48,000 100,000 125,000 50,000		25	51.75 28 12 14 12		40 84 28 25 150 110 28 14 12	and 25 miles of shell.
Montana Nevada New Jersey	Mount Vernon Pettis. Lewis and Clark Lincoln Churchill Ormsby. Atlantic.	200,000 105,000	15 7	20	45		60 20 40 15 14 19	13 miles of con-
New Mexico	Cumberland Essex Morris Sussex Dona Ana	1,140,505 400,000 154,100			158 85 26		20.36 158 85 26 40	crete road.

Table 25.—Counties, districts, beats, and townships giving complete mileage returns of roads built from proceeds of bonds—Continued.

-			proceeds					
			Mil	es of road	l built ar	nd plai	nned.	
State.	Counties, districts, beats, and townships.	Total amount voted to Jan. 1, 1914.	Sand- clay.	Gravel.	Mac- adam.	Bitu- mi- nous mac- ad- am.	, Total.	Remarks.
New York	Franklin	\$500,000					124	Gravel and mac- adam.
North Carolina.	Alamance Cabarrus	200,000 145,000		15	45 12	6	45 33	Also 10 steel
	Cumberland Edgecombe: Districts 1-5, 8-11.	40,000 200,000	50 450				50 450	bridges.
	GastonGuilfordHaywoodLee	300,000 300,000 60,000 100,000	10 1 8	15 2 84	90 105 30		100 120 33 92	
Ohio	Vance Fayette	218,000 909,000		200 421	4		200 425	Of this amount \$9,000 was used
	Franklin Geauga Hancock Highland Hocking	20,000				30	$\begin{array}{c} 65 \\ 2 \\ 102 \\ 2.4 \\ 7 \end{array}$	for bridges. 3 miles of brick. 2 miles of brick. 1.5 miles of brick.
	Licking	701, 000			95		133.5	5 miles of con- crete and 33.5 miles of brick
	Mahoning: District 1.	150,000			7.1		14.3	Glutrin 2.6 miles and brick 4.6 miles.
	Mercer				135		590.83	Concrete 15 miles.
	Montgomery Morgan Noble	477,000 40,000 48,000		15	55 3.5	1	71 4.75 6	Brick, 1.25 miles. Concrete, 6 miles.
	Preble Trumbull	11, 160 755, 000		10	116		128	Concrete, 2 miles. Bridge, \$85,000.
Oregon Pennsylvania	JacksonAllegheny	500, 000 15, 900, 000			604.78	52 1134.1	52 836.36	\$550,000 bridge bonds. Con- crete .62 miles brick 74.86 miles. and
South Carolina.	Carbon Dillon	50,000 100,000	70		10		10 70	plank 22 miles. Concrete bridge,
Tennessee	Campbell: Districts 1–5.	200,000		32	35		67	\$17,500.
Texas	Dickson	250, 000 325, 000 405, 000 100, 000 200, 000 1, 250, 000 40, 000	83	100 110 90 230 10	100 15		100 100 125 83 90 241	
	triet 7. Brown: Dis- triet 1.	150,000	35	60			95	
	Comal Cooke: District	153,000 100,000		50 28			50 28	
	El Paso	617, 000 50, 000		3			68 41	
	Gonzales: Dis- trict 1.	150,000		40			75	
	Hall. Hays: District 1. Hill: Precinct 1. Jackson Jefferson	65,000 87,000 250,000 124,500 809,500	6	15 30 80	9	5	20 45 80 200 100	

¹Includes 68.1 miles of bituminous-gravel road,

Table 25.—Counties, districts, beats, and townships giving complete mileage returns of roads built from proceeds of bonds—Continued.

			Mil	es of road	d built a	nd plai	nned.	
State.	Counties, districts, beats, and townships.	Total amount voted to Jan. 1, 1914.	Sand- clay.	Gravel.	Mac- adam.	Bitu- mi- nous mac- ad- am.	Total.	Remarks.
Texas	Jim Wells Leon: Districts	\$125,000 84,000		100			100 77	
	1, 2, 4, 5, 6. McCulloch McLennan Mitchell: District 1.	118,000 150,000 30,000		27.5 64			69 64 27	
	Smith. Stonewall. Taylor: District	405, 000 50, 000 150, 000	40	35	5		300 40 40	
Virginia	Waller Williamson Amherst Culpeper: Ca- talpa.	25, 000 300, 000 215, 000 120, 000	23	150 1.5	30.5		25 150 32 30	
	Dickenson: Clintwood. Kenady. Dinwiddie. Lee.	105,000	7		736		$^{14}_{16}_{125}$ 84	Includes 48 miles
	Montgomery Nelson Norfolk	35,000			8 7 30		8 7 30	of graded road. Proceeds of issue
	Orange. Rappahannock:				30 7.5		30 7.5	to build 3 toll roads and 3 toll bridges.
	Wakefield. Rockingham: Plains.	30,000			5		5	Mileage built with proceeds of bond issue and joint county and
	Spotsylvania Warren: Dis- trict 2.	100,000 60,000		41.8 14	····i		41.8 15	State funds.
	Wise	960,000			48.2		131	Includes 82.8 miles earth graded.
West Virginia Wisconsin	Marion: Fairmont Mannington Florence Vilas.	400,000 300,000 38,000 60,000	13.18	1.84	7.78		22 19 22. 8 30	Concrete and brick.
Total								
Bituminous con Concrete (exclus Chert gravel (36 Brick (exclusive	there are included crete pavement live of West Virgin miles of this in cou of West Virginia)	nia) urse of cons	truction)				152.45 41 256.96

¹ In this total there are included the following	g:	Mar
Bituminous concrete payement		Miles.
Concrete (exclusive of West Virginia)	ruction).	152.45
Chert gravel (36 miles of this in course of constr	ruction)	41
Brick (exclusive of West Virginia)		256. 96 25
Shell		57
Disintegrated granite surfaced		406
Clay		25
Glutrin		15 2, 6
Plank		22
Graded road		287.8
Road not specified		62.5
Total (exclusive of West Virginia)		1,354.31

Table 26.—Townships and towns ¹ giving complete mileage returns of roads built from proceeds of bonds.

			Mi	les of roa	d built a	and plan	ned.
State.	Counties and townships.	Total amount voted to Jan. 1, 1914.	Sand- clay.	Gravel.	Mac- adam.	Bitu- minous mac- adam.	Total.
Illinois	Carroll: Wysox Lee: Ashton	\$38,500 44,000			15 12		15 12
Indiana	Bartholomew: Flat Rock Wayne.	55, 500 35, 240 545, 726		18.5 17 343			18.5 17
	Clay: Sugar Ridge Daviess: Reeve Washington.	21,000 913,988		5 295.62			343 5 295, 62
	Gibson: Center	48, 460 69, 600			13 16		13 16
	Johnson. Montgomery Wabash, White River	171, 620 21, 000 85, 830		6, 5	41 		$\begin{array}{c} 41 \\ 6.5 \\ 22 \end{array}$
	Hamilton: Fallcreek. Washington. White River.	25, 931 65, 691 86, 985 14, 000		20 35 50			20 35 50
	Henry: Franklin	14,000 32,425 189,360		6 8 90	3		6 11 90
	Knox: Vincennes. Madison: Fall Creek Marshall: Bourbon. Shelby: Shelby.	6, 247 28, 500 126, 097		2. 5 33. 5	8.5		2. 5 8. 5 33. 5
Massachusetts	Wayne: Franklin and New Garden Green Franklin: Gill	7,180 12,000 4,500		2	2.5		$\begin{array}{c} 2 \\ 2.5 \\ 2.5 \end{array}$
Michigan	Baraga: Covington. Berrien: Lincoln. Clare: Redding	18,000 20,000 3,000		8 2.5 2	3		10 5.5 2
	Delta: Ford River Wells Gogebic: Marenisco	3,000 10,000 20,000		8	1 3.5		$\frac{1}{3.5}$
	Lake: Ellworth	6,000 39,000 44,250 25,000		3	11 7.85		3 11 7, 85
Minnesota	Osceola: Osceola Schoolcraft: Mueller Wexford: Henderson Cook:	25,000 $6,000$ $2,000$	6	3.75			2 8 6 1
344440000000000000000000000000000000000	Colvill Maple Hill Itasca:	$12,000 \\ 15,000$	15 10	2			15 12
	Balsom. Marcell. Trout Lake.	20,000 10,000 8,500	17 5 10	3			17 8 10
New Jersey	Roseau: Spruce. Burlington: Pemberton Cape May: Lower. Chemung: Big Flats. Fulton: Caroga.	5,000 10,000 5,000 40,645	2	3 3	8		4 3 3 8
	Fulton: Caroga. Westchester: Scarsdale.	35, 000 147, 350		.5	4.5	2 7	7 20
Ohio	White Plains Ashland: Montgomery Belmont: York Crawford: Whetstone	218,000 98,000 32,000 250,000		33	17 5	6	23 33 5 130
	Huron: Norwich. Sherman Lorain: Columbia.	46,000 40,000 24,000			10.75 10.25 6		10.75 10.25 6
	Mahoning: Poland. Smith. Springfield.	115,000 100,000 90,000			1		³ 12.5 ³ 5 ⁴ 7.33
	Medina: Medina Ottawa: Catawba	90,000 127,500 20,000	41 5		14		55 9

 $^{^1}$ In New York and the New England States the town is synonymous with township, 2 Concrete road, 2.25 miles. 3 Brick roads. 4 Brick road, 6.33 miles.

Table 26.—Townships and towns giving complete mileage returns of roads built from proceeds of bonds—Continued.

State.		Total	Miles of road built and planned.					
	Counties and townships.	amount voted to Jan. 1, 1914.	Sand- clay.	Gravel.	Mac- adam.	Bitu- minous mac- adam.	Total.	
Ohio (contd.)	Richland: Weller Seneca: Bloom. Trumbull: Liberty.	\$42,000 72,500 100,000					9 1 4 1 9	
Pennsylvania	Montgomery: Horsham Worcester.	22,500			6.5		6. 5 5	
Wisconsin	Warren: South West La Crosse: Onalaska Sauk: Delton	20,000 11,000 16,000	4	10	2 4		6 10 4	
	Total	4, 623, 625	117	1,153.87	277.35	15	² 1, 602. 30	

Table 27.—Summary of all highway and bridge bonds voted to Jan. 1, 1914.

State.	State bonds.	County and district bonds.	Township bonds.
Alabama		\$5,121,500	
Arizona		808,000	
Arkansas		1, 218, 315	
California	\$18,000,000	15,630,800	
Colorado		134,700	
Connecticut	10,500,000		\$576,500
Delaware		1,395,000	
Florida		7,285,000	
Georgia		1,176,000	
Idaho	505,000	1,221,837	
Illinois		420, 320	1,618,634
Indiana		18,072,049	35, 837, 348
Iowa Kansas		4,006,314	677,065
		1,132,375 1,759,872	077,000
Kentucky Louisiana		1,932,840	
Maine	2,000,000	1,932,040	78,000
Maryland.	9,170,000	750,500	10,000
Massachusetts	14, 365, 000	813,000	650, 473
Michigan	11,000,000	6,382,152	1,926,135
Minnesota		1,388,350	982, 805
Mississippi		8,710,872	
Missouri		1,721,500	65,000
Montana		2, 239, 606	
Nebraska		553,500	246, 170
Nevada		175,000	
New Hampshire	1,300,000		40,000
New Jersey.	**********	14,386,782	760,600
New Mexico New York	500,000	246,500	0 001 105
North Carolina	100,000,000	9,097,923 5,541,273	2,631,165 2,751,300
North Dakota.		63,000	2, 101, 000
Ohio		35, 241, 828	5, 283, 805
Oklahoma		1,440,000	382, 288
Oregon		2, 150, 000	002,200
Pennsylvania		24,839,050	2,333,609
Rhode Island	1,800,000		265,000
South Carolina		410,000	
South Dakota		77, 300	3,500
Tennessee		12,674,298	
Texas Utah.		24, 960, 837	
Vermont	260,000	440,500	17, 321
Virginia.		6,632,400	17,321
Washington		4, 408, 262	
West Virginia.	100,000	2,500,000	
Wisconsin		244,000	27,000
		211,000	
Total	158,590,000	229, 403, 355	57, 153, 718

¹ Brick roads.
² In this total there are included 2.25 miles of concrete road and 36.83 miles of brick road; total, 39.08 miles.

APPENDIX C.

TABLE SHOWING COST ELEMENTS OF GRAVEL, MACADAM, AND BITUMINOUS MACADAM ROADS IN MAINE, MASSACHUSETTS, AND NEW JERSEY.

Table 28.1—Table showing cost elements of gravel roads for years 1908-1911.

					Percentage of cost.		Cost per mile of equiva- lent 20-foot width.		
No.	Location.	Length (feet).	Width (feet).	Total cost of work.	Drain- age and grad- ing.	Surfac- ing.	Drain- age and grad- ing.	Surfac- ing.	Total.
	1908.								
1 2 3 4 5 6 7 8 9 10 11 11 12 13 14 15 16	Camden, Me. Eastport, Me Lisbon, Me. Presque Isle, Me Richmond, Me Rockland, Me May's Landing, N. J. Red Lion, N. J. Tuckahoe, N. J. Malaga, N. J. Half Acre, N. J. Farmingdale, N. J. Eatontown (1st), N. J. Bayhead, N. J. Lakehurst, N. J. Aldine, N. J.	1,400 1,900 1,800 1,115 7250 73,603 19,272 17,946 30,307 17,793 15,840 17,160 24,662 33,448 7,001	26 25 24 40 36 20 16 12 14 24 20 20 14 24 22 20	\$1, 795. 07 1, 634. 00 1, 703. 63 1, 526. 95 1, 066. 91 2, 382. 17 37, 416. 42 12, 607. 26 25, 558. 10 14, 040. 13 9, 961. 89 9, 232. 61 32, 439. 77 25, 950. 75 195. 598 11, 110. 11	69. 40 50. 00 52. 53 46. 35 53. 90 70. 30 34. 38 36. 64 54. 96 63. 89 34. 78 14. 01 36. 63 55. 57 56. 71	30. 62 50. 00 47. 40 53. 50 46. 10 29. 80 65. 62 63. 36 45. 04 70. 54 36. 11 63. 06 86. 12 63. 34 44. 51 43. 28	\$3,612 1,816 2,189 1,676 2,165 7,078 1,153 2,108 5,945 640 0 1,887 1,070 1,980 1,697 4,752	\$1,596 1,816 1,975 1,937 1,858 2,987 2,201 3,648 4,834 1,436 1,068 1,940 12,285 2,950 1,343 3,625	\$5, 208 3, 632 4, 164 4, 023 10, 065 3, 355 5, 756 10, 780 2, 037 2, 955 3, 010 14, 265 4, 645 3, 020 8, 377
	1909.								
17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34	Fairfield, Me. Falmouth, Me. Jay, Me. Presque Isle, Me. Rockland, Me. Sanford, Me. English Creek, N. J. Chestmut Neck, N. J. Schellenger's Landing, N. J. Goshen, N. J. Tuckahoe, N. J. Tuckahoe, N. J. Cranbury, N. J. Allentown, N. J. Lakewood, N. J. Lakewood, N. J. Barnsboro, N. J. Alloway, N. J.	1,541 1,100 1,100 1,600 2,425 35,481 2,745 11,066 13,743	15 21 15 40 23 22 20 27, 5 20 20 20 20 20 20 18 14 24–36 20 20	1, 165. 35 1, 021. 12 1, 386. 71 1, 500. 45 2, 366. 01 2, 773. 71 15, 061. 12 5, 697. 15 12, 258. 99 10, 688. 66 24, 544. 00 14, 556. 54 14, 556. 54 14, 558. 59 12, 488. 63 8, 448. 00 15, 048. 63 21, 100. 29	74. 11 85. 51 77. 06 56. 27 62. 00 55. 22 38. 94 85. 44 54. 37 35. 40 53. 10 34. 17 40. 37 36. 78 36. 08 54. 32 41. 15 55. 56	25. 87 14. 48 22. 94 44. 39 38. 39 41. 59 61. 05 14. 58 45. 62 64. 69 46. 91 65. 83 63. 21 63. 92 45. 68 65. 99 44. 44	3,353 2,842 6,833 2,039 4,201 3,017 873 6,805 3,225 1,451 3,055 1,471 970 1,474 2,014 1,900 1,565 2,462	1,166 480 2,038 1,600 2,603 2,454 1,368 1,161 2,670 3,300 1,432 2,533 3,571 1,600 2,510 1,970	4,520 3,323 8,872 3,639 6,805 5,471 2,241 7,967 5,895 4,106 5,011 2,400 4,007 5,586 3,500 4,075 4,432
35 36 37 38 39 40 41 42 43 44 45 46 47 48	Augusta, Me. Bridgton, Me. Camden, Me. Dexter, Me. Eastport, Me. Fairfield, Me. Gorham, Me. Kennebunk, Me. Lisbon, Me. Millinocket, Me. Milo, Me. Mount Desert, Me. Norway, Me. Orono, Me.	2,500 1,300 712 2,375 1,500 1,250 4,996 1,800 1,500	21 15 21 18 22 23 21 24 30 21 22 23 25 25	2,727.64 1,657.69 1,883.25 1,239.67 1,128.74 3,786.74 967.70 2,435.71 1,053.02 1,071.32 1,018.30 1,370.47 1,028.61 1,043.20 1,080.00	13. 49 71. 04 21. 56 42. 37 56. 61 63. 74 31. 50 13. 31 37. 65 29. 97 36. 99 85. 22 90. 65 68. 21 24. 06	46.78 28.96 78.48 57.63 43.38 36.27 68.48 87.00 62.35 70.30 63.01 14.78 9.40 31.80 75.92	529 3,312 1,569 3,714 1,575 7,545 1,119 427 970 756 1,214 5,456 3,836 1,670 756	1,833 1,366 5,714 5,038 1,208 4,390 2,434 2,023 1,605 1,760 2,150 945 398 779 2,384	2,362 4,678 7,283 8,752 2,784 11,936 3,553 2,450 2,575 2,516 3,364 6,401 4,234 2,449 3,140

¹ This table was compiled from the annual reports of the State highway departments of the three States concerned. Geographical names given in New Jersey are sometimes not names of places, but of roads or streets.

Table 28.—Table showing cost elements of gravel roads for years 1908-1911—Contd.

						tage of		r mile of 20-foot w	
No.	Location.	Length (feet).	Width (feet).	Total cost of work.	Drain- age and grad- ing.	Surfac- ing.	Drain- age and grad- ing.	Surfac- ing.	Total.
50 51 52 53 54 55 56	1910—Continued. Presque Isle, Me. Rockland, Me. Sanford, Me. Scarboro, Me. Waterville, Me. Yarmouth, Me. Cologne, N. J.	2,000 1,900 2,000 1,800 1,360 42,646	21 24 26 21 29 24 20	\$1,675.05 2,193.74 1,860.29 1,048.13 1,803.05 1,738.48 19,575.36	41. 92 88. 16 32. 15 19. 11 24. 70 42. 49 27. 38	58.10 11.84 67.85 80.89 75.26 54.66 72.62	\$2,205 4,245 1,280 502 901 2,550 664	\$3,380 570 2,700 2,133 2,743 3,075 1,760	\$5,586 4,815 3,980 2,636 3,644 5,625 2,424
57 58 59 60 61	Deans, N. J. Red Bank, N. J. Farmingdale, N. J. Lakewood, N. J. Barnsboro, N. J. 1911. Allentown, N. J. Red Bank, N. J.	10,032 13,200 17,476	20 18 18 14 20	9,773.00 19,735.21 11,427.88 7,381.65 8,489.80 15,117.98 17,262.78	34. 48 30. 24 64. 89 43. 91 61. 02 35. 61 17. 54	65. 52 69. 82 35. 11 56. 09 38. 98 64. 39 80. 96	1,227 1,735 4,332 1,851 1,564 3,082 2,592	2,333 4,005 2,344 2,364 999 5,520 9,994	3,560 5,741 6,677 4,215 2,564 8,602 12,586
64 65 66 67 68 69 70 71 72 73 74 75	Lakewood, N. J. Lakewood, N. J. Cedar Ave., N. J. Seaside Park, N. J. Elmerborough, N. J. Camden, Me. Dexter, Me. Eastport, Me. Fairfield, Me. Farmington, Me. Freeport, Me. Gorham, Me.	18, 458 5, 174 13, 807 28, 395 9, 387 1, 000 1, 400 1, 844 650 1, 350 900 2, 050	14 14 16, 18 24 18, 42 30 26 22 23 23 20 23	8, 737. 53 3, 579. 96 22, 442. 25 42, 347. 32 8, 048. 75 1, 588. 77 1, 105. 20 1, 175. 15 1, 549. 41 1, 225. 00 1, 440. 16 1, 220. 39	60. 55 50. 01 21. 70 35. 61 23. 58 42. 10 40. 43 59. 47 60. 91 52. 37 34. 24 42. 33	39. 52 49. 99 78. 30 64. 38 76. 42 57. 92 59. 65 40. 53 39. 09 47. 61 65. 76 57. 69	2,160 2,610 2,190 2,337 710 2,353 1,293 1,818 6,652 2,181 2,892 1,156	1,410 2,607 7,731 4,225 2,305 3,233 1,911 1,238 4,282 1,982 5,550 1,575	3,570 5,217 9,921 6,562 3,016 5,586 3,205 3,056 10,934 4,163 8,442 2,732
76 77 78 79 80 81 82 83 84 85 86 87	Kennebunk, Me Lisbon, Me Millimocket, Me Norway, Me Old Orchard, Me Orono, Me Presque Isle, Me Princeton, Me Rockport, Me Sanford, Me Windham, Me Yarmouth, Me	1,280 1,300 1,200 2,316 1,600 1,536 630 1,800 2,000	21 21 30 23 21 25 24 24 21 24 24 25 24	2,221.16 1,880.97 1,238.44 1,096.23 1,019.15 1,017.03 1,390.28 1,148.25 1,031.82 1,565.99 940.69 1,414.13	37. 98 39. 65 32. 29 42. 74 43. 57 57. 86 41. 90 88. 67 68. 09 12. 93 63. 28 49. 57	62.00 55.03 67.72 57.25 56.43 42.17 58.10 11.32 31.91 87.09 35.82 50.42	1,028 2,771 1,100 1,655 1,860 1,648 1,599 2,910 5,600 495 1,284 2,533	1,675 4,228 2,306 2,213 2,417 800 2,233 371 2,628 3,333 712 2,615	2,703 7,000 3,407 3,868 4,278 2,448 3,832 3,281 8,228 3,829 1,996 5,148
-01	Total and weighted averages	1,200	20	4,417.00	41. 15	58.85	1,817	2,599	4, 416

¹ Miles.

Table 29.1—Table showing cost elements of water-bound macadam roads for years 1908-1911.

			1000	-1011.					
					Percen	tage of	Cost pe	r mile of 15-foot w	equiva- idth.
No.	Location.	Length (feet).	Width (feet).	Total cost of work.	Drain- age and grad- ing.	Surfac- ing.	Drain- age and grad- ing.	Surfac- ing.	Total.
-	1908.								
1 2 2 3 4 4 5 6 6 7 7 8 9 100 111 112 113 114 115 116 117 118 119 200 201 22 22 22 29 30 31 132 23 33 33 34 35 36 6 37 7 38 38 39 40 41 41 42 42 42 42 42 42 42 42 42 42 42 42 42	1908. Augusta, Me. Biddeford, Me. Brewer, Me. Calais, Me. Caribou, Me. Farmington, Me. Gardiner, Me. Houlton, Me. Saco, Me. Sanford, Me. Saco, Me. Sanford, Me. Skowhegan, Me. South Portland, Me. Riverdale, N. J. Westwood, N. J. Franklin, N. J. Lumberton, N. J. Westfield, N. J. Harrison Street, N. J. Whitehouse, N. J. Etra, N. J. Brunswick, N. J. Colonia, N. J. Cranbury, N. J. Livingston Avenue, N. J. River Road "A.", J. River Road "A.", J. River Road "B." N. J. Jamesburg, N. J. Rumson Road, N. J. Rumson Road, N. J. Rumson Road, N. J. Rumson Road, N. J. Rumsonin, N. J. Midvale, N. J. Macopin, N. J. South Bound Brook, N. J. Dead River, N. J. North Broad Street, N. J. Terrill Road, N. J. Terrill Road, N. J. Terrill Road, N. J. Dead River, N. J. Dead River, N. J. Dead River, N. J. Dead River, N. J. Terrill Road, N. J. Terrill Road, N. J.	1, 800 1, 300 2, 100 670 1, 660 2, 000 1, 660 2, 400 1, 900 6, 250 8, 400 9, 770 6, 860 4, 670 11, 166 6, 280 16, 470 11, 540 8, 400 5, 300 5, 240 34, 190 6, 280 19, 540 8, 400 10, 15, 100 10, 100 1	21 27 47 21 45 16 16 16 15 20 14 14 14 16 16 16 16 16 16 16 16 16 16	\$2, 556. 29 4, 067. 68 2, 198. 44 1, 787. 05 1, 646. 14 1, 207. 99 1, 978. 10 2, 033. 50 1, 140. 18 1, 898. 45 2, 632. 04 2, 027. 85 1, 356. 30 33, 437. 76 8, 225. 83 34, 110. 09 32, 745. 23 17, 494. 24 10, 549. 60 17, 074. 76 10, 817. 30 52, 982. 30 10, 693. 87 17, 199. 90 10, 693. 87 17, 157. 42 10, 995. 50 17, 157. 42 19, 232. 805. 66 24, 102. 39 32, 183. 805. 66 24, 102. 39 32, 183. 805. 66 24, 102. 39 17, 157. 42 28, 105. 66 24, 102. 39 28, 106. 45 9, 123. 39 21, 113. 73 18, 589. 20 15, 801. 63	44. 9 48. 8 26. 6 25. 5 14. 8 22. 4 21. 6 25. 5 20. 4 31. 3 20. 2 56. 5 20. 4 31. 3 20. 2 59. 7 41. 2 59. 7 41. 2 15. 1 25. 0 30. 5 63. 3 28. 0 44. 3 28. 0 42. 1 27. 3 14. 6 14. 0 14. 1 27. 9 15. 1 15. 1 16. 1 17. 5 19. 4 17. 5	55. 1 51. 2 73. 4 73. 1 74. 5 85. 2 80. 3 24. 4 43. 5 79. 6 68. 7 79. 8 40. 3 58. 8 94. 9 75. 0 69. 5 75. 7 72. 0 69. 5 77. 4 66. 85. 4 86. 9 77. 4 66. 85. 4 86. 9 77. 9 72. 9 72. 9 72. 9 73. 9 74. 9 75.	\$2,410 3,240 760 860 1,100 830 780 2,980 4,100 3,180 1,710 6,520 4,140 2,230 2,320 1,780 2,320 1,560 1,560 1,560 1,250 4,630 1,250 4,630 1,250 4,630 1,250 4,630 1,250 4,630 1,250 4,630 1,250 4,630 1,250 4,630 1,250 1	\$2,950 3,400 2,080 3,220 5,340 3,220 5,349 3,070 1,320 2,450 6,670 5,940 4,950 5,940 4,400 5,900 8,110 6,830 6,250 6,310 6,840 6,870 6,470 6,430 7,690 6,310 6,830 6,270 6,670 6,830 6,470 6,680 6,470 6,680 6,470 6,830 6,470 6,830 6,470 6,830 6,470 6,830 6,470 6,690 6,830 6,470 6,690 6,830 6,470 6,490 6,830 6,290 6,490 6,830 6,290 6,310 6,40 6,800 6,40 6,800 6,40 6,800 6,40 6,800 6,40 6,800 6,40 6,800 6,40 6,800 6,40 6,800 6,40 6,800 6,40 6,800 6,900 6,9	\$5, 360 6, 640 2, 840 3, 200 4, 320 5, 640 4, 950 5, 630 5, 640 1, 210 1, 210 1
44 45	Terrill Road, N. J	5, 300	16 16	8,054.08	30. 1 28. 9	69. 9 71. 1	2,170	6, 620 10, 830 5, 350	9,390 15,500 7,520
46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65	Brewer, Me. Calais, Me. Calais, Me. Camden, Me. Cardon, Me. Dexter, Me. Eden, Me. Gardiner, Me. Houlton, Me. Rumford, Me. Saco, Me. Stowhegan, Me. South Portland, Me. Waterville, Me. Yesler Way, N. J. Valley Road, N. J. Bridge Street, N. J. Whitehouse, N. J. North Crosswicks, N. J. Cheesequakes Creek, N. J. Jamesburg, N. J.	1,575 2,100 750 533 675 1,100 1,200 1,500 6,831 775 1,550 14,020 16,530 700 30,980 1,160 10,400 6,971	24 21 30 37 19 24 21 21 20 35 15 25 40 14 14 16 14 16	1, 486. 75 1, 811.65 1, 712. 52 1, 106. 00 1, 009. 30 3, 012. 18 3, 038. 32 2, 499. 73 7, 364. 80 2, 134. 85 1, 420. 34 2, 726. 40 18, 850. 72 15, 409. 85 2, 374. 79 42, 934. 95 33, 366. 90 10, 782. 65	12. 7 20. 4 50. 9 13. 6 55. 3 50. 7 26. 3 50. 5 32. 5 14. 6 48. 2 13. 7 8. 5 32. 9 43. 6 41. 0 57. 0 9. 9	87. 3 79. 6 49. 1 86. 4 44. 7 49. 3 73. 7 49. 5 67. 5 67. 5 67. 5 67. 1 67. 1	390 660 3,070 610 3,430 4,580 2,510 3,170 1,380 3,500 1,190 1,340 6,140 3,210 1,100 10,340	2,720 2,590 2,960 3,840 2,780 4,450 4,450 3,760 3,100 2,880 5,150 3,760 3,940 10,720 4,630 8,930 7,890	3,110 3,250 6,030 4,450 6,210 9,030 9,540 6,270 4,260 6,030 7,260 8,560 4,150 7,600 5,280 16,860 17,840 10,030 18,150 8,750

¹ See footnote 1, Table 28, p. 86.

Table 29.1—Table showing cost elements of water-bound macadam roads for years 1908-1911—Continued.

		anth Width Metal and			Cost per mile of equiva- lent 15-foot width.			
Location.	Length (feet). Width (feet).	Total cost of work.	Drain- age and grad- ing.	Surfac- ing.	Drain- age and grad- ing.	Surfac- ing.	Total.	
1909—Continued.								
New Brunswick, N. J	6, 340 15, 950 620 6, 120 10, 940 18, 240 6, 180 3, 960	16 16 14 14 14 14 16 16	\$16, 850, 21 26, 599, 42 1, 014, 17 12, 469, 55 26, 714, 22 34, 747, 22 11, 210, 09 10, 246, 74	53. 7 20. 5 21. 8 43. 8 60. 4 47. 7 50. 1 46. 7	46. 3 79. 5 78. 2 56. 2 39. 6 52. 3 49. 9 53. 3	\$7,070 1,690 2,010 5,050 8,510 5,140 4,500 5,980	\$6,100 6,560 7,200 6,470 5,570 5,640 4,480 6,830	\$13, 170 8, 250 9, 210 11, 520 14, 080 10, 780 8, 980 12, 810
	505	01	001 10		05.0	010	F 110	F 050
Bath, Me. Biddeford, Me. Bréwer, Me. Calais, Me. Caribou, Me. Dover, Me. Fort Fairfield, Me. Freeport, Me. Hallowell, Me.	1,680 1,324 1,500 1,400 773 455 832 700 437	21 20 21 40 21 27 36 32 21 39 22 21 21 23 23	831. 12 2, 370. 50 2, 625. 50 1, 996. 84 1, 625. 53 2, 234. 00 1, 222. 56 1, 487. 00 1, 230. 74 1, 240. 90 2, 252. 00 1, 235. 56 1, 821. 93 6, 227. 56	4. 4 31. 5 18. 9 39. 9 39. 9 44. 9 23. 8 49. 7 33. 9 17. 2 33. 4 19. 0 32. 6 27. 0	95. 6 68. 5 81. 1 60. 1 55. 1 76. 2 50. 3 66. 1 82. 8 66. 6 81. 0 67. 4 74. 4 73. 0	1,760 1,410 1,050 1,740 3,810 1,410 2,200 2,250 990 1,930 770 2,230 1,270 1,300	5,110 3,830 6,070 1,590 2,630 4,670 4,500 2,220 4,380 4,770 3,850 3,280 4,600 3,690 3,500	5, 350 5, 590 7, 480 2, 640 4, 370 8, 480 5, 910 4, 420 6, 630 5, 760 5, 780 4, 050 6, 830 4, 960 4, 800
1911.								
Brunswick, Me. Caribou, Me. Hallowell, Me. Houlton, Me. Oldtown, Me. Rumford, Me.	333 500 1,700 800 1,125	21 46 20 21 22 23 21	1,836.82 1,406.24 1,080.00 2,667.10 1,829.07 2,604.47 1,311.21	25. 7 30. 4 19. 2 21. 5 42. 9 18. 5 28. 7	74. 3 69. 6 80. 8 78. 5 57. 1 81. 5 71. 3	1,370 2,210 1,640 1,270 3,530 1,480 1,180	3,950 5,060 6,910 4,640 4,700 6,500 2,920	5,320 7,270 8,550 5,910 8,230 7,980 4,100
1910.								
	21,550 5,280 68,800 18,250	14 14 14 14	36, 425. 67 7, 500. 00 15, 810. 67 34, 747. 92	31. 6 34. 4 43. 2 47. 7	68. 4 65. 6 56. 8 52, 3	3,020 2,770 5,620 5,140	6,540 5,270 7,380 5,630	9,560 8,040 13,000 10,770
Smalley's Corner, N. J Brunswick, N. J	5,340	15 16 14 14 14	22, 759, 49 10, 450, 65 32, 396, 84 20, 633, 71 31, 371, 99	24. 1 15. 4 15. 5 29. 6 37. 6	75. 9 84. 6 84. 5 70. 4 62. 4	1,890 1,490 160 3,300 3,430	5,960 8,200 860 7,850 5,700	7,850 9,690 1,020 11,150 9,130
Total and weighted		15	8,688.00	36, 89	63.11	3,400	5, 815	9, 215
	1909—Continued. Keyport, N. J. Penn's Grove, N. J. Terrill (1), N. J. Green Brook, N. J. Washington Valley, N. J. Washington Valley, N. J. Morris, N. J. New Brunswick, N. J. 1910. Augusta, Me. Bath, Me. Biddeford, Me. Brewer, Me. Calais, Me. Caribou, Me. Dover, Me. Fort Fairfield, Me. Freeport, Me. Houlton, Me. Jay, Me. Oldtown, Me. Rumford, Me. Berwick, Me. 1911. Brunswick, Me. Caribou, Me. Houlton, Me. Houlton, Me. Houlton, Me. Wilton, Me. Houlton, Me. 1910. Ringoes, N. J. Asbury, N. J. Main Street, N. J. Frankford, N. J. 1911. Smalley's Corner, N. J. Brunswick, N. J. Yardville, N. J. Greater Cross Roads, N. J. Buttzville, N. J. Total and weighted	1909—Continued. Keyport, N. J.	1909—Continued. Keyport, N. J. 6,340 16 Penn's Grove, N. J. 15,950 16 Terrill (1), N. J. 620 14 Green Brook, N. J. 6,120 14 Washington Valley, N. J. 10,940 14 Frankford, N. J. 18,240 14 Morris, N. J. 6,180 16 1910.	1909—Continued. Keyport, N. J.	Location. Length (feet). Length (feet). Total cost of work.	1909—Continued. 1909—Conti	Location. Length (feet). Width (feet). Total cost of work. Drainage and grading. Surfacging. Surfacg	Location. Length (feet). Width (feet). Total cost of work. Drainage and grading. Surfacage and grading. Sur

¹ See footnote 1, Table 28, p. 86. ² Miles.

Table 30.1-Table showing cost elements of bituminous-macadam roads for 1908-1911

						tage of st.	Cost pe lent	er mile of 15-foot v	equiva- vidth.
No.	Location.	Length (feet).	Width (feet).	Total cost of work.	Drain- age and grad- ing.	Surfac- ing.	Drain- age and grad- ing.	Surfac- ing.	Total.
	1908.								
1	Kennebunk, Me	426	27	\$1,597.30	25.3	74.7	\$2,780	\$8,220	\$11,000
2	Waterville, Me. ²	760	46	3, 565. 18	11.5	88. 5	930	7, 150	8,080
3 4 5 6 7 8 9 10 11 12 13	Camden, N. J. Evesham, N. J. ³ Hopewell, N. J. ² Trenton, N. J. Helmetta, N. J. Plainsboro, N. J. Terrill, N. J. Stoutsburg, N. J. Edgar, N. J. Washington Avenue, N. J. Walnut Avenue, N. J.	12, 693 12, 838 10, 720 13, 227 14, 271 12, 992 9, 982 10, 845 17, 526 6, 125 6, 313	14 14 18 16 14 14 16 14 16 16 16	29, 043. 42 22, 649. 61 16, 121. 40 24, 509. 44 21, 375. 59 21, 596. 57 26, 404. 08 19, 741. 90 42, 424. 74 14, 230. 20 15, 868. 00	28. 3 20. 8 21. 0 20. 3 11. 3 13. 7 37. 2 22. 0 25. 0 23. 4 19. 7	71. 7 79. 2 79. 0 79. 7 88. 7 86. 3 62. 8 78. 0 75. 0 76. 6 80. 3	3,660 2,080 1,390 1,870 960 1,290 4,870 2,270 2,990 2,690 2,450	9, 290 7, 910 5, 230 7, 320 7, 510 8, 100 8, 230 8, 030 8, 990 8, 810 9, 990	12,950 9,990 6,620 9,190 8,470 9,390 13,100 10,300 11,980 11,500 12,440
	1010								
14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32	Belfast, Me.4. Coffin's Corner, N. J. Nicholson, N. J. Brown's Corner, N. J. Runnymeade, N. J. Runnymeade, N. J. Kingston, N. J. Kingston, N. J. Somerset Street, N. J. Seventh Street, N. J. Morris Plains, N. J. Gladstone, N. J. Pompton, N. J. Union, N. J. Warrenville, N. J. Frankford, N. J. Raritan, N. J. Washington Avenue, N. J. Beattystown, N. J.	580 11, 866 6, 532 8, 601 8, 984 325 6, 458 3, 805 2, 040 8, 700 13, 718 21, 053 15, 516 4, 164 3, 600 17, 309 13, 013 1, 300 45, 341	21 14 14 14 16 16 16 14 14 14 14 14 14 14 14 14 14 14 14	1, 997. 53 25, 138. 87 13, 168. 82 20, 468. 00 19, 408. 76 561. 00 13, 705. 67 6, 555. 88 4, 252. 27 15, 213. 40 33, 176. 53 42, 979. 47 18, 930. 85 12, 251. 98 8, 310. 13 25, 313. 87 40, 820. 75 3, 272. 00 73, 580. 20	43.7 14.8 14.6 24.3 30.9 5.0 13.7 17.9 45.5 14.4 26.9 27.3 29.2 8.1 48.8 37.6 28.1 29.4 40.1	56. 3 85. 2 85. 4 75. 7 69. 1 95. 0 86. 3 82. 1 54. 5 72. 7 70. 8 91. 9 51. 2 62. 4 71. 9 70. 6 59. 9	5,670 1,780 1,660 3,270 3,310 440 1,740 5,380 1,390 3,680 3,130 6,370 3,100 4,360 3,670 3,680	7, 310 10, 220 9, 740 10, 180 7, 390 8, 190 9, 070 6, 440 8, 290 4, 890 4, 890 15, 290 6, 690 5, 170 11, 170 8, 810 5, 500	12, 980 12, 000 11, 400 13, 450 10, 700 8, 620 9, 680 13, 670 11, 820 9, 680 13, 670 11, 450 6, 910 13, 060 8, 530 12, 480 9, 180
33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53	Brunswick, Me	640 750 580 4, 515 859 18, 115 4, 200 8, 362 4, 720 8, 000 9, 800 4, 860 10, 250 10, 250 7, 920 4, 257 7, 920 4, 257 7, 450	21 26 28 14 30 16 14 15 15 15 15 15 15 15 15 15 15	1, 461, 37 1, 621, 35 1, 925, 00 12, 681, 75 4, 587, 51 45, 633, 30 8, 744, 39 26, 965, 52 9, 726, 00 10, 796, 00 5, 547, 00 10, 796, 00 5, 683, 00 14, 492, 00 11, 804, 00 8, 301, 00 8, 301, 00 10, 570, 00 11, 517, 00	11. 2 14. 1 34. 4 28. 1 9. 6 10. 4 35. 4 29. 3 42. 9 39. 4 46. 2 34. 2 39. 0 46. 7 50. 7 50. 5 16. 6 50. 2 24. 9	88. 8 85. 9 90. 4 90. 4 64. 6 76. 6 70. 7 57. 1 60. 6 53. 8 65. 8 65. 8 65. 8 62. 5 83. 4 69. 5 79. 8 75. 1	970 970 930 3,230 4,470 1,350 1,300 4,170 3,788 4,246 4,246 1,814 2,687 2,112 2,911 3,556 5,089 615 3,893 615 3,145 1,947 2,032	7, 660 5, 650 6, 160 11, 450 12, 720 11, 170 7, 692 5, 652 2, 791 3, 130 4, 062 4, 059 4, 948 6, 489 3, 088 7, 167 7, 692 6, 130	8, 630 6, 580 9, 390 15, 920 14, 070 12, 470 11, 770 10, 880 9, 898 4, 605 5, 817 7, 615 10, 037 10, 382 9, 638 3, 703 10, 312 9, 639 8, 162
	Total and weighted averages		15	10, 267. 00	26, 85	73. 15	2,765	7, 533	10, 298

See footnote 1, Table 28, p. 86.
 Bituminous surface coat.
 Bituminous pavement on 2,022 square yards.
 Bituminous-macadam surface 62 per cent.
 Five inches of gravel and a bituminous surface coat.
 Milec

⁶ Miles.

APPENDIX D.

THEORY OF INTEREST APPLIED TO HIGHWAY-BOND CALCULATIONS, WITH SINKING FUND, ANNUITY, AND INTEREST TABLES FOR 60 INTERVALS AND 14 RATES OF INTEREST.

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APPENDIX D.

THEORY OF INTEREST APPLIED TO BOND CALCULATIONS.

Introduction.—This appendix presents briefly the application of the theory of compound interest to highway bonds. There are six important quantities in terms of which the solution of most problems can be expressed. If i is the rate of interest and n the term of years, these quantities are:

The accumulation of 1 at the end of n years, r^n ;

The accumulation of an annuity of 1 per annum at the end of n years, $s_{\overline{n}|}$;

The annual sinking fund which will accumulate to 1 at the end of n years, $1/s_{\overline{n}}$;

The present value of 1 due in n years, v^n ;

The present value of an annuity of 1 per annum for n years, $a_{\overline{n}}$; and

The annuity for n years which 1 will purchase, or the annuity necessary to discharge a debt of 1 in n years with interest, $1/a_{\overline{n}}$.

The first three are accumulative functions and the last three are discount or present value functions.

The mathematical formulas for these six quantities are:

$$egin{aligned} oldsymbol{r}^n = (1+oldsymbol{i})^n & oldsymbol{s}_{\overline{n}} = rac{(1+oldsymbol{i})^n-1}{oldsymbol{i}} & rac{1}{oldsymbol{s}_{\overline{n}}} = rac{oldsymbol{i}}{(1+oldsymbol{i})^n-1} \ & oldsymbol{v}^n = (1+oldsymbol{i})^{-n} & oldsymbol{a}_{\overline{n}} = rac{1-(1+oldsymbol{i})^{-n}}{oldsymbol{i}} & rac{1}{oldsymbol{a}_{\overline{n}}} = rac{oldsymbol{i}}{1-(1+oldsymbol{i})^{-n}} \end{aligned}$$

The values of most of these functions are given more or less completely in published tables of interest.¹

Definitions.—Interest may be defined as the consideration for the use of capital. The capital is called the *principal*.

The rate at which a given principal is earning interest requires the adoption of some interval as the unit of time, and this is usually the year.

It is clear that interest when received may be added to the principal and so in turn earn interest. This process, called *compounding*, takes place at the end of *stated intervals*, as every three months, six months, or year.

 $^{^{1}}$ At the end of this appendix, pages 116 to 127, are short tables to seven places for 60 intervals and 14 interest rates.

Mathematical rates.—The effective rate of interest is the interest earned by one unit of principal (one dollar) in one unit of time (one year) when interest is compounded at the end of each stated interval.

The nominal rate of interest is the total interest earned by one unit of principal (one dollar) in one unit of time (one year) when interest is not compounded at the end of each stated interval.

It follows that the nominal and effective rates of interest coincide only when the *stated interval* is the unit of time (one year).

Commercial rate.—In commercial transactions the rate of interest is usually quoted as a rate *per cent*, or per hundred units of principal, instead of a rate *per unit* of principal, as in the above definitions. To find the mathematical rate as above defined, divide the commercial rate by 100. For example, the mathematical rate corresponding to the commercial rate 6 per cent is 6/100, or .06. The mathematical rate is used in the following formulas.

Relation between effective and nominal rates of interest.— In any transaction there is an effective rate of interest i and a corresponding nominal rate of interest j. This relation can be expressed by an algebraic formula which involves the number of stated intervals, m, in one year. At the nominal rate j, during each stated interval 1/mth of a year in length, one unit of principal would earn j/m in interest which, added to the unit, gives an amount 1+j/m. If the principal 1 accumulates in the first interval to 1+j/m, it follows by proportion that the principal 1+j/m would accumulate in the second interval to $(1+j/m)^2$. In like manner, at the end of the mth interval, the accumulation would be $(1+j/m)^m$. The total interest earned in the m intervals, or one year, is the difference between the accumulation and the original unit of principal, which by definition is the effective rate of interest i. Hence the fundamental formula:

$$\mathbf{i} = (1 + \mathbf{j}/m)^m - 1 \tag{1}$$

or

$$1 + i = (1 + j/m)^m. (2)$$

Solving for j, there results

$$j = m[(1+i)^{1/m} - 1].$$
 (3)

The number of times, m, that interest is added, or converted into principal each year, is the *frequency of conversion*. A nominal rate of interest, convertible m times a year, is indicated by the symbol $j_{(m)}$.

Example 1.—The nominal rate of interest j on deposits is 3% and interest is added to the principal every six months; to find the effective rate i.

Here j=.03 and m=2. From formula (1) there results

$$i = (1 + .03/2)^2 - 1 = (1.015)^2 - 1 = .030225.$$

The effective rate 3.0225% is thus slightly higher than the corresponding nominal rate convertible twice per annum.

Example 2.—The effective rate of interest is 6%; to find the corresponding nominal rate when interest is convertible semiannually.

Here i and m are given to find j; hence from formula (3) there results

$$j=2[(1+.06)^{\frac{1}{2}}-1]=2(1.06)^{\frac{1}{2}}-2=2.059126-2=.059126.$$

It is necessary to extract the square root of 1.06. The final result shows that j=5.9126%, and again the nominal rate is smaller than the corresponding effective rate.

Amount of 1 in n years at compound interest.—Let the effective rate of interest be i. At the end of the first year the accumulation is 1+i. During the second year this principal 1+i will be increased in the ratio of 1 to 1+i, and will therefore amount at the end of the second year to (1+i)(1+i), or $(1+i)^2$. In this way at the end of n years the amount is $(1+i)^n$.

Let P be the principal and S the amount of P at the end of n years at compound interest at the effective rate i. Since 1 amounts to $(1+i)^n$ in n years, P would amount to $P(1+i)^n$. There results, therefore, the formula

$$\mathbf{S} = \mathbf{P}(1+\mathbf{i})^n. \tag{4}$$

Hence

$$P = S/(1+i)^n = Sv^n, \tag{5}$$

where

$$v = 1/(1+i). \tag{6}$$

If in the above formulas 1+i is replaced by $(1+j/m)^m$, to which it is equivalent according to formula (2), it follows that

$$S = P(1+j/m)^{mn}, \tag{7}$$

and where

$$P = S/(1+j/m)^{mn} = Sv^{mn},$$
(8)

$$v = 1/(1+j/m)$$
. (9)

These formulas express the relation between P and S in terms of the nominal rate j and the frequency of conversion m. The values to seven places of decimals of $(1+i)^n$ and v^n for various rates of interest and for 60 intervals or years are given in Tables 31 and 34.

Example 3.—To find the amount of \$12,375 at 3% compound interest in 30 years. By formula (4)

$$S = (1+.03)^{30} \times \$12,375 = 2.4272625 \times \$12,375 = \$30,037.37.$$

The value of $(1.03)^{30}$ was taken from Table 31.

Example 4.—\$12,375 is placed in a bank; to find the amount in 30 years if interest is 3% and is compounded semiannually.

The nominal rate of 3%, convertible twice a year, requires formula (7) with j=.03 and m=2. Substituting, the result is:

 $S = (1 + .03/2)^{2 \times 30} \times \$12,375 = (1.015)^{60} \times \$12,375 = 2.4432198 \times \$12,375 = \$30,234.85.$

The discount factor.—Because of the power of money to earn interest the value of money depends upon the time to which it is referred. Then in order to compare sums of money due at different times, they must be referred to the *same point in time*.

Formula (5) gives the principal P which will accumulate at the effective rate i in n years to the amount S. If S=1 and n=1, the formula gives the present value of 1 due in one year. This is usually denoted by the symbol v, so that

$$v = 1/(1+i) = (1+i)^{-1}$$
.

Similarly $v^2 = 1/(1+i)^2 = (1+i)^{-2}$ is the present value of 1 due in two years, and $v^n = 1/(1+i)^n = (1+i)^{-n}$ is the present value of 1 due in n years.

The symbol v is often called the discount factor, and if it is desired to find the value of money n years before the point in time under consideration, it is necessary only to multiply the quantity by v^n . The factor 1+i, which is frequently denoted by r, is accumulative in character, and formula (4) shows that, to find the value of a quantity of money Q, n years after the point in time under consideration, it is necessary merely to multiply the quantity by $(1+i)^n$.



More generally, when i is the effective rate per interval, the value of Q, at a time n intervals after the point t, is $Q(1+i)^n = Qr^n$, and its value n intervals before point t is $Q(1+i)^{-n} = Qv^n$.

Annuities-certain.—An annuity is a series of payments made at equal intervals during the continuance of a given status.

The status, or condition of payment of the annuity, may take a variety of forms. If the status is a fixed term of years, the annuity is an annuity-certain. Thus payments of one hundred dollars a year for ten years constitute an annuity-certain. The sum of the payments on an annuity in one year, when the payments are of the same amount, is the annual rent.

Payments of twenty-five dollars are made at the end of every month for ten years. This is an annuity-certain with an annual rent of three hundred dollars.

When payments are made at the *end* of each interval, the annuity-certain is said to be *immediate*; when payments are made at the *beginning* of each interval, the annuity-certain is said to be *due*.

Amount of an immediate annuity-certain.—The value of an annuity at the end of its term is called the *amount*. The amount of an immediate annuity-certain for n years with an annual rent 1.

payable at the end of each year, is designated by the symbol $s_{\overline{n}|}$. To find $s_{\overline{n}|}$ each annual payment must be accumulated, at the effective rate of interest i, to the end of the term of the annuity. The first payment of 1 accumulates in n-1 years to $(1+i)^{n-1}$; the second payment of 1, in n-2 years, to $(1+i)^{n-2}$; etc. . . . ; the (n-1)th payment of 1, in 1 year, to (1+i); and the nth payment at the end of the term is 1. Adding the separate amounts in reverse order, there results

$$s_{\overline{n}} = 1 + (1+i) + (1+i)^2 + \dots + (1+i)^{n-1}$$

The sum of this geometric series is

$$s_{\overline{n}|} = \frac{(1+i)^n - 1}{i} \tag{10}$$

Values of this quantity are given for various rates of interest and terms in Table 32.

Example 5.—To find the accumulation in 47 years of an annual sinking fund of 1% of \$1,000,000, if the fund is credited annually with 3% compound interest.

This is an application of formula (10) where n=47 and i=.03; since $s_{\overline{47}|}=100.3965009$ the accumulation will be

 $100.3965009 \times \$10.000 = \$1.003.965.01$.

The same principles may be applied to find the amount of an annuity for n years with annual rent 1 payable in p equal installments during each year. The amount of such an annuity is designated by the symbol $s^{(p)}_{\overline{n}}$, and its value is represented by the following formula:

$$s_{\overline{n}|}^{(\underline{p})} = \frac{(1+i)^n - 1}{p[(1+i)^{1/p} - 1]}.$$
(11)

If 1+i is replaced by $(1+j/m)^m$ in accordance with formula (2), the amount of the annuity is then expressed in terms of the nominal rate of interest j with frequency of conversion m, thus:

$$s_{\overline{n}|} = \frac{(1+j/m)^{mn} - 1}{(1+j/m)^m - 1},\tag{12}$$

$$s_{n}^{(p)} = \frac{(1+j/m)^{mn} - 1}{p[(1+j/m)^{m/p} - 1]}$$
(13)

Example 6.—What will be the accumulation in 47 years of an annual sinking fund of 1% of \$1,000,000, paid in semiannually, if the fund is credited as received with 3% interest compounded annually?

This is an application of formula (11) where n=47, p=2, i=.03, hence

$$s_{\frac{47}{47}|}^{(2)} = \frac{(1+.03)^{47}-1}{2\left[(1+.03)^{\frac{1}{2}}-1\right]} = \frac{3.0118950}{.0297783} = 101.143954$$

and the accumulation will be $101.143954 \times \$10,000 = \$1,011,439.54$.

The special case where interest is converted with the same frequency as the payment of annuity installments, or when m=p, deserves particular mention. Formula (13) then reduces to

$$\mathbf{s}_{\overline{n}|}^{(\underline{p})} = \frac{1}{p} \cdot \frac{(1 + \mathbf{j}/p)^{np} - 1}{\mathbf{j}/p} = \frac{1}{p} \cdot s_{\overline{np}|}, \tag{14}$$

where $s_{\overline{np}}$ is to be taken at the effective rate j/p.

Example 7.—What will be the accumulation in 47 years of an annual sinking fund of 1% of \$1,000,000, paid in semiannually, if the fund is credited with a nominal rate of 3% convertible twice a year?

This is an application of formula (14) where n=47, p=2, and $s_{\overline{94}}$ is taken at $1\frac{1}{2}\%$;

hence

$$\frac{1}{2}s_{94} \times \$10,000 = \$1,017,764.25.$$

Sinking fund which will amount to 1.—An annuity with annual rent of 1 will amount in n years to $s_{\overline{n}}$; it follows that an annuity with annual rent of $1/s_{\overline{n}}$ will amount in n years to 1. The quantity $1/s_{\overline{n}}$ is the $sinking\ fund$ which will accumulate to 1 in n years.

Values for this important function

$$\frac{1}{s_{n}} = \frac{i}{(1+i)^{n} - 1} \tag{15}$$

are given for various rates of interest and for terms ranging from 1 to 60 intervals or years in Table 33.

Example 8.—To find an annual sinking fund, which, credited with 3% compound interest, will accumulate in 50 years to \$1,000,000.

Applying formula (15) where n=50, and i=.03, there results $1/s_{\overline{s}\,\overline{o}\,|}=.0088655$. Therefore the required sinking fund is

$$.0088655 \times \$1,000,000 = \$8,865.50.$$

In like manner $1/s^{(p)}_{\overline{n}|}$ is the annual rent of an annuity which, at the nominal rate j convertible m times a year, will accumulate to 1 in n years. The annual rent is payable in p installments during each year; hence each installment is equal to $1/ps^{(p)}_{\overline{n}|}$. The installments may be regarded as the sinking fund, payable at the end of every pth part of a year, which in n years will accumulate to 1. The amount of each payment to the sinking fund is

$$\frac{1}{ps^{(p)}_{n}} = \frac{(1+j/m)^{m/p} - 1}{(1+j/m)^{mn} - 1}$$
 (16)

When p=1 and m=2, formula (16) gives the value of the annual sinking fund which, improved at compound interest semiannually, will accumulate in n years to 1.

The formula simplifies to the following:

$$\frac{(1+j/2)^2-1}{j/2} \cdot \frac{j/2}{(1+j/2)^{2n}-1} = s_{\overline{2}} \cdot \frac{1}{s_{\overline{2n}}}$$
 at $j/2\%$. (17)

This formula is of considerable practical importance because payments to the sinking fund are usually made annually and the fund

credited with interest semiannually. Table 6, on page 15, was calculated by formula (17).

Example 9.—To find the annual payment which will accumulate in 20 years to \$100,000 when interest is $3\frac{1}{2}$ per cent compounded semiannually.

Taking n=20 and j=.035 and consulting Tables 32 and 33 with $1\frac{\pi}{4}$ per cent interest for values of $s_{\overline{2}|}$ and $1/s_{\overline{40}|}$, respectively, there results:

$$s_{\overline{2}}$$
 · $\frac{1}{s_{\overline{40}}} = 2.0175 \times .0174721 = .0352500$.

Hence the annual payment to sinking fund is

$$.0352500 \times \$100,000 = \$3,525.00$$

Example 10.—To find the sinking fund, which set aside semiannually and accumulated as received, with 3% compound interest, will amount in 50 years to \$1,000,000. Here formula (16) is used with p=2, m=1, j=.03, n=50, and

$$\frac{1}{2s^{\frac{(2)}{50}}} = \frac{(1+.03)^{\frac{1}{2}}-1}{(1+.03)^{50}-1} = .00439999.$$

The required sinking fund is therefore

$$.00439999 \times \$1,000,000 = \$4,399.99$$

In the special case when the frequency of conversion coincides with the number of payments per annum, or m=p, the amount of each payment to the sinking fund is

$$\frac{1}{p s_{\overline{n}|}^{(p)}} = \frac{j/p}{(1+j/p)^{np}-1} = \frac{1}{s_{np}},\tag{18}$$

where $s_{\overline{np}}$ is to be taken at rate j/p.

Example 11.—To find a sinking fund which, set aside semiannually and credited with a nominal rate of 3% convertible twice a year, will accumulate in 30 years to \$1,000,000.

Here apply formula (18) by substituting p=2, j=.03, and n=30; this gives

$$\frac{1}{2s_{\overline{90}|}^{(2)}} = \frac{1}{s_{\overline{60}|}} = .0103934,$$

where $1/s_{\overline{60}|}$ is taken at $1\frac{1}{2}\%$. Then the sinking fund which would accumulate to \$1,000,000 is

$$.0103934 \times \$1.000.000 = \$10.393.40$$
.

Four important cases of sinking funds are illustrated in the preceding examples. They arise from the fact that payments to a sinking fund may be annual or semiannual and interest on a sinking fund annual or semiannual. Formula (16) covers all of them when p and m are properly chosen. The following schedule illustrates this fact:

Case.	p	Sinking-fund payments.	m	Interest on sinking fund.	Illus- trated in example.
1 2 3 4	$\begin{array}{ c c }\hline 1\\1\\2\\2\\2\end{array}$	Annual Annual Semiannual Semiannual	$\begin{array}{c} 1 \\ 2 \\ 1 \\ 2 \end{array}$	Annual Semiannual Annual Semiannual	8 9 10 11

In most cases in the illustrative tables in the body of this bulletin, for simplicity of presentation, annual payments and annual interest are assumed, whereas in practice usually annual payments and semi-annual interest are employed.

Present value of an immediate annuity-certain.—The present value of an immediate annuity-certain for n years, with annual rent 1 payable at the end of each year, is designated by the symbol $a_{\overline{n}}$.

It is equal to the sum of the present values of 1, due at the succeeding yearly intervals. By formula (5) the present value of 1, due at the end of one year at the effective rate of interest i, is v=1/(1+i); at the end of two years, $v^2=1/(1+i)^2$, etc. ; at the end of n years, $v^n=1/(1+i)^n$. Hence

$$a_{\overline{n}} = v + v^2 + \dots + v^n$$

= $\frac{1}{1+i} + \frac{1}{(1+i)^2} + \dots + \frac{1}{(1+i)^n}$.

The sum of this geometric series is

$$a_{\overline{n}|} = \frac{1 - v^n}{i} = \frac{1 - (1 + i)^{-n}}{i}$$
 (19)

and its values are given in Table 35.

Example 12.—To find the present value at 3% of an annual payment of 856,325 at the end of each year for thirty years.

Referring to Table 35, it is seen that $a_{\overline{30}|}$ at 3% is 19.6004413, and therefore the equired present value is

$$19.6004413 \times \$56,325 = \$1,103,994.86$$

While the above demonstration relates to an annuity of 1 per annum, payable at the end of each year, the same principles apply to finding the present value of an annuity of 1 per annum, payable in p installments during each year. The present value of such an annuity is designated by the symbol $a^{(p)}_{ni}$, and its value is represented by the following formula:

$$a_{\overline{n}|}^{(p)} = \frac{1 - v^n}{p[(1+i)^{1/p} - 1]} = \frac{1 - (1+i)^{-n}}{p[(1+i)^{1/p} - 1]}$$
(20)

In formulas (19) and (20) the values of the annuities are expressed in terms of the effective rate i. If (1+i) is replaced by $(1+j/m)^m$ in accordance with formula (2), there result the present values of the same annuities expressed as follows in terms of the nominal rate of interest j, with frequency of conversion m:

$$a_{\overline{n}|} = \frac{1 - (1 + j/m)^{-mn}}{(1 + j/m)^m - 1},$$
 (21)

and

$$a_{\overline{n}|}^{(p)} = \frac{1 - (1 + j/m)^{-mn}}{p[(1 + j/m)^{m/p} - 1]}.$$
 (22)

Fundamental relations between the present value and the amount of an annuity.—Since $a_{\overline{n}|}$ and $s_{\overline{n}|}$ are the values of the same annuity upon two dates differing by n years, it follows by the principle of reduction of values from one date to another, explained on page 95, that

$$a_{\overline{n}|} = v^n s_{\overline{n}|}, \ s_{\overline{n}|} = (1+i)^n a_{\overline{n}|},$$

and in like manner that

$$a^{(\underline{p})}_{\underline{n}|} = v^n s^{(\underline{p})}_{\underline{n}|},$$

$$s^{(\underline{p})}_{\underline{n}|} = (1+i)^n a^{(\underline{p})}_{\underline{n}|}.$$

As tables are not published giving the values of $a_{\overline{n}|}^{(p)}$ and $s_{\overline{n}|}^{(p)}$, when p is different from 1, it is desirable for purposes of computation to express a relation between these functions and the tabulated functions $a_{\overline{n}|}$ and $s_{\overline{n}|}$. This can easily be done by accumulating to the end of each year the p payments of 1/p which in $a_{\overline{n}|}^{(p)}$ and $a_{\overline{n}|}^{(p)}$ are distributed at equal intervals through the year. By formula (11) this accumulation to the end of each year will be equal to

$$s^{(p)}_{\overline{1}|} = \frac{i}{p[(1+i)^{1/p}-1]} = \frac{i}{j_{(p)}} \cdot$$

This converts the annuity into one with annual rent $s_{1}^{(p)}$ payable at the end of each year for n years. Therefore

$$a_{\overline{n}|}^{(p)} = s_{\overline{1}|}^{(p)} a_{\overline{n}|}, \tag{23}$$

$$\boldsymbol{s}_{\overline{n}|}^{(p)} = \boldsymbol{s}_{\overline{1}|}^{(p)} \boldsymbol{s}_{\overline{n}|}. \tag{24}$$

The most frequent intervals in practice are semiannual, quarterly, and monthly, and to meet this requirement the values of $s_{\overline{1}|}^{(2)}$, $s_{\overline{1}|}^{(4)}$, and $s_{\overline{1}|}^{(12)}$ are given below for various rates of interest.

	Values of $s^{(\underline{p})}_{\overline{1} } = i j_{(p)} = \frac{i}{p[(1+i)^{1/p}-1]}$									
p	1½%	134%	2%	21/4%	21/2%	234%	3%			
2 4 12	1.00373604 1.00560755 1.00685652	1.00435603 1.00653878 1.00799571	1.00497525 1.00746906 1.00913389	1. 00559371 1. 00839839 1. 01027107	1.00621142 1.00932677 1.01140725	1.00682837 1.01025422 1.01254243	1. 00744458 1. 01118072 1. 01367662			
p	3½%	4%	4½%	5%	5½%	6%	7%			
2 4 12	1.00867475 1.01303094 1.01594203	1.00990195 1.01487744 1.01820351	1.01112621 1.01672026 1.02046109	1.01234754 1.01856942 1.02271479	1. 01356596 1. 02039495 1. 02496465	1.01478151 1.02222688 1.02721070	1.01720402 1.02588002 1.03169143			

Example 13.—What is the present value of an annuity for 30 years at effective rate 3%, payable in monthly installments of \$25?

By formula (23) with n=30, p=12, i=.03,

$$a^{\frac{(12)}{30|}} \!\!=\!\! s^{\frac{(12)}{1|}} \cdot a_{\overline{30|}} \!\!=\!\! 1.01367662 \times 19.6004413 \!\!=\!\! 19.86850909.$$

Therefore the present value of a similar annuity of \$25 per month, or with annual rent of \$300, is

The annuity which 1 will purchase.—The present value a_{n} of an annuity may be viewed as the principal which, invested at the effective rate of interest i, will provide a payment of 1 at the end of each year and will not be exhausted until the end of the nth year; in other words, $a_{\overline{n}|}$ is just sufficient to purchase an n year annuity of annual rent 1 payable at the end of each year. By proportion it appears that 1 will purchase an n year annuity of annual rent $1/a_{\overline{n}}$ payable at the end of each year. This quantity may be described as the annuity which 1 will purchase, and its value is

$$\frac{1}{a_{n}} = \frac{i}{1 - v^{n}} = \frac{i}{1 - (1 + i)^{-n}}.$$
 (25)

This function is of great importance in annuity bond calculations, and its values are given for 60 terms and different rates of interest in Table 36, on pages 126 and 127.

Example 14.—To find the uniform annual payment which in 20 years will discharge a loan of \$100,000, including both principal and interest, at 5 per cent compounded annually.

In this case n=20, i=.05; employing formula (25) and referring to Table 36, it follows that a loan of 1 will be discharged, both principal and interest, by an annual payment of

 $\frac{1}{a_{20}} = .0802426;$

hence the loan of \$100,000 will be likewise discharged by an annual payment of $.0802426 \times $100,000 = $8,024.26$.

By similar reasoning it follows that 1 will purchase an immediate annuity-certain with annual rent $1/a^{(p)}_{\overline{n}}$, payable in p installments each year. The value of each *periodical installment* is

$$\frac{1}{pa_{n}^{(p)}} = \frac{(1+j/m)^{m/p} - 1}{1 - (1+j/m)^{-mn}},$$
(26)

where interest is at the nominal rate j with frequency of conversion m. When m=1, the nominal rate $j_{(1)}$ becomes the effective rate i. When the conversion of interest occurs with the same frequency as the periodical payment, that is, when m=p, formula (26) reduces to the important particular case

$$\frac{1}{pa_{\frac{(p)}{n}}} = \frac{j/p}{1 - (1 + j/p)^{-np}} = \frac{1}{a^{\frac{n}{np}}},$$
(27)

where $a_{\overline{np}}$ is to be taken at j/p per cent.

Example 15.—To find the half yearly payment at 5% compounded semiannually which will discharge both principal and interest on a loan of \$100.000 in three years.

By formula (27) with n=3, p=2, a loan of 1 will be discharged, both principal and interest, in three years by a semiannual payment of

$$\frac{1}{a_{6} (\text{taken at } 2\frac{1}{2}\%)} = .1815500.$$

and the loan of \$100,000 will be discharged in like manner by

Installment annuity loan.—The preceding example shows how the function $1/a_n$ may be employed to determine the periodical fixed payment which in n years will discharge both principal and interest on a loan. It is to be noted particularly that the lender receives interest throughout the term of the loan on all *outstanding* principal. The following schedule, based on the above example, illustrates the progress of the loan.

Schedule I.—Showing repayment of principal and interest on a loan of \$100,000 by six equal semiannual payments, each of \$18,155; interest 5 per cent, compounded semiannually.

Year.	Principal outstand- ing at beginning of interval.	Interest for interval.	Semiannual payment.	Principal repayment for interval.
$1 \\ 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 2 \\ 1 \\ 2 \\ 3$	\$100, 000. 00 84, 345. 00 68, 298. 63 51, 851. 10 34, 992. 38 17, 712. 19	\$2, 500. 00 2, 108. 63 1, 707. 47 1, 296. 28 874. 81 442. 81	\$18, 155. 00 18, 155. 00 18, 155. 00 18, 155. 00 18, 155. 00 18, 155. 00	\$15, 655. 00 16, 046. 37 16, 447. 53 16, 858. 72 17, 280. 19 17, 712. 19
Totals	357, 199. 30	8, 930. 00	108, 930. 00	100, 000. 00

The initial invested principal of \$100,000 earns \$2,500 interest during the first half year; the first payment of \$18,155.00 takes care of this and there remains a balance of \$15,655.00 which goes to reduce the outstanding principal to \$84,345.00, beginning with the second half year. This process is repeated until the end of the third year, when the last outstanding principal is retired. When preparing such a schedule, the work can be checked by adding the columns. It is evident from the nature of the calculations that, for example, if the first row were omitted from this schedule, the remaining five would represent the schedule for a loan of \$84,345.00 on the same terms as the original loan, except that it would be discharged in two and one-half years by five equal semiannual payments. It must therefore be the present value of the five payments, that is,

$$a^{\frac{1}{5}} \times \frac{\$100,000}{a^{\frac{1}{6}}} = \$84,345.00,$$

where the annuities are taken at $2\frac{1}{2}$ per cent. Similarly, by successively employing $a_{\overline{4}|}$, $a_{\overline{3}|}$, $a_{\overline{2}|}$, and $a_{\overline{1}|}$, all at $2\frac{1}{2}$ per cent, as multipliers, the figures in the first column of principal outstanding at the beginning of the interval could be obtained. When these are known, the figures in the second column are obtained by multiplying the corresponding figures in the first column by the interest rate for the interval, .025; in the fourth, by successive subtractions of the figures

in the first; and in the third, by adding those in the second to those in the fourth as a check.

Generalization of the annuity loan.—The preceding discussion can most easily be generalized by considering the loan of $a_{\overline{n}|}$ dollars where both principal and interest at effective rate i per annum are discharged by equal annual installments of 1 at the end of each year for n years. The initial principal is $a_{\overline{n}|}$; the interest, $ia_n = 1 - v^n$; the annual payment, 1, of which $1 - (1 - v^n) = v^n$ is applied to repayment of principal. But $a^{\overline{n}|} - v^n = a_{\overline{n-1}|}$; hence the outstanding principal at the beginning of the second year is $a_{\overline{n-1}|}$, as might have been predicted in advance. A repetition of this process leads to the following schedule:

Schedule II.—Showing repayment of principal and interest at effective rate i per annum on a loan of $a_{\overline{n}}$ by equal annual payments of 1 at the end of each year for n years.

Year.	Principal outstanding at begin- ning of year.	Interest due at end of year.	Annual pay- ment at end of year.	Principal repaid at end of year.
1 2 3 : k : n	$\begin{array}{c} a_{\overline{n} } \\ a_{\overline{n-1} } \\ a_{\overline{n-2} } \\ \vdots \\ a_{\overline{n-k+1} } \\ \vdots \\ a_{\overline{1} } \end{array}$		1 1 1 : 1	v^{n} v^{n-1} v^{n-2} \vdots v^{n-k+1} \vdots
Totals	$(n-a_{\overline{n }})/i$	$n-a_{\overline{n} }$	n	$a_{\overline{n} }$

Since this is a schedule for a loan of $a_{\overline{n}|}$, if each item in it, apart from those in the column headed "year," is divided by $a^{\overline{n}|}$ and multiplied by L, there results the corresponding schedule for a loan of L dollars.

For example, the items on a loan of L dollars for the kth year would be

$$La_{n-k+1}/a_{\overline{n}}, L(1-v^{n-k+1})/a_{\overline{n}}, L/a_{\overline{n}}, Lv^{n-k+1}/a_{\overline{n}}.$$
 (28)

There are some curious properties revealed by the above schedule, among which the following may be pointed out. The principal repayments on an annuity loan increase in geometrical progression, the factor being 1+i. The sum of these repayments is $a_{\overline{n}}$; the sum of the annual payments is n; the total interest is $n-a_{\overline{n}}$; and the check on the first and second columns shows that

$$i(a_{\overline{1}} + a_{\overline{2}} + \ldots + a_{\overline{n}}) = n - a_{\overline{n}}.$$

It is apparent that most of the items in the schedule can be filled in directly from the $a^{\overline{n}}$ and v^n tables. Having thus filled in each

number, it would be necessary only to multiply each item by $L/a^{\overline{n}}$ to obtain the corresponding schedule for a loan of L.

If in the preceding discussion *year* is replaced by *interval*, the schedule may be made to apply to loans repaid by equal installments at the end of each interval.

Relation between annuity which 1 will purchase and sinking fund which will amount to 1.—The important relation

$$\frac{1}{a_{\overline{n}}} = \frac{1}{s_{\overline{n}}} + i \tag{29}$$

can easily be verified by substitution of the values of $1/a^{\overline{n}}$ and $1/s^{\overline{n}}$ expressed in terms of i, by formulas (25) and (15).

The relation (29) merely expresses the fact that the annual rent, $1/a^{\overline{n}}$ on the annuity which 1 will purchase, must include, not only the interest i on the unit so invested, but also a sinking fund, $1/s^{\overline{n}}$, which will accumulate to the invested unit at the end of the term of the annuity.

Application to bond calculations.—An important application of the theory of compound interest and annuities arises in the valuation of bonds. First to determine the value of a bond issue redeemable in one sum on a given date, with interest, or dividends, on the outstanding bonds at rate g, and all computed, or *valued*, so as to yield the purchaser a given effective rate of interest i. Consider an issue of \$100,000 highway bonds, denomination \$500, dated January 1, 1914, maturing January 1, 1948, interest 5 per cent, payable annually.

The annual interest, or dividends, on these bonds is 5 per cent, and the bonds are redeemed at the end of 34 years. Suppose an intending purchaser desires to pay a price which will yield a net income of 3 per cent on his investment; how much ought he to bid? This is the nature of the general problem. If the purchaser desires to realize 5 per cent on his investment, he must bid \$100,000 for the bonds, or \$1 for each dollar to be redeemed. If, however, he is content with 3 per cent, more than \$100,000 must be paid for the bonds, that is, more than \$1 for each dollar to be redeemed. In this case the bonds are said to be bought at a premium; if less than \$1 is paid for each dollar to be redeemed, the bonds are said to be bought at a discount.

In the general case, let C denote the price to be paid on redemption; i, the effective rate of interest employed in the valuation of the bonds, which is the *net income* rate to the purchaser; g, the *ratio* of the dividend per annum to C; n, the number of years after which the bonds are redeemed; K, the present value of C, due n years hence,

at the effective rate of interest i; and A, the present value of, or bid on, the bonds.

In the above illustration C=100,000, and n=34. The dividend or interest per annum is 5,000. Hence g=5,000/100,000=.05.

Returning to the general problem, the value of the bonds, so far as the purchaser or holder is concerned, consists of two parts:

- 1. The annual interest, or dividend, to be received.
- 2. The sum to be redeemed at the end of n years.

Hence, to find the present value, A, of the bonds, the present value of each of these parts must be determined and added together. The interest per unit of the redemption price C is, by definition, g; if the interest on 1 unit is g, the interest on C units is g. Hence at the end of every year for n years the holder will receive g C units.

	Dividend		Redemption payment, C		
	payments gC	gC	gC	gC	
!	1 yr.	2 yrs.	n-1 yrs.	n yrs.	

It is evident that these interest or dividend payments of gC at the end of every year constitute an immediate annuity-certain of annual rent gC and term of n years. The value of such an annuity with annual rent 1 is $a_{\overline{n}}$; hence the value of the annuity with annual rent gC is

$$gC a_{\overline{n}},$$

where $a_{\overline{n}}$ is to be taken at the rate of interest *i* to be employed in the valuation of the bonds, a rate which in general is different from g, the rate of dividend.

By formula (5), the present value of the sum C, to be redeemed in n years, is $v^n = C$.

Adding these parts together, the result is

$$A = v^n C + g C a_n.$$

Substituting in this relation the value of $a_{\overline{n}i}$ given by formula (19), it follows that

$$A=v^nC+\frac{g}{i}(C-v^nC).$$

Since, by definition, $K=v^nC$, the bid is given by

$$\mathbf{A} = \mathbf{K} + \frac{\mathbf{g}}{\mathbf{i}} (\mathbf{C} - \mathbf{K}) \tag{30}$$

and the premium by

$$A - C = (C - K) \frac{(g - i)}{i}$$
 (31)

If in formula (31) the total sum to be redeemed is regarded as unity, then C=1 and $K=v^n$, the present value of 1 due in n years, and there results

$$A = 1 + \frac{(1 - v^n)}{i} (g - i) = 1 + (g - i) a_{\bar{n}j}$$
 (32)

In this formula $a_{\overline{n}_i}$ is taken at i per cent, and gives the bid on a bond where the sum to be redeemed is 1. Denoting the excess of A over 1 by k, which is called the *premium*, formula (32) becomes

$$\boldsymbol{k} = (\boldsymbol{g} - \boldsymbol{i}) \boldsymbol{a}_{\overline{n}|}^{i\%}, \tag{33}$$

where the *i* per cent over the symbol $a_{\overline{n}}$ means that the function is to be taken from the *i* per cent annuity table.

This is the fundamental formula in bond calculations. It admits of a very simple interpretation, for it states that the premium on a bond is equal to the present value of an n year annuity at i per cent whose annual rent is the excess (g-i) of the nominal rate of dividend of the bond over the effective rate of interest i, desired to be realized by the investor.

The dividend paid each year on each unit of the bond to be redeemed is g, which may be divided into two parts, i and g-i. For the first part the investor pays 1 and in return receives interest of i each year and the 1 is redeemed at the end of n years. For the second part the investor pays the premium, $k = (g-i)a_{\overline{n}}$, and this is repaid, both principal and interest at rate i, in n equal annual installments of (g-i). A portion of each installment goes toward the repayment of the premium k which is eventually reduced to zero. This is called the amortization or writing off of the premium.

It is thus seen that, if k is positive, the bond is bought at a premium; and if k is negative, it is bought at a discount. Since $a_{\overline{n}}$ is always positive, it appears from formula (33) that the sign of k will be positive when g is greater than i, or when the rate of dividend is greater than the rate of interest used in valuation; conversely, when g is less than i, k is negative.

Example 16.—To find the bid on the highway bond mentioned on page 104, on the hypothesis that the purchaser wishes to realize 3% on his investment.

Consider a dollar (unit) of the loan C=100,000. Here n=34, g=.05, i=.03, and by formula (33),

$$k = (.05 - .03)a_{\overline{34}|}^{3\%} = .02 \times 21.1318367 = .422636734,$$

or the premium is slightly over 42 cents on the dollar. Since for each dollar of the loan the purchaser must pay \$1.422636734, for the whole loan of \$100,000 he must pay

Dividends payable and interest convertible semiannually.—When the net income interest rate desired by the investor is nominal, say $j_{(m)}$, and the dividends per unit of the sum to be redeemed are paid in m equal installments, g/m, during the year, it is evident that it is a case of m times n intervals with g/m as dividend and j/m as the effective rate of interest per interval. Hence formula (33) becomes

$$k = \frac{(g-j)}{m} a_{mn}^{j/m\%}$$
 (34)

In particular, if the net income is $j_{(2)}$, and the dividend payments are semiannual,

$$k = \frac{(g-j)}{2} a_{2n|}^{j/2\%}$$
 (35)

This formula provides for the valuation of all bonds, redeemed in one sum at the end of a term of n years and with semiannual dividends. Particular attention is called to the fact that the annuity must be taken for the term 2n, and at the rate of interest j/2.

Example 17.—What is the bid on \$100,000 highway 5% bonds maturing at the end of 3 years, interest payable semiannually, to net purchaser a nominal rate of 4% convertible half-yearly?

Here
$$n=3$$
, $g=.05$, $j=.04$, $m=2$, and formula (35) gives
$$k=\frac{(.05-.04)}{2}a\frac{2\%}{6|}=.005\times5.6014309=.0280071545.$$

Hence the premium on \$100.000 is \$2,800.72, and the corresponding bid is \$102.800.72. The progress of this bond loan is illustrated in the following schedule.

SCHEDULE III.

Year.	Book value or principal at be- ginning of half- year.	Semiannual interest of 2% .	Semiannual dividend of $2\frac{1}{2}\%$ on bonds.	Amortiza- tion of pre- mium at end of half-year.	Redemption payment at end of half- year.
$ \begin{array}{c} 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 2 \\ 2 \\ 3 \end{array} $	\$102, 800. 72 102, 356. 73 101, 903. 86 101, 441. 94 100, 970. 78 100, 490. 20	\$2,056.01 2,047.13 2,038.08 2,028.84 2,019.42 2,009.80	\$2, 500. 00 2, 500. 00 2, 500. 00 2, 500. 00 2, 500. 00 2, 500. 00 2, 500. 00	\$443. 99 452. 87 461. 92 471. 16 480. 58 490. 20	0.00 0.00 0.00 0.00 0.00 0.00 \$100,000.00
Totals	609, 964. 23	12, 199. 28	15, 000. 00	2, 800. 72	100, 000. 00

At the outset the holder has an investment of \$102,800.72 upon which, at 2 per cent, at the end of the first half-year, \$2,056.01 interest is due; the dividend payment of \$2,500.00 then made on the bonds provides for this interest and a balance of \$443.99 remains, which is applied to amortize or write off the premium so that the book-value, or invested principal, is reduced to \$102,356.73 at the beginning of the second half-year. This process continues for three years until the entire premium of \$2,800.72 is written off and the bonds are redeemed by the payment of \$100,000. The various columns are added and the checks upon these totals are obvious.

Example 18.—What is the bid on \$100,000 highway 3% bonds maturing at the end of 3 years, interest payable semiannually, to net purchaser a nominal rate of 4% convertible half-yearly?

Here n=3, g=.03, j=.04, m=2, and formula (35) gives

$$k\!=\!\frac{(.03-.04)}{2}a\frac{2\%}{6|}\!=\!-.005\!\times\!5.6014309\!=\!-.0280071545.$$

Hence the *discount* on \$100,000 is \$2,800.72, and the corresponding bid is \$97,199.28. The progress of this bond loan is illustrated in the following schedule.

SCHEDULE IV.

Year.	Book value or principal at beginning of half-year.	Semiannual interest of 2%.	Semiannual dividend of $1\frac{1}{2}\%$ on bonds.	Accumulation of discount at end of half-year.	Redemption payment at end of half-year.
$ \begin{array}{c} 1 \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 2 \\ 2 \\ 3 \end{array} $	\$97, 199. 28 97, 643. 27 98, 096. 14 98, 558. 06 99, 029. 22 99, 509. 80	\$1, 943. 99 1, 952. 87 1, 961. 92 1, 971. 16 1, 980. 58 1, 990. 20	\$1,500.00 1,500.00 1,500.00 1,500.00 1,500.00 1,500.00	\$443. 99 452. 87 461. 92 471. 16 480. 58 490. 20	0.00 0.00 0.00 0.00 0.00 0.00 \$100,000.00
Totals	590, 035. 77	11, 800. 72	9, 000. 00	2, 800. 72	100, 000. 00

In this case the holder has an initial investment of \$97,199.28, and at the end of the first half-year 2 per cent interest, or \$1,943.99, is due. The dividend payment of \$1,500.00, then made on the bonds, is not sufficient to provide for this interest, and the difference of \$443.99 is added to the principal and determines the book value at the beginning of the second half-year. This is called the accumulation or writing on of discount. By continuing this process for three years the entire discount of \$2,800.72 is written on the initial principal, and the book value, \$100,000, is then redeemed. The totals of the several columns may be used to check the numerical work.

Valuation of bonds redeemed in installments.—For the valuation of bonds which are not redeemed in one sum, but in a series of installments, first consider the simpler case where the dividend payments are annual and the rate of interest is the effective rate i. Let C_1, C_2, \ldots, C_r , denote the successive installments by which

the bonds are to be redeemed;

 $n_1, n_2, \ldots n_r,$

 K_1, K_2, \ldots, K_r

the respective number of years after which the successive installments become due:

the present values, at the effective rate of interest i, of

 C_1 due n_1 years hence, C_2 due n_2 years hence,

 C_r due n_r years hence;

g, the fixed rate of dividend to be paid on the outstanding bonds;

i, the effective rate of interest employed in the valuation of the bonds, which is the *net income* rate to the purchaser:

and $A_1, A_2, \ldots A_r$,

the present values, at the effective rate i, of the separate installments with their respective dividends.



Each installment redeemed may be regarded as furnishing a distinct problem under formula (30) so that, in order to value the entire bond issue, it may be treated as made up of r distinct issues and, after finding the value of each one, they may be added together for the value or bid on the total issue.

By formula (30) in the case of a single issue of C_1 at *net income* rate i, dividend rate g, due in n_1 years, the present value, or bid, A_1 , is:

Adding,

$$\begin{split} (\dot{A}_1 + A_2 + \ldots + A_r) &= (K_1 + K_2 + \ldots + K_r) \\ &+ (g/i)[(C_1 + C_2 + \ldots + C_r) - (K_1 + K_2 + \ldots + K_r)]. \end{split}$$

The total sum to be redeemed, $C_1 + C_2 + \ldots + C_r$, is denoted by C; the total present value of C_1 in n_1 years, C_2 in n_2 years, and so on, which by definition is equal to $K_1 + K_2 + \ldots + K_r$, by K; and the total value of the issue, $A_1 + A_2 + \ldots + A_r$, by A; then for the bid there results

$$\mathbf{A} = \mathbf{K} + (\mathbf{g}/\mathbf{i}) \ (\mathbf{C} - \mathbf{K}), \tag{36}$$

and for the premium,

$$\mathbf{A} - \mathbf{C} = (\mathbf{C} - \mathbf{K}) (\mathbf{g} - \mathbf{i})/\mathbf{i}. \tag{37}$$

It thus appears that formulas (30) and (31), which were derived before for the case of a bond issue redeemed in one sum, hold also for the more general issue redeemed in any number of installments.

Installment bonds when total sum to be redeemed is 1.— When 1 is the total sum to be redeemed, that is, when C=1, formula (37) becomes

$$A-1=(1-K)(g-i)/i,$$
 (38)

where A is the value of each unit of the sum to be redeemed, and K is the present value of the various parts of the unit at effective rate i due in n_1, n_2, \ldots, n_r years. Letting A-1=k, formula (38) becomes

$$\boldsymbol{k} = (1 - \boldsymbol{K}) (\boldsymbol{g} - \boldsymbol{i}) / \boldsymbol{i}. \tag{39}$$

The premium is positive if g is greater than i, and negative, or a discount, if g is less than i; for the first factor (1-K) can not be negative, as K by definition is the *present value* of a series of future payments whose sum is 1, and hence their present discounted value must be less than 1. This shows in all cases that a bond issue must be bought at a *premium*, if it is valued at a *lower* rate i than the rate of dividend g; and at a discount, if it is valued at a higher rate i than the rate of dividend g.

Serial bonds.—To apply the general formula (39) to the case of a bond issue redeemed by n equal annual installments, consider a unit of the total sum to be redeemed. Since this unit is to be redeemed in n equal installments over n years, the annual portion redeemed is 1/n.

The present value, K, of these n installments is clearly the value of an annuity of annual rent 1/n; hence

$$K = a_{\overline{n}} \times 1/n = a_{\overline{n}}/n$$
.

Substituting this value of K in formula (39), the following formula is obtained:

$$k = (1 - a_{\overline{n}}/n) (g - i)/i. \tag{40}$$

Example 19.—What is the bid on \$100,000 highway 4% serial bonds maturing in 20 equal annual installments, to net the purchaser an effective rate of 3%?

Here
$$n$$
=20, g =.04, i =.03, and $a\frac{3\%}{20|}$ =14.8774749; consequently k =(1-14.8774749/20)(.04-.03)/.03 =(1-.743873745) \times 1/3=.256126255 \times 1/3=.085375418.

Hence the bid on \$100,000 is

 $1.085375418 \times \$100,000 = \$108,537.54.$

Extension of formulas to case when dividends are payable and interest is convertible m times per annum.—Formula (36) assumes that dividends are payable once a year and that the effective rate of interest is i per annum. Replacing year by interval and assuming dividends to be paid at the end of each interval and the rate of interest realized by the investor a nominal rate convertible m times a year, formula (36) still applies, if the present value K of the several

installments to be redeemed is calculated at the effective rate j/m per interval, and the dividend per unit of the sum to be redeemed is taken at the rate g/m per interval. The formula is unchanged in form since m cancels out in the ratio g/m to j/m.

General formula for valuation of bonds.—Assume that:

- 1. The bonds are redeemed in r equal installments.
- 2. The first redemption of bonds is made at the end of f years.
- 3. The remaining r-1 bond redemptions are made at intervals of t years.
 - 4. The annual rate of dividend is g paid in m equal installments.
 - 5. The bond issue is valued at the nominal rate $j_{(m)}$.

First find the present value, A, of an issue of the above type where C=1. The value of a similar total issue of C is then found by multiplying A by C. Since the unit fund is redeemed in r equal installments, each one will be 1/r.

Redemption payments
$$1/r$$
 $1/r$ $1/$

The total term of the issue is seen to be f+(r-1)t years. As in preceding extension of formulas when dividends are payable and interest is convertible m times per annum, apply formula (36) to each installment of 1/r in the unit issue and the formula for the value of k, the premium per unit of the total sum to be redeemed, may readily be obtained. Expressed in terms of annuities, it appears as follows:

$$k = \left[1 - \frac{a_{\overline{m(f+tr)}} - a_{\overline{mf}}}{ra_{\overline{mt}}}\right] (g - j)/j \quad \text{at rate } j/m. \quad (41)$$

The annuity present values in this formula must be computed at the rate of interest j/m. The most common case in practice is where the dividends are paid semiannually. Here m=2, and formula (41) becomes:

$$\mathbf{k} = \left[1 - \frac{a_{\overline{2(j+tr)}} - a_{\overline{2j}}}{ra_{\overline{2t}}}\right] (g-j)/j \quad \text{at rate } \mathbf{j}/2.$$
 (42)

The last two formulas are very general in their application and have the advantage that when employed in practical computations it is necessary to consult only a table of values of $a_{\overline{n}}$.

Example 20.—To find the bid on \$1,100,000 highway bonds, interest 5% payable semiannually, dated January 1, 1914, maturing \$100,000 on January 1, 1922, 1924, 1926, 1928, 1930, 1932, 1934, 1936, 1938, 1940, and 1942, to net the purchaser a nominal rate of 4%, compounded semiannually, on his investment.

Here f=8, t=2, r=11, g=.05, m=2, and $j_{(2)}=.04$. Accordingly, m(f+tr)=60, mf=16, and mt=4. Substituting in formula (42),

$$k = \left[1 - \frac{a_{\overline{60}} - a_{\overline{16}}}{11 \times a_{\overline{4}}}\right] (.05 - .04) / .04 \quad \text{at } 2\%.$$

Entering Table 35 with 2% for the values of the annuities and numbering the successive steps for convenience of explanation, the calculation may be outlined as follows:

The bid on one dollar is 1+k=1.1235635; consequently the bid on the whole issue is

 $1.1235635 \times \$1,100,000 = \$1,235,919.85.$

Example 21.—To find the price of \$100,000 highway bonds, interest 5%, semi-annual, dated January 1, 1914, maturing \$50,000 January 1, 1917, and \$50,000 January 1, 1919, to net the investor 4% compounded semiannually.

In this case f=3, r=2, t=2, t=2, t=2, t=2, t=3, t=3, t=3, t=3, and, substituting as in the preceding example, the required price is found to be \$103,646.00. The progress of the loan is indicated in the following schedule.

Schedule	V.
SCHEDULE	ν.

Year.	Book value or principal at beginning of half-year.	Se miannual interest of 2%.	Semiannual dividend of $2\frac{1}{2}\%$ on bonds.	Amortization of premium at end of half-year.	Redemption payment at end of half-year.
$ \begin{array}{c} \frac{1}{2} \\ 1 \\ 1\frac{1}{2} \\ 2 \\ 2\frac{1}{2} \\ 3 \\ 3\frac{1}{2} \\ 4 \end{array} $	\$103, 646. 00 103, 218. 92 102, 783. 30 102, 338. 97 101, 885. 75 101, 423. 47 50, 951. 94 50, 720. 98	\$2, 072. 92 2, 064. 38 2, 055. 67 2, 046. 78 2, 037. 72 2, 028. 47 1, 019. 04 1, 014. 42	\$2,500.00 2,500.00 2,500.00 2,500.00 2,500.00 2,500.00 2,500.00 1,250.00	\$427. 08 435. 62 444. 33 453. 22 462. 28 471. 53 230. 96 235. 58	0. 00 0. 00 0. 00 0. 00 0. 00 0. 00 \$50, 000. 00 0. 00 0. 00
$\frac{4\frac{1}{2}}{5}$ Totals	50, 485. 40 50, 245. 11 817, 699. 84	1, 009. 71 1, 004. 89 16, 354. 00	1, 250. 00 1, 250. 00 20, 000. 00	240. 29 245. 11 3, 646. 00	0. 00 50, 000. 00 100, 000. 00

Extension of term of tables.—It sometimes happens in applying formula (42) that the value of 2(f+tr) is greater then the term given in the tables. In example 20 one of the required annuity values was $a_{\overline{00}}$ but, if the interval between redemptions had been three years instead of two, 2(f+tr)=82 would have called for the value of an annuity $a_{\overline{80}}$ beyond the limits of the tables. It is easy, however, to extend these limits by making use of the following obvious relations:

$$v^{m+n} = v^m v^n, \tag{43}$$

$$(1+i)^{m+n} = (1+i)^m (1+i)^n, (44)$$

$$a_{m+n} = [1 - v^m v^n]/i, (45)$$

$$a_{\overline{m+n}|} = a_{\overline{m}|} + v^m a_{\overline{n}|}, \tag{46}$$

$$s_{\overline{m+n}} = [(1+i)^m (1+i)^n - 1]/i, \tag{47}$$

$$s_{\overline{m+n}} = (1+i)^n s_{\overline{m}} + s_{\overline{n}}. \tag{48}$$

Example 22.—To find $\mathfrak{s}_{\overline{94}}$ at $1\frac{1}{2}\%$ when the limit of the tables is 60 years or terms. Applying formula (47) there results

$$s_{\overline{94}} \! = \! s_{\overline{60+34}} \! \! = \! \underbrace{(1.015)^{60+\beta4} \! - 1}_{.015} = \! \underbrace{(1.015)^{60} \! \times (1.015)^{34} \! - 1}_{.015}$$

$$= \frac{2.4432198 \times 1.6589964 - 1}{.015} = 203.5528568.$$

By formula (48)

$$s_{\overline{94}} = s_{\overline{60+34}} = (1.015)^{34} \cdot s_{\overline{60}} + s_{\overline{34}}$$

 $=1.6589964 \times 96.2146517 + 43.9330915 = 203.5528523.$

The correct value of $s_{\widetilde{94}}$, at $1\frac{1}{2}\%$ to seven places of decimals is 203.5528497; so the above method may be regarded as giving the correct value to about five places of decimals. In most practical cases this will be sufficiently accurate.

Valuation of serial bonds bearing semiannual dividends.— The most common type of serial bond bears semiannual dividends and is redeemed in equal annual installments, the first of which is paid at the end of the first year. Formula (42) lends itself directly to the valuation of this bond at a nominal rate of interest j convertible twice a year. In this case f=t=1, r=n, and

$$k = \left[1 - \frac{a_{\overline{2n+2}} - a_{\overline{2}}}{na_{\overline{2}}}\right] (g-j)/j \quad \text{at rate } j/2.$$
 (49)

Formula (49) requires the use of a table of values of $a_{\overline{n}|}$ only. It can be put in another convenient form for computation involving the use of a table of values of $a_{\overline{n}|}$ and $s_{\overline{n}|}$. For, by formula (46), $a_{\overline{2}+2\overline{n}|} = a_{\overline{2}|} + v^2 a_{\overline{2}\overline{n}|}$, and, since $v^2/a_{\overline{2}|} = 1/(1+i)^2 a_{\overline{2}|} = 1/s_{\overline{2}|}$, after a simple reduction, there results

$$\mathbf{k} = \left[1 - \frac{a_{\overline{2n}}}{n s_{\overline{2}}}\right] (\mathbf{g} - \mathbf{j})/\mathbf{j}$$
 at rate $\mathbf{j}/2$. (50)

Example 23.—\$300,000 highway serial bonds bearing 4% interest payable semi-annually, dated January 1, 1914, mature \$100,000 January 1, 1915, 1916, and 1917. What price should be paid to realize a net income of 3% compounded semiannually? Here n=3, q=.04, $j_{(2)}=.03$, and by formula (49)

$$k = \left[1 - \frac{a_{\overline{8}} - a_{\overline{2}}}{3a_{\overline{2}}}\right] (.04 - .03) / .03$$
 at $1\frac{1}{2}\%$
= .0575373×1/3=.0191791,

therefore the price to earn 3% compounded semiannually is

$$1.0191791 \times \$300,000 = \$305,753.73.$$

The following schedule illustrates the progress of this loan.

Schedule VI.

Year.	Book value or principal at beginning of half-year.	Semiannual interest of $1\frac{1}{2}\%$.	Semiannual dividend of 2% on bonds.	Amortization of premium at end of half-year.	Redemption payment at end of half-year.
$ \begin{array}{c} \frac{1}{2} \\ 1 \\ 1 \\ 1 \\ 2 \\ 2 \\ 2 \\ 1 \\ 3 \end{array} $	\$305, 753, 73 304, 340, 04 202, 905, 14 201, 948, 72 100, 977, 95 100, 492, 62	\$4, 586, 31 4, 565, 10 3, 043, 58 3, 029, 23 1, 514, 67 1, 507, 38	\$6,000.00 6,000.00 4,000.00 4,000.00 2,000.00 2,000.00	\$1, 413. 69 1, 434. 90 956. 42 970. 77 485. 33 492. 62	0.00 \$100,000.00 0.00 100,000.00 0.00 100,000.00
Totals	1, 216, 418. 20	18, 246. 27	24, 000. 00	5, 753. 73	300, 000. 00

Annuity bonds.—On pages 101 to 104 the operation of a loan where both principal and interest are discharged by equal installments is fully described. It is evident that bonds may be issued on this basis and retired in accordance with the principal repayments contained in the annuity installments. Since these principal repayments are not exact multiples of the amounts or denominations in which bonds are usually issued, it is necessary to adjust the exact schedule so as to meet this requirement. The adjusted schedule gives an issue in which the bonds are retired year by year in increasing amounts. Examples of exact and adjusted schedules appear in the body of this bulletin on pages 16 and 17.

To finance a loan of \hat{L} by an issue of annuity bonds bearing interest or dividends at rate g per annum.—The annual installment which will retire the bonds in n years and at the same time pay interest at the rate of g per cent on outstanding bonds is

$$L/a_{\overline{n}}$$
 at rate g . (51)

If the bonds are to bear interest of g per cent per ainum, payable in p installments of g/p per cent during the year, then

$$L/a_{\overline{np}}$$
 at rate g/p (52)

is the periodical payment or annuity installment which will take care of interest on the bonds and retire them in n years.

Example 24.—Adjust Schedule I, page 102, to finance the same loan by an annuity bond issue of \$100,000, denomination \$100, bearing 5% interest, compounded semi-annually, and retired in three years by six equal (nearly) semiannual annuity installments.

Referring to Schedule I on page 102, the adjustments in the last column to even multiples of \$100 are easily made; a check on this work is that the adjusted column must foot up to \$100,000. When the column of bond redemptions is decided upon, the other columns in the schedule are readily derived.

Year.	Book value or principal at beginning of half-year. Semiannual interest of $2\frac{1}{2}\%$.		Annuity installments at end of half-year.	Amortization of premium at end of half-year.	Amount of bonds retired at end of half-year.
$\begin{array}{c} \frac{1}{2} \\ 1 \\ \frac{1}{2} \\ 2 \\ \frac{2}{2} \\ 3 \\ \end{array}$ Totals	\$100,000 84,300 68,300 51,900 35,000 17,700 357,200	\$2, 500. 00 2, 107. 50 1, 707. 50 1, 297. 50 875. 00 442. 50 8, 930. 00	\$18, 200. 00 18, 107. 50 18, 107. 50 18, 197. 50 18, 175. 00 18, 142. 50 108, 930. 00	0. 00 0. 00 0. 00 0. 00 0. 00 0. 00 0. 00	\$15, 700 16, 000 16, 400 16, 900 17, 300 17, 700

Valuation of annuity bonds.—In order to value an issue of this character, so as to yield the purchaser a net income at a rate of interest different from the rate of dividend on the bonds, it will ordinarily be necessary to value separately the several parts of the total issue in accordance with the respective dates on which they are retired. This calculation may frequently be shortened by employing formula (36). Bond tables may also be consulted to advantage. The following example and schedule respectively illustrate the calculation of the bid and progress of the loan.

Example 25.—Determine the bid on the entire issue of annuity bonds in Example 24 so as to yield the investor a net income of 4%, compounded semiannually.

Applying formula (35) successively to the several bond issues in the order in which they are retired with g=.05 and j=.04, the following premiums are found:

\$76. 96 155. 32 236. 48 321. 75 407. 71 495. 73 \$1, 693. 95

Accordingly, the bid on the entire issue is \$101,693.95. The schedule illustrating the progress of this bond issue follows. It is constructed in the same manner as preceding bond schedules and needs no additional explanation.

Schedule VIII.—Showing the progress of an annuity bond issue of \$100,000, denomination \$100, bearing 5 per cent interest, compounded semiannually, and retired in three years by six equal (nearly) semiannual annuity installments. Bought to yield the investor 4 per cent, compounded semiannually.

Year.	Book value or principal at beginning of half-year.	Semiannual interest of 2%.	Annuity installments at end of half-year.	Amortization of premium at end of half-year.	Amount of bonds retired at end of half-year.
$egin{array}{c} rac{1}{2} \\ 1 \\ 1rac{1}{2} \\ 2 \\ 2rac{1}{2} \\ 3 \\ \end{array}$	\$101, 693. 95 85, 527. 83 69, 130. 89 52, 406. 01 35, 256. 63 17, 786. 76	\$2, 033. 88 1, 710. 56 1, 382. 62 1, 048. 12 705. 13 355. 74 7, 236. 05	\$18, 200. 00 18, 107. 50 18, 107. 50 18, 197. 50 18, 175. 00 18, 142. 50 108, 930. 00	\$466. 12 396. 94 324. 88 249. 38 169. 87 86. 76	\$15, 700 16, 000 16, 400 16, 900 17, 300 17, 700

Table 31.—The accumulation of 1 at the end of n years.

$$r^n = (1+i)^n.$$

Years.	1 ½%.	134%.	2%.	21/4%.	2½%.	2¾%.	3%.	Years
1	1, 0150000	1. 0175000	1, 0200000	1. 0225000	1. 0250000	1. 0275000	1, 0300000	1
2	1, 0302250	1. 0353063	1, 0404000	1. 0455063	1. 0506250	1. 0557563	1, 0609000	2
3	1, 0456784	1. 0534241	1, 0612080	1. 0690301	1. 0768906	1. 0847896	1, 0927270	3
4	1, 0613636	1. 0718590	1, 0824322	1. 0930833	1. 1038129	1. 1146213	1, 1255088	4
5	1, 0772840	1. 0906166	1, 1040808	1. 1176777	1. 1314082	1. 1452733	1, 1592741	5
6 7 8 9 10	1, 0934433 1, 1098449 1, 1264926 1, 1433900 1, 1605408	1, 1097024 1, 1291222 1, 1488818 1, 1689872 1, 1894445	1. 1261624 1. 1486857 1. 1716594 1. 1950926 1. 2189944	1. 1428254 1. 1685390 1. 1948311 1. 2217148 1. 2492034	1, 1596934 1, 1886858 1, 2184029 1, 2488630 1, 2800845	1. 1767684 1. 2091295 1. 2423806 1. 2765460 1. 3116510	1, 1940523 1, 2298739 1, 2667701 1, 3047732 1, 3439164	6 7 8 9
11	1, 1779489	1, 2102598	1, 2433743	1, 2773105	1. 3120867	1, 3477214	1, 3842339	11
12	1, 1956182	1, 2314393	1, 2682418	1, 3060500	1. 3448888	1, 3847838	1, 4257609	12
13	1, 2135524	1, 2529895	1, 2936066	1, 3354361	1. 3785110	1, 4228653	1, 4685337	13
14	1, 2317557	1, 2749168	1, 3194788	1, 3654834	1. 4129738	1, 4619941	1, 5125897	14
15	1, 2502321	1, 2972279	1, 3458683	1, 3962068	1. 4482982	1, 5021990	1, 5579674	15
16	1. 2689856	1,3199294	1. 3727857	1. 4276215	1. 4845056	1, 5435094	1, 6047064	16
17	1. 2880203	1,3430281	1. 4002414	1. 4597429	1. 5216183	1, 5859560	1, 6528476	17
18	1. 3073406	1,3665311	1. 4282463	1. 4925872	1. 5596587	1, 6295697	1, 7024331	18
19	1. 3269508	1,3904454	1. 4568112	1. 5261704	1. 5986502	1, 6743829	1, 7535061	19
20	1. 3468550	1,4147782	1. 4859474	1. 5605092	1. 6386164	1, 7204284	1, 8061112	20
21	1, 3670578	1.4395368	1, 5156663	1. 5956207	1. 6795819	1.7677402	1.8602946	21
22	1, 3875637	1.4647287	1, 5459797	1. 6315221	1. 7215714	1.8163531	1.9161034	22
23	1, 4083772	1.4903615	1, 5768993	1. 6682314	1. 7646107	1.8663028	1.9735865	23
24	1, 4295028	1.5164428	1, 6084373	1. 7057666	1. 8087260	1.9176261	2.0327941	24
25	1, 4509454	1.5429805	1, 6406060	1. 7441463	1. 8539441	1.9703608	2.0937779	25
26	1, 4727095	1, 5699827	1. 6734181	1.7833896	1. 9002927	2. 0245458	2. 1565913	26
27	1, 4948002	1, 5974574	1. 7068865	1.8235159	1. 9478000	2. 0802208	2. 2212890	27
28	1, 5172222	1, 6254129	1. 7410242	1.8645450	1. 9964950	2. 1374268	2. 2879277	28
29	1, 5399805	1, 6538576	1. 7758447	1.9064973	2. 0464074	2. 1962061	2. 3565655	29
30	1, 5630802	1, 6828001	1. 8113616	1.9493934	2. 0975676	2. 2566017	2. 4272625	30
31	1, 5865264	1.7122491	1,8475888	1, 9932548	2. 1500068	2, 3186583	2,5000804	31
32	1, 6103243	1.7422135	1,8845406	2, 0381030	2. 2037569	2, 3824214	2,5750828	32
33	1, 6344792	1.7727022	1,9222314	2, 0839603	2. 2588509	2, 4479380	2,6523352	33
34	1, 6589964	1.8037245	1,9606760	2, 1308495	2. 3153221	2, 5152563	2,7319053	34
35	1, 6838813	1.8352897	1,9998896	2, 1787936	2. 3732052	2, 5844258	2,8138625	35
36	1.7091395	1.8674073	2. 0398873	2. 2278164	2. 4325353	2. 6554975	2.8982783	36
37	1.7347766	1.9000869	2. 0806851	2. 2779423	2. 4933487	2. 7285237	2.9852267	37
38	1.7607983	1.9333384	2. 1222988	2. 3291960	2. 5556824	2. 8035581	3.0747835	38
39	1.7872103	1.9671718	2. 1647448	2. 3816029	2. 6195745	2. 8806560	3.1670270	39
40	1.8140184	2.0015973	2. 2080397	2. 4351890	2. 6850638	2. 9598740	3.2620378	40
41	1. 8412287	2. 0366253	2, 2522005	2. 4899807	2. 7521904	3. 0412705	3. 3598989	41
42	1. 8688471	2. 0722662	2, 2972445	2. 5460053	2. 8209952	3. 1249055	3. 4606959	42
43	1. 8968798	2. 1085309	2, 3431894	2. 6032904	2. 8915201	3. 2108404	3. 5645168	43
44	1. 9253330	2. 1454302	2, 3900531	2. 6618644	2. 9638081	3. 2991385	3. 6714523	44
45	1. 9542130	2. 1829752	2, 4378542	2. 7217564	3. 0379033	3. 3898648	3. 7815958	45
46	1, 9835262	2. 2211773	2. 4866113	2.7829959	3. 1138509	3. 4830861	3, 8950437	46
47	2, 0132791	2. 2600479	2. 5363435	2.8456133	3. 1916971	3. 5788709	4, 0118950	47
48	2, 0434783	2. 2995987	2. 5870704	2.9096396	3. 2714896	3. 6772899	4, 1322519	48
49	2, 0741305	2. 3398417	2. 6388118	2.9751065	3. 3532768	3. 7784154	4, 2562194	49
50	2, 1052424	2. 3807889	2. 6915880	3.0420464	3. 4371087	3. 8823218	4, 3839060	50
51	2. 1368211	2. 4224527	2.7454198	3. 1104924	3. 5230364	3. 9890856	4. 5154232	51
52	2. 1688734	2. 4648457	2.8003282	3. 1804785	3. 6111124	4. 0987855	4. 6508859	52
53	2. 2014065	2. 5079805	2.8563348	3. 2520393	3. 7013902	4. 2115021	4. 7904125	53
54	2. 2344276	2. 5518701	2.9134614	3. 3252102	3. 7939249	4. 3273184	4. 9341249	54
55	2. 2679440	2. 5965279	2.9717307	3. 4000274	3. 8887730	4. 4463196	5. 0821486	54
56	2.3019631	2, 6419671	3, 0311653	3. 4765280	3. 9859924	4. 5685934	5. 2346131	56
57	2.3364926	2, 6882015	3, 0917886	3. 5547499	4. 0856422	4. 6942298	5. 3916514	57
58	2.3715400	2, 7352450	3, 1566244	3. 6347318	4. 1877832	4. 8233211	5. 5534010	58
59	2.4071131	2, 7831118	3, 2166969	3. 7165132	4. 2924778	4. 9559624	5. 7200030	59
60	2.4432198	2, 8318163	3, 2810308	3. 8001348	4. 3997897	5. 0922514	5. 8916031	60

Table 31.—The accumulation of 1 at the end of n years—Continued.

$$r^n = (1+i)^n$$
.

Tears.	312%.	4%.	415%.	5%.	5 ½%.	6%.	7%.	Years
1 2 3 4 5	1, 0350000	1. 0400000	1. 0450000	1. 0500000	1. 0550000	1, 0600000	1. 0700000	1
	1, 0712250	1. 0816000	1. 0920250	1. 1025000	1. 1130250	1, 1236000	1. 1449000	2
	1, 1087179	1. 1248640	1. 1411661	1. 1576250	1. 1742414	1, 1910160	1. 2250430	3
	1, 1475230	1. 1698586	1. 1925186	1. 2155063	1. 2388247	1, 2624770	1. 3107960	4
	1, 1876863	1. 2166529	1. 2461819	1. 2762816	1. 3069600	1, 3382256	1. 4025517	5
6	1. 2292553	1. 2653190	1. 3022601	1. 3400956	1. 3788428	1. 4185191	1,5007304	6
7	1. 2722793	1. 3159318	1. 3608618	1. 4071004	1. 4546792	1. 5036303	1,6057815	7
8	1. 3168090	1. 3685691	1. 4221006	1. 4774554	1. 5346865	1. 5938481	1,7181862	8
9	1. 3628974	1. 4233118	1. 4860951	1. 5513282	1. 6190943	1. 6894790	1,8384592	9
10	1. 4105988	1. 4802443	1. 5529694	1. 6288946	1. 7081445	1. 7908477	1,9671514	10
11	1. 4599697	1. 5394541	1. 6228531	1.7103394	1. 8020924	1. 8982986	2. 1048520	11
12	1. 5110687	1. 6010322	1. 6958814	1.7958563	1. 9012075	2. 0121965	2. 2521916	12
13	1. 5639561	1. 6650735	1. 7721961	1.8856491	2. 0057739	2. 1329283	2. 4098450	13
14	1. 6186945	1. 7316765	1. 8519449	1.9799316	2. 1160915	2. 2609040	2. 5785342	14
15	1. 6753488	1. 8009435	1. 9352824	2.0789282	2. 2324765	2. 3965582	2. 7590315	15
16	1.7339860	1. 8729813	2. 0223702	2. 1828746	2. 3552627	2. 5403517	2. 9521638	16
17	1.7946756	1. 9473005	2. 1133768	2. 2920183	2. 4848022	2. 6927728	3. 1588152	17
18	1.8574892	2. 0258165	2. 2084788	2. 4066192	2. 6214663	2. 8543392	3. 3799323	18
19	1.9225013	2. 1068492	2. 3078603	2. 5269502	2. 7656469	3. 0255995	3. 6165275	19
20	1.9897889	2. 1911231	2. 4117140	2. 6532977	2. 9177575	3. 2071355	3. 8696845	20
21	2. 0594315	2, 2787681	2. 5202412	2. 7859626	3. 0782342	3. 3995636	4. 1405624	21
22	2. 1315116	2, 3699188	2. 6336520	2. 9252607	3. 2475370	3. 6035374	4. 4304017	22
23	2. 2061145	2, 4647155	2. 7521664	3. 0715238	3. 4261516	3. 8197497	4. 7405299	23
24	2. 2833285	2, 5633042	2. 8760138	3. 2250999	3. 6145899	4. 0489346	5. 0723670	24
25	2. 3632450	2, 6658363	3. 0054345	3. 3863549	3. 8133924	4. 2918707	5. 4274326	25
26	2. 4459586	2. 7724698	3. 1406790	3. 5556727	4. 0231289	4. 5493830	5, 8073529	26
27	2. 5315671	2. 8835686	3. 2820096	3. 7334563	4. 2444010	4. 8223459	6, 2138676	27
28	2. 6201720	2. 9987033	3. 4297000	3. 9201291	4. 4778431	5. 1116867	6, 6488384	28
29	2. 7118780	3. 1186515	3. 5840365	4. 1161356	4. 7241244	5. 4183879	7, 1142571	29
30	2. 8067937	3. 2433975	3. 7453181	4. 3219424	4. 9839513	5. 7434912	7, 6122550	30
31 32 33 34 35	2. 9050315 3. 0067076 3. 1119424 3. 2208603 3. 3335905	3. 3731334 3. 5080588 3. 6483811 3. 7943163 3. 9460890	3. 9138575 4. 0899810 4. 2740302 4. 4663615 4. 6673478	4, 5380395 4, 7649415 5, 0031885 5, 2533480 5, 5160154	5. 2580686 5. 5472624 5. 8523618 6. 1742417 6. 5138250	6. 0881006 6. 4533867 6. 8405899 7. 2510253 7. 6860868	8. 1451129 8. 7152708 9. 3253398 9. 9781135 10. 6765815	31 32 33 34 34 35
36	3. 4502661	4. 1039326	4. 8773785	5. 7918161	6. 8720854	8. 1472520	11. 4239422	36
37	3. 5710254	4. 2680899	5. 0968605	6. 0814069	7. 2500501	8. 6360871	12. 2236181	37
38	3. 6960113	4. 4388135	5. 3262192	6. 3854773	7. 6488028	9. 1542524	13. 0792714	38
39	3. 8253717	4. 6163660	5. 5658991	6. 7047512	8. 0694870	9. 7035075	13. 9948204	39
40	3. 9592597	4. 8010206	5. 8163645	7. 0399887	8. 5133088	10. 2857179	14. 9744578	40
41	4. 0978338	4. 9930615	6. 0781009	7. 3919882	8. 9815408	10. 9028610	16. 0226699	41
42	4. 2412580	5. 1927839	6. 3516155	7. 7615876	9. 4755255	11. 5570327	17. 1442568	42
43	4. 3897020	5. 4004953	6. 6374382	8. 1496669	9. 9966794	12. 2504546	18. 3443548	43
44	4. 5433416	5. 6165151	6. 9361229	8. 5571503	10. 5464968	12. 9854819	19. 6284596	44
45	4. 7023586	5. 8411757	7. 2482484	8. 9850078	11. 1265541	13. 7646108	21. 0024518	45
46	4. 8669411	6. 0748227	7. 5744196	9. 4342582	11. 7385146	14. 5904875	22, 4726234	46
47	5. 0372840	6. 3178156	7. 9152685	9. 9059711	12. 3841329	15. 4659167	24, 0457070	47
48	5. 2135890	6. 5705282	8. 2714556	10. 4012697	13. 0652602	16. 3938717	25, 7289065	48
49	5. 3960646	6. 8333494	8. 6436711	10. 9213331	13. 7838495	17. 3775040	27, 5299300	49
50	5. 5849269	7. 1066834	9. 0326363	11. 4673998	14. 5419612	18. 4201543	29, 4570251	50
51	5. 7803993	7. 3909507	9. 4391049	12. 0407698	15. 3417691	19. 5253635	31, 5190168	51
52	5. 9827133	7. 6865887	9. 8638646	12. 6428083	16. 1855664	20. 6968853	33, 7253480	52
53	6. 1921082	7. 9940523	10. 3077385	13. 2749487	17. 0757725	21. 9386985	36, 0861224	53
54	6. 4088320	8. 3138144	10. 7715868	13. 9386961	18. 0149400	23. 2550204	38, 6121509	54
55	6. 6331411	8. 6463669	11. 2563082	14. 6356309	19. 0057617	24. 6503216	41, 3150015	55
56	6. 8653011	8. 9922216	11. 7628420	15. 3674125	20, 0510786	26. 1293409	44. 2070516	56
57	7. 1055866	9. 3519105	12. 2921699	16. 1357831	21, 1538879	27. 6971013	47. 3015452	57
58	7. 3542822	9. 7259869	12. 8453176	16. 9425722	22, 3173518	29. 3589274	50. 6126534	58
59	7. 6116820	10. 1150264	13. 4233569	17. 7897009	23, 5448061	31. 1204631	54. 1555391	59
60	7. 8780909	10. 5196274	14. 0274079	18. 6971859	24, 8397705	32. 9876909	57. 9464268	60

Table 32.—The accumulation of an annuity of 1 per annum at the end of n years.

$$s_{n} = \frac{(1+i)^n - 1}{i}.$$

Years.	1½%.	134%.	2%.	21/4%.	2½%.	23/4%.	3%.	Years.
1	1. 0000600	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1
2	2. 0150000	2.0175000	2.0200000	2.0225000	2.0250000	2.0275000	2.0300000	2
3	3. 0452250	3.0528063	3.0604000	3.0680063	3.0756250	3.0832563	3.0909000	3
4	4. 0909034	4.1062304	4.1216080	4.1370364	4.1525156	4.1680458	4.1836270	4
5	5. 1522669	5.1780894	5.2040402	5.2301197	5.2563285	5.2826671	5.3091358	5
6 7 8 9 10	6. 2295509 7. 3229942 8. 4328391 9. 5593317 10. 7027217	6. 2687060 7. 3784083 8. 5075305 9. 6564122 10. 8253995	6.3081210 7.4342834 8.5829691 9.7546284 10.9497210	6.3477974 7.4906228 8.6591619 9.8539930 11.0757078	6.3877367 7.5474302 8.7361159 9.9545188 11.2033818	6. 4279404 7. 6047088 8. 8138383 10. 0562188 11. 3327648	6. 4684099 7. 6624622 8. 8923361 10. 1591061 11. 4638793	6 7 8 9
11	11. 8632625	12. 0148439	12. 1687154	12. 3249113	12. 4834663	12. 6444159	12.8077957	11
12	13. 0412114	13. 2251037	13. 4120897	13. 6022218	13. 7955530	13. 9921373	14.1920296	12
13	14. 2368296	14. 4565430	14. 6803315	14. 9082718	15. 1404418	15. 3769211	15.6177905	13
14	15. 4503821	15. 7095325	15. 9739382	16. 2437079	16. 5189528	16. 7997864	17.0863242	14
15	16. 6821378	16. 9844494	17. 2934169	17. 6091913	17. 9319267	18. 2617805	18.5989139	15
16	17. 9323698	18. 2816772	18. 6392853	19. 0053981	19. 3802248	19. 7639795	20. 1568813	16
17	19. 2013554	19. 6016066	20. 0120710	20. 4330196	20. 8647305	21. 3074889	21. 7615877	17
18	20. 4893757	20. 9446347	21. 4123124	21. 8927625	22. 3863487	22. 8934149	23. 4144354	18
19	21. 7967164	22. 3111658	22. 8405586	23. 3853497	23. 9460074	24. 5230146	25. 1168684	19
20	23. 1236671	23. 7016112	24. 2973698	24. 9115200	25. 5446576	26. 1973975	26. 8703745	20
21	24. 4705221	25. 1163894	25. 7833172	26. 4720292	27. 1832741	27. 9178259	28. 6764857	21
22	25. 8375799	26. 5559262	27. 2989835	28. 0676499	28. 8628559	29. 6855662	30. 5367803	22
23	27. 2251436	28. 0206549	28. 8449632	29. 6991720	30. 5844273	31. 5019192	32. 4528837	23
24	28. 6335208	29. 5110164	30. 4218625	31. 3674034	32. 3490380	33. 3682220	34. 4264702	24
25	30. 0630236	31. 0274592	32. 0302997	33. 0731700	34. 1577639	35. 2858481	36. 4592643	25
26	31. 5139690	32. 5704397	33. 6709057	34. 8173163	36. 0117080	37. 2562089	38. 5530423	26
27	32. 9866785	34. 1404224	35. 3443238	36. 6007059	37. 9120007	39. 2807547	40. 7096335	27
28	34. 4814787	35. 7378798	37. 0512103	38. 4242218	39. 8598008	41. 3609754	42. 9309225	28
29	35. 9987009	37. 3632927	38. 7922345	40. 2887668	41. 8562958	43. 4984022	45. 2188502	29
30	37. 5386814	39. 0171503	40. 5680792	42. 1952640	43. 9027032	45. 6946083	47. 5754157	30
31	39.1017616	40. 6999504	42. 3794408	44. 1446575	46. 0002707	47, 9512100	50. 0026782	31
32	40.6882880	42. 4121996	44. 2270296	46. 1379123	48. 1502775	50, 2698683	52. 5027585	32
33	42.2986123	44. 1544131	46. 1115702	48. 1760153	50. 3540345	52, 6522897	55. 0778413	33
31	43.9330915	45. 9271153	48. 0338016	50. 2599756	52. 6128853	55, 1002277	57. 7301765	34
35	45.5920879	47. 7308398	49. 9944776	52. 3908251	54. 9282074	57, 6154839	60. 4620818	35
36	47, 2759692	49. 5661295	51. 9943672	54,5696186	57, 3014126	60, 1999097	63. 2759443	36
37	48, 9851087	51. 4335368	54. 0342545	56,7974351	59, 7339479	62, 8554072	66. 1742226	37
38	50, 7198854	53. 3336236	56. 1149396	59,0753774	62, 2272966	65, 5839309	69. 1591493	38
39	52, 4806837	55. 2669621	58. 2372384	61,4045733	64, 7829791	68, 3874890	72. 2342328	39
40	54, 2678939	57. 2341339	60. 4019832	63,7861762	67, 4025535	71, 2681450	75. 4012597	40
41	56. 0819123	59. 2357312	62. 6100228	66. 2213652	70. 0876174	74. 2280190	78. 6632975	41
42	57. 9231410	61. 2723565	64. 8622233	68. 7113459	72. 8398078	77. 2692895	82. 0231965	42
43	59. 7919881	63. 3446228	67. 1594678	71. 2573512	75. 6608030	80. 3941950	85. 4838923	43
44	61. 6888679	65. 4531537	69. 5026571	73. 8606416	78. 5523231	83. 6050353	89. 0484091	44
45	63. 6142010	67. 5985839	71. 8927103	76. 5225061	81. 5161312	86. 9041738	92. 7198614	45
46	65. 5684140	69. 7815591	74. 3305645	79. 2442624	84.5540344	90. 2940386	96. 5014572	46
47	67. 5519402	72. 0027364	76. 8171758	82. 0272583	87.6678853	93. 7771246	100. 3965010	47
48	69. 5652193	74. 2627843	79. 3535193	84. 8728717	90.8595824	97. 3559956	104. 4083960	48
49	71. 6086976	76. 5623830	81. 9405897	87. 7825113	94.1310720	101. 0332854	108. 5406479	49
50	73. 6828280	78. 9022247	84. 5794015	90. 7576178	97.4843488	104. 8117008	112. 7968673	50
51	75. 7880705	81. 2830136	87. 2709895	93. 7996642	100. 9214575	108. 6940226	117. 1807733	51
52	77. 9248915	83. 7054664	90. 0164093	96. 9101566	104. 4444940	112. 6831082	121. 6961965	52
53	80. 0937649	86. 1703120	92. 8167375	100. 0906351	108. 0556063	116. 7818937	126. 3470824	53
54	82. 2951714	88. 6782925	95. 6730722	103. 3426744	111. 7569965	120. 9933957	131. 1374949	54
55	84. 5295989	91. 2301626	98. 5865337	106. 6678846	115. 5509214	125. 3207141	136. 0716197	55
56	86. 7975429	93. 8266904	101. 5582643	110. 0679120	119. 4396944	129, 7670338	141. 1537683	56
57	89. 0995061	96. 4686575	104. 5894296	113. 5444400	123. 4256868	134, 3356272	146. 3883814	57
58	91. 4359987	99. 1568590	107. 6812182	117. 0991899	127. 5113289	139, 0298569	151. 7800328	58
59	93. 8075386	101. 8921041	110. 8348426	120. 7339217	131. 6991122	143, 8531780	157. 3334338	59
60	96. 2146517	104. 6752159	114. 0515394	124. 4504349	135. 9915900	148, 8091404	163. 0534368	60

Table 32.—The accumulation of an annuity of 1 per annum at the end of n years—Con.

$$s_{\overline{n}} = \frac{(1+i)^n - 1}{i}$$

Yrs.	3½%.	4%.	4½%.	5%.	5½%.	6%.	7%.	Yrs.
1	1.0000000	1,0000000	1.0000000	1.0000000	1.0000000	1.0000000	1.0000000	1
2	2.0350000	2,0400000	2.0450000	2.0500000	2.0550000	2.0600000	2.0700000	2
3	3.1062250	3,1216000	3.1370250	3.1525000	3.1680250	3.1836000	3.2149000	3
4	4.2149429	4,2464640	4.2781911	4.3101250	4.3422664	4.3746160	4.4399430	4
5	5.3624659	5,4163226	5.4707097	5.5256313	5.5810910	5.6370930	5.7507390	5
6	6. 5501522	6.6329755	6.7168917	6.8019128	6. 8880510	6. 9753185	7.1532907	6
7	7. 7794075	7.8982945	8.0191518	8.1420085	8. 2668938	8. 3938377	8.6540211	7
8	9. 0516868	9.2142263	9.3800136	9.5491089	9. 7215730	9. 8974679	10.2598026	8
9	10. 3684958	10.5827953	10.8021142	11.0265643	11. 2562595	11. 4913160	11.9779888	9
10	11. 7313932	12.0061071	12.2882094	12.5778925	12. 8753538	13. 1807949	13.8164480	10
11	13.1419919	13. 4863514	13.8411788	14. 2067872	14.5834983	14. 9716426	15. 7835993	11
12	14.6019616	15. 0258055	15.4640318	15. 9171265	16.3855907	16. 8699412	17. 8884513	12
13	16.1130303	16. 6268377	17.1599133	17. 7129829	18.2867981	18. 8821377	20. 1406429	13
14	17.6769864	18. 2919112	18.9321094	19. 5986320	20.2925720	21. 0150659	22. 5504879	14
15	19.2956809	20. 0235876	20.7840543	21. 5785636	22.4086635	23. 2759699	25. 1290220	15
16	20. 9710297	21.8245311	22. 7193367	23.6574918	24.6411400	25. 6725281	27,8880536	16
17	22. 7050158	23.6975124	24. 7417069	25.8403664	26.9964027	28. 2128798	30,8402173	17
18	24. 4996913	25.6454129	26. 8550837	28.1323847	29.4812048	30. 9056526	33,9990325	18
19	26. 3571805	27.6712294	29. 0635625	30.5390039	32.1026711	33. 7599917	37,3789648	19
20	28. 2796818	29.7780786	31. 3714228	33.0659541	34.8683180	36. 7855912	40,9954923	20
21	30. 2694707	31. 9692017	33. 7831368	35.7192518	37.7860755	39. 9927267	44.8651768	21
22	32. 3289022	34. 2479698	36. 3033780	38.5052144	40.8643097	43. 3922903	49.0057392	22
23	34. 4604137	36. 6178886	38. 9370300	41.4304751	44.1118467	46. 9958277	53.4361409	23
24	36. 6665282	39. 0826041	41. 6891963	44.5019989	47.5379983	50. 8155774	58.1766708	24
25	38. 9498567	41. 6459083	44. 5652102	47.7270988	51.1525882	54. 8645120	63.2490377	25
26	41. 3131017	44, 3117446	47. 5706446	51.1134538	54. 9659805	59.1563827	68. 6764704	26
27	43. 7590602	47, 0842144	50. 7113236	54.6691265	58. 9891094	63.7057657	74. 4838233	27
28	46. 2906273	49, 9675830	53. 9933332	58.4025828	63. 2335105	68.5281116	80. 6976909	28
29	48. 9107993	52, 9662863	57. 4230332	62.3227119	67. 7113535	73.6397983	87. 3465293	29
30	51. 6226773	56, 0849378	61. 0070697	66.4388475	72. 4354780	79.0581862	94. 4607863	30
31	54. 4294710	59. 3283353	64, 7523878	70. 7607899	77. 4194293	84.8016774	102.0730414	31
32	57. 3345025	62. 7014687	68, 6662452	75. 2988294	82. 6774979	90.8897780	110.2181543	32
33	60. 3412101	66. 2095274	72, 7562263	80. 0637708	88. 2247603	97.3431647	118.9334251	33
34	63. 4531524	69. 8579085	77, 0302565	85. 0669594	94. 0771221	104.1837546	128.2587648	34
35	66. 6740127	73. 6522249	81, 4966180	90. 3203074	100. 2513638	111.4347799	138.2368784	35
36	70.0076032	77. 5983139	86.1639658	95.8363227	106. 7651888	119. 1208667	148. 9134598	36
37	73.4578693	81. 7022464	91.0413443	101.6281389	113. 6372742	127. 2681187	160. 3374020	37
38	77.0288947	85. 9703363	96.1382048	107.7095458	120. 8873243	135. 9042058	172. 5610202	38
39	80.7249060	90. 4091497	101.4644240	114.0950231	128. 5361271	145. 0584581	185. 6402916	39
40	84.5502778	95. 0255157	107.0303231	120.7997742	136. 6056141	154. 7619656	199. 6351120	40
41	88. 5095375	99. 8265363	112.8466876	127.8397630	145.1189229	165. 0476836	214.6095698	41
42	92. 6073713	104. 8195978	118.9247885	135.2317511	154.1004636	175. 9505446	230.6322397	42
43	96. 8486293	110. 0123817	125.2764040	142.9933387	163.5759891	187. 5075772	247.7764695	43
44	101. 2383313	115. 4128770	131.9138422	151.1430056	173.5726685	199. 7580319	266.1208513	44
45	105. 7816729	121. 0293920	138.8499651	159.7001559	184.1191653	212. 7435138	285.7493108	45
46	110. 4840315	126. 8705677	146. 0982135	168. 6851637	195.2457194	226.5081246	306, 7517626	46
47	115. 3509726	132. 9453904	153. 6726331	178. 1194219	206.9842339	241.0986121	329, 2243860	47
48	120. 3882566	139. 2632060	161. 5879016	188. 0253929	219.3683668	256.5645288	353, 2700930	48
49	125. 6018456	145. 8337343	169. 8593572	198. 4266626	232.4336270	272.9584006	378, 9989995	49
50	130. 9979102	152. 6670837	178. 5030283	209. 3479957	246.2174765	290.3359046	406, 5289295	50
51	136. 5828370	159. 7737670	187. 5356646	220. 8153955	260, 7594377	308. 7560589	435, 9859545	51
52	142. 3632363	167. 1647177	196. 9747695	232. 8561653	276, 1012067	328. 2814224	467, 5049714	52
53	148. 3459496	174. 8513064	206. 8386341	245. 4989735	292, 2867731	348. 9783077	501, 2303194	53
54	154. 5380578	182. 8453587	217. 1463726	258. 7739222	309, 3625456	370. 9170062	537, 3164417	54
55	160. 9468898	191. 1591730	227. 9179594	272. 7126183	327, 3774856	394. 1720266	575, 9285926	55
56	167. 5800310	199. 8055399	239.1742676	287. 3482492	346. 3832473	418. 8223482	617, 2435941	56
57	174. 4453321	208. 7977615	250.9371096	302. 7156617	366. 4343259	444. 9516891	661, 4506457	57
58	181. 5509187	218. 1496720	263.2292795	318. 8514448	387. 5882139	472. 6487904	708, 7521909	58
59	188. 9052009	227. 8756589	276.0745971	335. 7940170	409. 9055656	502. 0077178	759, 3648443	59
60	196. 5168829	237. 9906852	289.4979540	353. 5837179	433. 4503717	533. 1281809	813, 5203834	60

Table 33.—The annual sinking fund which will accumulate to 1 at the end of n years.

$$\frac{1}{s_{\overline{n}}} = \frac{i}{(1+i)^n - 1} \cdot$$

Years.	1 ½%.	134%.	2%.	21/4%.	2½%.	23/4%.	3%.	Years.
1	1,0000000	1. 0000000	1. 0000000	1. 0000000	1.0000000	1. 0000000	1. 0000000	1
2	0,4962779	0. 4956630	0. 4950495	0. 4944376	0.4938272	0. 4932183	0. 4926108	2
3	0,3283830	0. 3275675	0. 3267547	0. 3259446	0.3251372	0. 3243324	0. 3235304	3
4	0,2444448	0. 2435324	0. 2426238	0. 2417189	0.2408179	0. 2399206	0. 2390271	4
5	0,1940893	0. 1931214	0. 1921584	0. 1912002	0.1902469	0. 1892983	0. 1883546	5
6	0. 1605252	0. 1595226	0. 1585258	0.1575350	$\begin{array}{c} 0.1565500 \\ 0.1324954 \\ 0.1144674 \\ 0.1004569 \\ 0.0892588 \end{array}$	0. 1555708	0. 1545975	6
7	0. 1365562	0. 1355306	0. 1345120	0.1335003		0. 1314975	0. 1305064	7
8	0. 1185840	0. 1175429	0. 1165098	0.1154846		0. 1134580	0. 1124564	8
9	0. 1046098	0. 1035581	0. 1025154	0.1014817		0. 0994410	0. 0984339	9
10	0. 0934342	0. 0923753	0. 0913265	0.0902877		0. 0882397	0. 0872305	10
11	0. 0842938	0. 0832304	0. 0821779	0.0811365	0. 0801060	0. 0790863	0. 0780775	11
12	0. 0766800	0. 0756138	0. 0745596	0.0735174	0. 0724871	0. 0714687	0. 0704621	12
13	0. 0702404	0. 0691728	0. 0681184	0.0670769	0. 0660483	0. 0650325	0. 0640295	13
14	0. 0647233	0. 0636556	0. 0626020	0.0615623	0. 0605365	0. 0595246	0. 0585263	14
15	0. 0599444	0. 0588774	0. 0578255	0.0567885	0. 0557665	0. 0547592	0. 0537666	15
16	0. 0557651	0. 0546996	0. 0536501	0. 0526166	0. 0515990	0. 0505971	$\begin{array}{c} 0.0496109 \\ 0.0459525 \\ 0.0427087 \\ 0.0398139 \\ 0.0372157 \end{array}$	16
17	0. 0520797	0. 0510162	0. 0499698	0. 0489404	0. 0479278	0. 0469319		17
18	0. 0488058	0. 0477449	0. 0467021	0. 0456772	0. 0446701	0. 0436806		18
19	0. 0458785	0. 0448206	0. 0437818	0. 0427618	0. 0417606	0. 0407780		19
20	0. 0432457	0. 0421912	0. 0411567	0. 0401421	0. 0391471	0. 0381717		20
21	0. 0408655	0.0398146	0. 0387848	0, 0377757	0. 0367873	0. 0358194	$\begin{array}{c} 0.0348718 \\ 0.0327474 \\ 0.0308139 \\ 0.0290474 \\ 0.0274279 \end{array}$	21
22	0. 0387033	0.0376564	0. 0366314	0, 0356282	0. 0346466	0. 0336864		22
23	0. 0367308	0.0356878	0. 0346681	0, 0336710	0. 0326964	0. 0317441		23
24	0. 0349241	0.0338857	0. 0328711	0, 0318802	0. 0309128	0. 0299686		24
25	0. 0332635	0.0322295	0. 0312204	0, 0302360	0. 0292759	0. 0283400		25
26	0.0317320	0.0307027	0. 0296992	0.0287213	0. 0277687	0. 0268412	$\begin{array}{c} 0.0259383 \\ 0.0245642 \\ 0.0232932 \\ 0.0221147 \\ 0.0210193 \end{array}$	26
27	0.0303153	0.0292908	0. 0282931	0.0273219	0. 0263769	0. 0254578		27
28	0.0290011	0.0279815	0. 0269897	0.0260253	0. 0255879	0. 0241774		28
29	0.0277788	0.0267642	0. 0257784	0.0248208	0. 0238913	0. 0229894		29
30	0.0266392	0.0256298	0. 0246499	0.0236993	0. 0227776	0. 0218844		30
31	0. 0255743	0.0245701	0.0235964	0.0226528	0.0217390	0, 0208545	0.0199989	31
32	0. 0245771	0.0235781	0.0226106	0.0216742	0.0207683	0, 0198926	0.0190466	32
33	0. 0236414	0.0226478	0.0216865	0.0207572	0.0198594	0, 0189925	0.0181561	33
34	0. 0227619	0.0217736	0.0208187	0.0198966	0.0190068	0, 0181488	0.0173220	34
35	0. 0219336	0.0209508	0.0200022	0.0190873	0.0182056	0, 0173565	0.0165393	35
36	0. 0211524	0. 0201751	0. 0192329	0. 0183252	$\begin{array}{c} 0.0174516 \\ 0.0167409 \\ 0.0160701 \\ 0.0154362 \\ 0.0148362 \end{array}$	0. 0166113	0. 0158038	36
37	0. 0204144	0. 0194426	0. 0185068	0. 0176064		0. 0159095	0. 0151116	37
38	0. 0197161	0. 0187499	0. 0178206	0. 0169275		0. 0152476	0. 0144593	38
39	0. 0190546	0. 0180940	0. 0171711	0. 0162854		0. 0146226	0. 0138439	39
40	0. 0184271	0. 0174721	0. 0165558	0. 0156774		0. 0140315	0. 0132624	40
41	0. 0178311	0. 0168817	0. 0159719	0. 0151009	0. 0142679	0. 0134720	$\begin{array}{c} 0.0127124 \\ 0.0121917 \\ 0.0116981 \\ 0.0112298 \\ 0.0107852 \end{array}$	41
42	0. 0172643	0. 0163206	0. 0154173	0. 014536	0. 0137288	0. 0129418		42
43	0. 0167247	0. 0157867	0. 0148899	0. 0140336	0. 0132169	0. 0124387		43
44	0. 0162104	0. 0152781	0. 0143879	0. 0135390	0. 0127304	0. 0119610		44
45	0. 0157198	0. 0147932	0. 0139096	0. 0130681	0. 0122675	0. 0115069		45
46	0. 0152512	0. 0143304	0. 0134534	0. 0126192	0. 0118268	0. 0110749	0. 0103625	46
47	0. 0148034	0. 0138884	0. 0130179	0. 0121911	0. 0114067	0. 0106636	0. 0099605	47
48	0. 0143750	0. 0134657	0. 0126018	0. 0117823	0. 0110060	0. 0102716	0. 0095778	48
49	0. 0139648	0. 0130612	0. 0122040	0. 0113918	0. 0106235	0. 0098977	0. 0092131	49
50	0. 0135717	0. 0126739	0. 0118232	0. 0110184	0. 0102581	0. 0095409	0. 0088655	50
51	0.0131947	0.0123027	0. 0114586	0.0106610	0.0099087	0.0092001	0.0085338	51
52	0.0128329	0.0119467	0. 0111091	0.0103188	0.0095745	0.0088744	0.0082172	52
53	0.0124854	0.0116049	0. 0107739	0.0099909	0.0092545	0.0085630	0.0079147	53
54	0.0121514	0.0112767	0. 0104523	0.0096765	0.0089480	0.0082649	0.0076256	54
55	0.0118302	0.0109613	0. 0101434	0.0093749	0.0086542	0.0079795	0.0073491	55
56	0. 0115211	0.0106580	0.0098466	0.0090853	0.0083724	0.0077061	0.0070845	56
57	0. 0112234	0.0103661	0.0095612	0.0088071	0.0081020	0.0074440	0.0068311	57
58	0. 0109366	0.0100850	0.0092867	0.0085398	0.0078424	0.0071927	0.0065885	58
59	0. 0106601	0.0098143	0.0090224	0.0082827	0.0075931	0.0069515	0.0063559	59
60	0. 0103934	0.0095534	0.0087680	0.0080353	0.0073534	0.0067200	0.0061330	60

Table 33.—The annual sinking fund which will accumulate to 1 at the end of n years—Continued.

$$\frac{1}{s\overline{n}} = \frac{i}{(1+i)^n - 1}$$

Years.	3½%.	4%.	4½%.	5%.	5½%.	6%.	7%.	Year
1	1. 0000000	1. 0000000	1. 0000000	1. 0000000	1.0000000	1. 0000000	1. 0000000	1
2	0. 4914005	0. 4901961	0. 4889976	0. 4878049	0.4866180	0. 4854369	0. 4830918	2
3	0. 3219342	0. 3203485	0. 3187734	0. 3172086	0.3156541	0. 3141098	0. 3110517	3
4	0. 2372511	0. 2354901	0. 2337437	0. 2320118	0.2302945	0. 2285915	0. 2252281	4
5	0. 1864814	0. 1846271	0. 1827916	0. 1809748	0.1791764	0. 1773964	0. 1738907	5
6 7 8 9	0. 1526682 0. 1285445 0. 1104767 0. 0964460 0. 0852414	0. 1507619 0. 1266096 0. 1085278 0. 0944930 0. 0832909	0. 1488784 0. 1247015 0. 1066097 0. 0925745 0. 0813788	0. 1470175 0. 1228198 0. 1047218 0. 0906901 0. 0795046	0. 1451790 0. 1209644 0. 1028640 0. 0888395 0. 0776678	0. 1433626 0. 1191350 0. 1010359 0. 0870222 0. 0758680	0. 1397958 0. 1155532 0. 0974678 0. 0834865 0. 0723775	6 7 8 9 10
11	0. 0760920	0. 0741490	0. 0722482	0. 0703889	0.0685707	0.0667929	0.0633569	11
12	0. 0684840	0. 0665522	0. 0646662	0. 0628254	0.0610292	0.0592770	0.0559020	12
13	0. 0620616	0. 0601437	0. 0582754	0. 0564558	0.0546843	0.0529601	0.0496509	13
14	0. 0565707	0. 0546690	0. 0528203	0. 0510240	0.0492791	0.0475849	0.0443449	14
15	0. 0518251	0. 0499411	0. 0481138	0. 0463423	0.0446256	0.0429628	0.0397946	15
16	0. 0476848	0.0458200	0. 0440154	0. 0422699	0. 0405825	0. 0389521	0. 0358577	16
17	0. 0440431	0.0421985	0. 0404176	0. 0386991	0. 0370420	0. 0354448	0. 0324252	17
18	0. 0408168	0.0389933	0. 0372369	0. 0355462	0. 0339199	0. 0323565	0. 0294126	18
19	0. 0379403	0.0361386	0. 0344073	0. 0327450	0. 0311501	0. 0296209	0. 0267530	19
20	0. 0353611	0.0335818	0. 0318761	0. 0302426	0. 0286793	0. 0271846	0. 0243929	20
21	0. 0330366	0. 0312801	0. 0296006	0. 0279961	0. 0264648	0. 0250046	0.0222890	21
22	0. 0309321	0. 0291988	0. 0275457	0. 0259705	0. 0244712	0. 0230456	0.0204058	22
23	0. 0290188	0. 0273091	0. 0256825	0. 0241368	0. 0226696	0. 0212785	0.0187139	23
24	0. 0272728	0. 0255868	0. 0239870	0. 0224709	0. 0210358	0. 0196790	0.0171890	24
25	0. 0256740	0. 0240120	0. 0224390	0. 0209525	0. 0195494	0. 0182267	0.0158105	25
26 27 28 29 30	0. 0242054 0. 0228524 0. 0216027 0. 0204454 0. 0193713	0. 0225674 0. 0212385 0. 0200130 0. 0188799 0. 0178301	0. 0210214 0. 0197195 0. 0185208 0. 0174146 0. 0163915	0. 0195643 0. 0182919 0. 0171225 0. 0160455 0. 0150514	0. 0181931 0. 0169523 0. 0158144 0. 0147686 0. 0138054	0. 0169044 0. 0156972 0. 0145926 0. 0135796 0. 0126489	0. 0145610 0. 0134257 0. 0123919 0. 0114487 0. 0105864	26 27 28 28 29 30
31	0. 0183724	0. 0168554	0. 0154435	0. 0141321	0. 0129167	0. 0117922	0.0097969	31 32 33
32	0. 0174415	0. 0159486	0. 0145632	0. 0132804	0. 0120952	0. 0110023	0.0090729	
33	0. 0165724	0. 0151036	0. 0137445	0. 0124900	0. 0113347	0. 0102729	0.0084081	
34	0. 0157597	0. 0143148	0. 0129819	0. 0117554	0. 0106296	0. 0095984	0.0077967	
35	0. 0149984	0. 0135773	0. 0122705	0. 0110717	0. 0099749	0. 0089739	0.0072340	
36	0. 0142842	0. 0128869	0. 0116058	0. 0104345	0.0093664	0.0083948	0.0067153	36
37	0. 0136133	0. 0122396	0. 0109840	0. 0098398	0.0087999	0.0078574	0.0062369	
38	0. 0129821	0. 0116319	0. 0104017	0. 0092842	0:0082722	0.0073581	0.0057951	
39	0. 0123878	0. 0110608	0. 0098557	0. 0087646	0.0077799	0.0068938	0.0053868	
40	0. 0118273	0. 0105235	0. 0093432	0. 0082782	0.0073203	0.0064615	0.0050091	
41 42 43 44 45	0. 0112982 0. 0107983 0. 0103254 0. 0098777 0. 0094534	0. 0100174 0. 0095402 0. 0090899 0. 0086645 0. 0082625	0.0088616 0.0084087 0.0079824 0.0075807 0.0072020	0.0078223 0.0073947 0.0069933 0.0066163 0.0062617	0.0068909 0.0064893 0.0061134 0.0057613 0.0054313	0.0060589 0.0056834 0.0053331 0.0050061 0.0047005	0.0046596 0.0043359 0.0040359 0.0037577 0.0034996	41 42 43 44 44 44
46	0. 0090511	0.0078821	0.0068447	0.0059282	0. 0051218	0.0044149	0.0032600	46
47	0. 0086692	0.0075219	0.0065073	0.0056142	0. 0048313	0.0041477	0.0030374	47
48	0. 0083065	0.0071807	0.0061886	0.0053184	0. 0045585	0.0038977	0.0028307	48
49	0. 0079617	0.0068571	0.0058872	0.0050397	0. 0043023	0.0036636	0.0026385	49
50	0. 0076337	0.0065502	0.0056022	0.0047767	0. 0040615	0.0034443	0.0024599	50
51	0.0073216	0.0062589	0.0053323	0.0045287	0.0038350	0. 0032388	0.0022937	51
52	0.0070243	0.0059821	0.0050768	0.0042945	0.0036219	0. 0030462	0.0021390	52
53	0.0067410	0.0057192	0.0048347	0.0040733	0.0034213	0. 0028655	0.0019951	53
54	0.0064709	0.0054691	0.0046052	0.0038644	0.0032325	0. 0026960	0.0018611	54
55	0.0062132	0.0052312	0.0043875	0.0036669	0.0030546	0. 0025370	0.0017363	55
56	0.0059673	0.0050049	0.0041811	0.0034801	0.0028870	0. 0023877	0.0016201	58
57	0.0057325	0.0047893	0.0039851	0.0033034	0.0027290	0. 0022474	0.0015118	
58	0.0055081	0.0045840	0.0037990	0.0031363	0.0025801	0. 0021157	0.0014109	
59	0.0052937	0.0043884	0.0036222	0.0029780	0.0024396	0. 0019920	0.0013169	
60	0.0050886	0.0042019	0.0034543	0.0028282	0.0023071	0. 0018757	0.0012292	

Table 34.—The present value of 1 due in n years.

$$v^n = (1+i)^{-n}$$
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Years.	1 ½%.	134%.	2%.	21/4%.	2½%.	23/4%.	3%.	Years
1	0. 9852217	0. 9828010	0. 9803922	0. 9779951	0. 9756098	0. 9732360	0. 9708738	1
2	0. 9706618	0. 9658978	0. 9611688	0. 9564744	0. 9518144	0. 9471883	0. 9425959	2
3	0. 9563170	0. 9492853	0. 9423223	0. 9354273	0. 9285994	0. 9218378	0. 9151417	3
4	0. 9421842	0. 9329585	0. 9238454	0. 9148434	0. 9059506	0. 8971657	0. 8884871	4
5	0. 9282603	0. 9169125	0. 9057308	0. 8947123	0. 8838543	0. 8731540	0. 8626088	5
6 7 8 9	0. 9145422 0. 9010268 0. 8877111 0. 8745922 0. 8616672	0. 9011425 0. 8856438 0. 8704116 0. 8554414 0. 8407286	0. 8879714 0. 8705602 0. 8534904 0. 8367553 0. 8203483	0. 8750243 0. 8557695 0. 8369384 0. 8185216 0. 8005101	0. 8622969 0. 8412652 0. 8207466 0. 8007284 0. 7811984	0. 8497849 0. 8270413 0. 8049064 0. 7833639 0. 7623979	0.8374843 0.8130915 0.7894092 0.7664167 0.7440939	6 7 8 9 10
11	0. 8489332	0. 8262689	0.8042630	0. 7828950	0. 7621448	0. 7419931	0.7224213	11
12	0. 8363874	0. 8120579	0.7884932	0. 7656675	0. 7435559	0. 7221344	0.7013799	12
13	9. 3240270	0. 7980913	0.7730325	0. 7488191	0. 7254204	0. 7028072	0.6809513	13
14	0. 8118493	0. 7843649	0.7578750	0. 7323414	0. 7077272	0. 6839973	0.6611178	14
15	0. 7998515	0. 7708746	0.7430147	0. 7162263	0. 6904656	0. 6656908	0.6418620	15
16	0.7880310	0.7576163	0.7284458	0. 7004658	0. 6736249	0. 6478742	0. 6231669	16
17	0.7763853	0.7445861	0.7141626	0. 6850521	0. 6571951	0. 6305345	0. 6050165	17
18	0.7649116	0.7317799	0.7001594	0. 6699776	0. 6411659	0. 6136589	0. 5873946	18
19	0.7536075	0.7191940	0.6864308	0. 6552348	0. 6255277	0. 5972350	0. 5702860	19
20	0.7424704	0.7068246	0.6729713	0. 6408165	0. 6102709	0. 5812506	0. 5536758	20
21	0. 7314980	0. 6946679	0. 6597758	0. 6267154	0.5953863	0. 5656940	0.5375493	21
22	0. 7206876	0. 6827203	0. 6468390	0. 6129246	0.5808647	0. 5505538	0.5218925	22
23	0. 7100371	0. 6709782	0. 6341559	0. 5994372	0.5666972	0. 5358187	0.5066918	23
24	0. 6995439	0. 6594380	0. 6217215	0. 5862467	0.5528754	0. 5214781	0.4919337	24
25	0. 6892058	0. 6480963	0. 6095309	0. 5733464	0.5393906	0. 5075213	0.4776056	25
26	0. 6790205	0. 6369497	0.5975793	0.5607300	0.5262347	0. 4939380	0.4636947	26
27	0. 6689857	0. 6259948	0.5858620	0.5483912	0.5133997	0. 4807182	0.4501891	27
28	0. 6590993	0. 6152283	0.5743746	0.5363239	0.5008778	0. 4678523	0.4370768	28
29	0. 6493589	0. 6046470	0.5631123	0.5245221	0.4886613	0. 4553307	0.4243464	29
30	0. 6397624	0. 5942476	0.5520709	0.5129801	0.4767427	0. 4431442	0.4119868	30
31	0.6303078	0.5840272	0.5412460	0.5016920	0.4651148	0. 4312839	0.3999872	31
32	0.6209929	0.5739825	0.5306333	0.4906523	0.4537706	0. 4197410	0.3883370	32
33	0.6118157	0.5641105	0.5202287	0.4798556	0.4427030	0. 4085071	0.3770263	33
34	0.6027741	0.5544084	0.5100282	0.4692964	0.4319053	0. 3975738	0.3660449	34
35	0.5938661	0.5448731	0.5000276	0.4589696	0.4213711	0. 3869331	0.3553834	35
36	0. 5850897	0.5355018	0.4902232	0.4488700	0.4110937	0. 3765773	0. 3450324	36
37	0. 5764431	0.5262917	0.4806109	0.4389927	0.4010671	0. 3664986	0. 3349829	37
38	0. 5679242	0.5172400	0.4711872	0.4293327	0.3912849	0. 3566896	0. 3252262	38
39	0. 5595313	0.5083440	0.4619482	0.4198853	0.3817414	0. 3471432	0. 3157536	39
40	0. 5512623	0.4996010	0.4528904	0.4106458	0.3724306	0. 3378522	0. 3065568	40
41	0.5431156	0. 4910083	0. 4440102	0.4016095	0.3633470	0. 3288100	0. 2976280	41
42	0.5350893	0. 4825635	0. 4353041	0.3927722	0.3544848	0. 3200097	0. 2889592	42
43	0.5271815	0. 4742639	0. 4267688	0.3841293	0.3458389	0. 3114450	0. 2805429	43
44	0.5193907	0. 4661070	0. 4184007	0.3756765	0.3374038	0. 3031094	0. 2723718	44
45	0.5117149	0. 4580904	0. 4101968	0.3674098	0.3291744	0. 2949970	0. 2644386	45
46	0.5041527	0.4502117	0. 4021537	0.3593250	0.3211458	0. 2871017	0. 2567365	46
47	0.4967021	0.4424685	0. 3942684	0.3514181	0.3133129	0. 2794177	0. 2492588	47
48	0.4893617	0.4348585	0. 3865376	0.3436852	0.3056712	0. 2719394	0. 2419988	48
49	0.4821298	0.4273793	0. 3789584	0.3361224	0.2982158	0. 2646612	0. 2349503	49
50	0.4750047	0.4200288	0. 3715279	0.3287261	0.2909422	0. 2575778	0. 2281071	50
51	0. 4679849	0.4128048	0.3642430	0.3214925	0. 2838461	0. 2506840	0. 2214632	51
52	0. 4610689	0.4057049	0.3571010	0.3144181	0. 2769230	0. 2439747	0. 2150128	52
53	0. 4542551	0.3987272	0.3500990	0.3074994	0. 2701688	0. 2374450	0. 2087503	53
54	0. 4475419	0.3918695	0.3432343	0.3007329	0. 2635793	0. 2310900	0. 2026702	54
55	0. 4409280	0.3851297	0.3365043	0.2941153	0. 2571505	0. 2249051	0. 1967672	55
56	0. 4344118	0. 3785059	0.3299061	0. 2876433	0. 2508786	0. 2188858	0. 1910361	56
57	0. 4279919	0. 3719959	0.3234374	0. 2813137	0. 2447596	0. 2130275	0. 1854719	57
58	0. 4216669	0. 3655980	0.3170955	0. 2751235	0. 2387898	0. 2073260	0. 1800698	58
59	0. 4154354	0. 3593100	0.3108779	0. 2690694	0. 2329657	0. 2017772	0. 1748251	59
60	0. 4092960	0. 3531303	0.3047823	0. 2631486	0. 2272836	0. 1963768	0. 1697331	60

Table 34.—The present value of 1 due in n years—Continued.

 $v'' = (1+i)^{-n}$.

Years.	3½%.	4%.	4½%.	5%.	5½%.	6%.	7%.	Years
1	0.9661836	0.9615385	0. 9569378	0.9523810	0.9478673	0.9433962	0. 9345794	1
2	0.9335107	0.9245562	0. 9157300	0.9070295	0.8984524	0.8899964	0. 8734387	2
3	0.9019427	0.8889964	0. 8762966	0.8638376	0.8516137	0.8396193	0. 8162979	3
4	0.8714422	0.8548042	0. 8385613	0.8227025	0.8072167	0.7920937	0. 7628952	4
5	0.8419732	0.8219271	0. 8024511	0.7835262	0.7651344	0.7472582	0. 7129862	5
6 7 8 9	0.8135006 0.7859910 0.7594116 0.7337310 0.7089188	0. 7903145 0. 7599178 0. 7306902 0. 7025867 0. 6755642	0.7678957 0.7348285 0.7031851 0.6729044 0.6439277	0.7462154 0.7106813 0.6768394 0.6446089 0.6139133	0. 7252458 0. 6874368 0. 6515989 0. 6176293 0. 5854306	0.7049605 0.6650571 0.6274124 0.5918985 0.5583948	0.6663422 0.6227497 0.5820091 0.5439337 0.5083493	6 7 8 9 10
11	0. 6849457	0. 6495809	0.6161987	0. 5846793	0.5549105	0.5267875	0. 4750928	11
12	0. 6617833	0. 6245971	0.5896639	0. 5568374	0.5259815	0.4969694	0. 4440120	12
13	0. 6394042	0. 6005741	0.5642716	0. 5303214	0.4985607	0.4688390	0. 4149645	13
14	0. 6177818	0. 5774751	0.5399729	0. 5050680	0.4725694	0.4423010	0. 3878172	14
15	0. 5968906	0. 5552645	0.5167204	0. 4810171	0.4479331	0.4172651	0. 3624460	15
16	0.5767059	0. 5339082	0. 4944693	0. 4581115	0. 4245811	0.3936463	0. 3387346	16
17	0.5572038	0. 5133733	0. 4731764	0. 4362967	0. 4024465	0.3713644	0. 3165744	17
18	0.5383611	0. 4936281	0. 4528004	0. 4155207	0. 3814659	0.3503438	0. 2958639	18
19	0.5201557	0. 4746424	0. 4333018	0. 3957340	0. 3615791	0.3305130	0. 2765083	19
20	0.5025659	0. 4563870	0. 4146429	0. 3768895	0. 3427290	0.3118047	0. 2584190	20
21	0. 4855709	0. 4388336	0.3967874	0.3589424	0.3248616	0. 2941554	0. 2415131	21
22	0. 4691506	0. 4219554	0.3797009	0.3418499	0.3079257	0. 2775051	0. 2257132	22
23	0. 4532856	0. 4057263	0.3633501	0.3255713	0.2918727	0. 2617973	0. 2109469	23
24	0. 4379571	0. 3901215	0.3477035	0.3100679	0.2766566	0. 2469786	0. 1971466	24
25	0. 4231470	0. 3751168	0.3327306	0.2953028	0.2622337	0. 2329986	0. 1842492	25
26	0.4088377	0.3606892	0.3184025	0. 2812407	0. 2485628	0. 2198100	0. 1721955	26
27	0.3950122	0.3468166	0.3046914	0. 2678483	0. 2356045	0. 2073680	0. 1609304	27
28	0.3816543	0.3334775	0.2915707	0. 2550936	0. 2233218	0. 1956301	0. 1504022	28
29	0.3687482	0.3206514	0.2790150	0. 2429463	0. 2116794	0. 1845567	0. 1405628	29
30	0.3562784	0.3083187	0.2670000	0. 2313775	0. 2006440	0. 1741101	0. 1313671	30
31	0. 3442304	0. 2964603	0. 2555024	0.2203595	0.1901839	0.1642548	0.1227730	31
32	0. 3325897	0. 2850579	0. 2444999	0.2098662	0.1802691	0.1549574	0.1147411	32
33	0. 3213427	0. 2740942	0. 2339712	0.1998725	0.1708712	0.1461862	0.1072347	33
34	0. 3104761	0. 2635521	0. 2238959	0.1903548	0.1619632	0.1379115	0.1002193	34
35	0. 2999769	0. 2534155	0. 2142544	0.1812903	0.1535196	0.1301052	0.0936629	35
36 37 38 39 40	0. 2898327 0. 2800316 0. 2705619 0. 2614125 0. 2525725	0. 2436687 0. 2342969 0. 2252854 0. 2166206 0. 2082890	0.2050282 0.1961992 0.1877504 0.1796655 0.1719287	$\begin{array}{c} 0.1726574 \\ 0.1644356 \\ 0.1566054 \\ 0.1491480 \\ 0.1420457 \end{array}$	0.1455162 0.1379301 0.1307394 0.1239236 0.1174631	$\begin{array}{c} 0.1227408 \\ 0.1157932 \\ 0.1092389 \\ 0.1030555 \\ 0.0972222 \end{array}$	0. 0875355 0. 0818088 0. 0764569 0. 0714550 0. 0667804	36 37 38 39 40
41	0. 2440314	0. 2002779	0. 1645251	0.1352816	0.1113395	0.0917191	0.0624116	41
42	0. 2357791	0. 1925749	0. 1574403	0.1288396	0.1055350	0.0865274	0.0583286	42
43	0. 2278059	0. 1851682	0. 1506605	0.1227044	0.1000332	0.0816296	0.0545127	43
44	0. 2201023	0. 1780464	0. 1441728	0.1168613	0.0948182	0.0770091	0.0509464	44
45	0. 2126592	0. 1711984	0. 1379644	0.1112965	0.0898751	0.0726501	0.0476135	45
46	0. 2054679	0. 1646139	0.1320233	$\begin{array}{c} 0.1059967 \\ 0.1009492 \\ 0.0961421 \\ 0.0915639 \\ 0.0872037 \end{array}$	0.0851897	0.0685378	0.0444986	46
47	0. 1985197	0. 1582826	0.1263381		0.0807485	0.0646583	0.0415875	47
48	0. 1918065	0. 1521948	0.1268977		0.0765389	0.0609984	0.0388668	48
49	0. 1853202	0. 1463411	0.1156916		0.0725487	0.0575457	0.0363241	49
50	0. 1790534	0. 1407126	0.1107097		0.0687665	0.0542884	0.0339478	50
51	0.1729984	0.1353006	0.1059423	0.0830512	0.0651815	0.0512154	0.0317269	51
52	0.1671482	0.1300967	0.1013801	0.0790964	0.0617834	0.0483165	0.0296513	52
53	0.1614959	0.1250930	0.0970145	0.0753299	0.0585625	0.0455816	0.0277115	53
54	0.1560347	0.1202817	0.0928368	0.0717427	0.0555095	0.0430015	0.0258986	54
55	0.1507581	0.1156555	0.0888391	0.0683264	0.0526156	0.0405674	0.0242043	55
56	0.1456600	0.1112072	0. 0850135	0.0650728	0.0498726	0. 0382712	0. 0226208	56
57	0.1407343	0.1069300	0. 0813526	0.0619741	0.0472726	0. 0361049	0. 0211410	57
58	0.1359752	0.1028173	0. 0778494	0.0590229	0.0448082	0. 0340612	0. 0197579	58
59	0.1313770	0.0988628	0. 0744970	0.0562123	0.0424722	0. 0321332	0. 0184653	59
60	0.1269343	0.0950604	0. 0712890	0.0535355	0.0402580	0. 0303143	0. 0172573	60

Table 35.—The present value of an annuity of 1 for n years.

$$a_{\overline{n}|} = \frac{1 - v^n}{i}.$$

Years.	1½%.	134%.	2%.	21/4%.	2½%	2¾%.	3%.	Years.
1	0. 9852217	0. 9828010	0. 9803922	0. 9779951	0. 9756098	0. 9732360	0. 9708738	1
2	1. 9558834	1. 9486988	1. 9415609	1. 9344696	1. 9274242	1. 9204243	1. 9134697	2
3	2. 9122004	2. 8979840	2. 8838833	2. 8698969	2. 8560236	2. 8422621	2. 8286114	3
4	3. 8543847	3. 8309425	3. 8077287	3. 7847402	3. 7619742	3. 7394279	3. 7170984	4
5	4. 7826450	4. 7478551	4. 7134595	4. 6794525	4. 6458285	4. 6125819	4. 5797072	5
6 7 8 9 10	5. 6971872 6. 5982140 7. 4859251 8. 3605173 9. 2221846	5. 6489976 6. 5346414 7. 4050530 8. 2604943 9. 1012229	5. 6014309 6. 4719911 7. 3254814 8. 1622367 8. 9825850	5. 5544768 6. 4102463 7. 2471846 8. 0657062 8. 8662164	5. 5081254 6. 3493906 7. 1701372 7. 9708655 8. 7520639	5, 4623668 6, 2894081 7, 0943144 7, 8776783 8, 6400762	5. 4171914 6. 2302830 7. 0196922 7. 7861089 8. 5302028	6 7 8 9
11	10. 0711178	9. 9274918	9. 7868481	9. 6491113	9.5142087	9. 3820693	9. 2526241	11
12	10. 9075052	10. 7395497	10. 5753412	10. 4147788	10.2577646	10. 1042037	9. 9540040	12
13	11. 7315322	11. 5376410	11. 3483738	11. 1635979	10.9831850	10. 8070109	10. 6349553	13
14	12. 5433815	12. 3220059	12. 1062488	11. 8959392	11.6909122	11. 4910081	11. 2960731	14
15	13. 3432330	13. 0928805	12. 8492635	12. 6121655	12.3813777	12. 1566989	11. 9379351	15
16	14. 1312641	13. 8504968	13. 5777093	13. 3126313	13. 0550027	12. 8045732	12.5611020	16
17	14. 9076493	14. 5950828	14. 2918719	13. 9976834	13. 7121977	13. 4351077	13.1661185	17
18	15. 6725609	15. 3268627	14. 9920313	14. 6676611	14. 3533636	14. 0487666	13.7535131	18
19	16. 4261684	16. 0460567	15. 6784620	15. 3228959	14. 9788913	14. 6460016	14.3237991	19
20	17. 1686388	16. 7528813	16. 3514333	15. 9637124	15. 5891623	15. 2272521	14.8774749	20
21	17. 9001367	17. 4475492	17. 0112092	16. 5904278	16. 1845486	15. 7929461	15. 4150241	21
22	18. 6208244	18. 1302695	17. 6580482	17. 2033523	16. 7654132	16. 3434999	15. 9369166	22
23	19. 3308615	18. 8012476	18. 2922041	17. 8027896	17. 3321105	16. 8793186	16. 4436084	23
24	20. 0304054	19. 4606857	18. 9139256	18. 3890362	17. 8849858	17. 4007967	16. 9355421	24
25	20. 7196112	20. 1087820	19. 5234565	18. 9623826	18. 4243764	17. 9083180	17. 4131477	25
26	21. 3986317	20. 7457317	20. 1210358	19. 5231126	18. 9506111	18. 4022559	17. 8768424	26
27	22. 0676175	21. 3717264	20. 7068978	20. 0715038	19. 4640109	18. 8829741	18. 3270315	27
28	22. 7267167	21. 9869547	21. 2812724	20. 6078276	19. 9648887	19. 3508264	18. 7641082	28
29	23. 3760756	22. 5916017	21. 8443847	21. 1323498	20. 4535499	19. 8061571	19. 1884546	29
30	24. 0158380	23. 1858493	22. 3964556	21. 6453299	20. 9302926	20. 2493013	19. 6004414	30
31	24. 6461458	23. 7698765	22. 9377015	22. 1470219	21. 3954074	20. 6805852	20, 0004285	31
32	25. 2671387	24. 3438590	23. 4683348	22. 6376742	21. 8491780	21. 1003262	20, 3887655	32
33	25. 8789544	24. 9079695	23. 9885636	23. 1175298	22. 2918809	21. 5088333	20, 7657918	33
34	26. 4817285	25. 4623779	24. 4985917	23. 5868262	22. 7237863	21. 9064071	21, 1318367	34
35	27. 0755946	26. 0072510	24. 9986193	24. 0457958	23. 1451573	22. 2933403	21, 4872201	35
36	27. 6606843	26. 5427528	25. 4888425	24. 4946658	23. 5562511	22. 6699175	21. 8322525	36
37	28. 2371274	27. 0690446	25. 9694534	24. 9336585	23. 9573181	23. 0364161	22. 1672354	37
38	28. 8050516	27. 5862846	26. 4406406	25. 3629912	24. 3486030	23. 3931057	22. 4924616	38
39	29. 3645829	28. 0946286	26. 9025888	25. 7828765	24. 7303444	23. 7402488	22. 8082151	39
40	29. 9158452	28. 5942296	27. 3554792	26. 1935222	25. 1027751	24. 0781011	23. 1147720	40
41	30. 4589608	29. 0852379	27. 7994895	26. 5951317	25. 4661220	24. 4069110	23. 4124000	41
42	30. 9940500	29. 5678014	28. 2347936	26. 9879039	25. 8206068	24. 7269207	23. 7013592	42
43	31. 5212316	30. 0420652	28. 6615623	27. 3720332	26. 1664457	25. 0383656	23. 9819021	43
44	32. 0406222	30. 5081722	29. 0799631	27. 7477097	26. 5038495	25. 3414751	24. 2542739	44
45	32. 5523372	30. 9662626	29. 4901599	28. 1151195	26. 8330239	25. 6364721	24. 5187125	45
46	33. 0564898	31. 4164743	29. 8923136	28. 4744445	27. 1541696	25. 9235738	24. 7754491	46
47	33. 5531920	31. 8589428	30. 2865820	28. 8258626	27. 4674826	26. 2029915	25. 0247078	47
48	34. 0425537	32. 2938013	30. 6731196	29. 1695478	27. 7731537	26. 4749309	25. 2667066	48
49	34. 5246834	32. 7211806	31. 0520780	29. 5056702	28. 0713695	26. 7395922	25. 5016569	49
50	34. 9996881	33. 1412095	31. 4236059	29. 8343963	28. 3623117	26. 9971700	25. 7297640	50
51	35. 4676730	33. 5540142	31. 7878489	30. 1558888	28. 6461577	27. 2478540	25. 9512272	51
52	35. 9287419	33. 9597191	32. 1449499	30. 4703069	28. 9230807	27. 4918287	26. 1662400	52
53	36. 3829969	34. 3584463	32. 4950489	30. 7778062	29. 1932495	27. 7292737	26. 3749903	53
54	36. 8305388	34. 7503158	32. 8382833	31. 0785391	29. 4568288	27. 9603637	26. 5776605	54
55	37. 2714668	35. 1354455	33. 1747875	31. 3726544	29. 7139793	28. 1852688	26. 7744276	55
56	37. 7058786	35. 5139514	33. 5046937	31. 6602977	29. 9648578	28. 4041545	26. 9654637	56
57	38. 1338706	35. 8859473	33. 8281310	31. 9416114	30. 2096174	28. 6171820	27. 1509357	57
58	38. 5555375	36. 2515452	34. 1452265	32. 2167349	30. 4484072	28. 8245081	27. 3310055	58
59	38. 9709729	36. 6108553	34. 4561044	32. 4858043	30. 6813729	29. 0262852	27. 5058306	59
60	39. 3802689	36. 9639855	34. 7608867	32. 7489529	30. 9086565	29. 2226620	27. 6755637	60

Table 35.—The present value of an annuity of 1 for n years—Continued.

$$a_{\widetilde{n}} = \frac{1 - v^n}{i}$$

Years.	3½%.	4%.	4½%.	5%.	5½%.	6%.	7%.	Years.
1	0.9661836	0.9615385	0, 9569378	0. 9523810	0. 9478673	0. 9433962	0. 9345794	1
2	1.8996943	1.8860947	1, 8726678	1. 8594104	1. 8463197	1. 8333927	1. 8080182	2
3	2.8016370	2.7750910	2, 7489644	2. 7232480	2. 6979334	2. 6730120	2. 6243160	3
4	3.6730792	3.6298952	3, 5875257	3. 5459505	3. 5051501	3. 4651056	3. 3872113	4
5	4.5150524	4.4518223	4, 3899767	4. 3294767	4. 2702845	4. 2123638	4. 1001974	5
6	5, 3285530	5, 2421369	5. 1578725	5. 07569 3	4. 9955303	4, 9173243	4.7665397	6
7	6, 1145440	6, 0020547	5. 8927009	5. 7863731	5. 6829671	5, 5823814	5.3892894	7
8	6, 8739555	6, 7327449	6. 5958861	6. 4632128	6. 3345660	6, 2097938	5.9712985	8
9	7, 6076865	7, 4353316	7. 2687905	7. 1078217	6. 9521953	6, 8016923	6.5152323	9
10	8, 3166053	8, 1108958	7. 9127182	7. 7217349	7. 5376258	7, 3600871	7.0235816	10
11	9,0015510	8. 7604767	8. 5289169	8. 3064142	8. 0925363	7. 8868746	7. 4986744	11
12	9,6633343	9. 3850738	9. 1185808	8. 8632516	8. 6185179	8. 3838439	7. 9426863	12
13	10,3027385	9. 9856479	9. 6828524	9. 3935730	9. 1170785	8. 8526830	8. 3576508	13
14	10,9205203	10. 5631229	10. 2228253	9. 8986409	9. 5896479	9. 2949839	8. 7454680	14
15	11,5174109	11. 1183874	10. 7395457	10. 3796580	10. 0375809	9. 7122490	9. 1079140	15
16	12. 0941168	11, 6522956	11, 2340151	10. 8377696	10, 4621620	10, 1058953	9, 4466486	16
17	12. 6513206	12, 1656689	11, 7071914	11. 2740663	10, 8646086	10, 4772597	9, 7632230	17
18	13. 1896817	12, 6592970	12, 1599918	11. 6895869	11, 2460745	10, 8276035	10, 0590869	18
19	13. 7098374	13, 1339394	12, 5932936	12. 0853209	11, 6076535	11, 1581165	10, 3355953	19
20	14. 2124033	13, 5903263	13, 0079365	12. 4622103	11, 9503825	11, 4699212	10, 5940143	20
21	14, 6979742	14. 0291600	13, 4047239	12. 8211527	12. 2752441	11, 7640766	10, 8355273	21
22	15, 1671248	14. 4511153	13, 7844248	13. 1630026	12. 5831697	12, 0415817	11, 0612405	22
23	15, 6204105	14. 8568417	14, 1477749	13. 4885739	12. 8750424	12, 3033790	11, 2721874	23
24	16, 0583676	15. 2469631	14, 4954784	13. 7986418	13. 1516990	12, 5503575	11, 4693340	24
25	16, 4815146	15. 6220799	14, 8282090	14. 0939446	13. 4139327	12, 7833562	11, 6535832	25
26	16. 8903523	15. 9827692	15. 1466115	14. 3751853	13. 6624954	13, 0031662	11. 8257787	26
27	17. 2853645	16. 3295858	15. 4513028	14. 6430336	13. 8980999	13, 2105341	11. 9867091	27
28	17. 6670189	16. 6630632	15. 7428735	14. 8981273	14. 1214217	13, 4061643	12. 1371113	28
29	18. 0357670	16. 9837146	16. 0218885	15. 1410736	14. 3331012	13, 5907210	12. 2776741	29
30	18. 3920454	17. 2920333	16. 2888885	15. 3724510	14. 5337452	13, 7648312	12. 4090412	30
31	18.7362758	17. 5884936	16.5443910	15. 5928105	14. 7239291	13. 9290860	12.5318142	31
32	19.0688655	17. 8735515	16.7888909	15. 8026767	14. 9041982	14. 0840434	12.646553	32
33	19.3902082	18. 1476457	17.0228621	16. 0025492	15. 0750694	14. 2302296	12.7537900	33
34	19.7006842	18. 4111978	17.2467580	16. 1929040	15. 2370326	14. 3681411	12.8540094	34
35	20.0006611	18. 6646132	17.4610124	16. 3741943	15. 3905522	14. 4982464	12.9476723	35
36	20, 2904938	18. 9082820	17, 6660406	16,5468517	15. 5360684	14. 6209871	13. 0352078	36
37	20, 5705254	19. 1425788	17, 8622398	16,7112873	15. 6739985	14. 7367803	13. 1170166	37
38	20, 8410874	19. 3678642	18, 0499902	16,8678927	15. 8047379	14. 8460192	13. 1934735	38
39	21, 1024999	19. 5844848	18, 2296557	17,0170407	15. 9286615	14. 9490747	13. 2649285	39
40	21, 3550723	19. 7927739	18, 4015844	17,1590864	16. 0461247	15. 0462969	13. 3317089	40
41	21, 5991037	19. 9930518	18. 5661095	17, 2943680	16, 1574642	15, 1380159	13. 3941204	41
42	21, 8348828	20. 1856267	18. 7235498	17, 4232076	16, 2629992	15, 2245433	13. 4524490	42
43	22, 0626887	20. 3707949	18. 8742103	17, 5459120	16, 3630324	15, 3061729	13. 5069617	43
44	22, 2827910	20. 5488413	19. 0183831	17, 6627733	16, 4578506	15, 3831820	13. 5579081	44
45	22, 4954503	20. 7200397	19. 1563474	17, 7740698	16, 5477257	15, 4558321	13. 6055216	45
46	22.7009181	20, 8846536	19. 2883707	17. 8800665	16, 6329154	15. 5243699	13, 6500202	46
47	22.8994378	21, 0429361	19. 4147088	17. 9810157	16, 7136639	15. 5890282	13, 6916077	47
48	23.0912443	21, 1951309	19. 5356065	18. 0771578	16, 7902027	15. 6500266	13, 7304744	48
49	23.2765645	21, 3414720	19. 6512981	18. 1687217	16, 8627514	15. 7075723	13, 7667986	49
50	23.4556179	21, 4821846	19. 7620078	18. 2559255	16, 9315179	15. 7618606	13, 8007463	50
51	23, 6286163	21. 6174852	19, 8679500	18. 3389766	16, 9966994	15, 8130761	13. 8324732	51
52	23, 7957645	21. 7475819	19, 9693302	18. 4180730	17, 0584829	15, 8613925	13. 8621245	52
53	23, 9572604	21. 8726749	20, 0663447	18. 4934028	17, 1170454	15, 9069741	13. 8898359	53
54	24, 1132951	21. 9929567	20, 1591815	18. 5651456	17, 1725549	15, 9499755	13. 9157345	54
55	24, 2640532	22. 1086122	20, 2480206	18. 6334720	17, 2251705	15, 9905430	13. 9399388	55
56	24. 4097133	22, 2198194	20. 3330340	18. 6985447	17. 2750431	16. 0288141	13, 9625596	56
57	24. 5504476	22, 3267494	20. 4143866	18. 7605188	17. 3223158	16. 0649190	13, 9837006	57
58	24. 6864228	22, 4295668	20. 4922360	18. 8195417	17. 3671239	16. 0989802	14, 0034585	58
59	24. 8177998	22, 5284296	20. 5667330	18. 8757540	17. 4095961	16. 1311134	14, 0219238	59
60	24. 9447341	22, 6234900	20. 6380220	18. 9292895	17. 4498542	16. 1614277	14, 0391812	60

 $\begin{array}{c} {\rm Table} \ 36. - The \ annuity \ for \ n \ years \ which \ 1 \ will \ buy \ or \ the \ annuity \ needed \ to \ discharge \\ a \ debt \ of \ 1 \ in \ n \ years \ with \ interest. \end{array}$

$$\frac{1}{a_{\overline{n}}} = \frac{i}{1 - v^n}$$

Years.	1½%.	1¾%.	2%.	21/4%.	2½%.	23/4%.	3%.	Years.
1	1. 0150000	1. 0175000	1. 0200000	1. 0225000	1. 0250000	1. 0275000	1. 0300000	1
2	0. 5112779	0. 5131630	0. 5150495	0. 5169376	0. 5188272	0. 5207183	0. 5226108	2
3	0. 3433830	0. 3450675	0. 3467547	0. 3484446	0. 3501372	0. 3518324	0. 3535304	3
4	0. 2594448	0. 2610324	0. 2626238	0. 2642189	0. 2658179	0. 2674206	0. 2690271	4
5	0. 2090893	0. 2106214	0. 2121584	0. 2137002	0. 2152469	0. 2167983	0. 2183546	5
6	0. 1755252	0. 1770226	0. 1785258	0. 1800350	0. 1815500	0. 1830708	0. 1845975	6
7	0. 1515562	0. 1530306	0. 1545120	0. 1560003	0. 1574954	0. 1589975	0. 1605064	7
8	0. 1335840	0. 1350429	0. 1365098	0. 1379846	0. 1394674	0. 1409580	0. 1424564	8
9	0. 1196098	0. 1210581	0. 1225154	0. 1239817	0. 1254569	0. 1269410	0. 1284339	9
10	0. 1084342	0. 1098754	0. 1113265	0. 1127877	0. 1142588	0. 1157397	0. 1172305	10
11	0. 0992938	0. 1007304	0. 1021779	0. 1036365	0. 1051060	0, 1065863	0. 1080775	11
12	0. 0916800	0. 0931138	0. 0945596	0. 0960174	0. 0974871	0, 0989687	0. 1004621	12
13	0. 0852404	0. 0866728	0. 0881184	0. 0895769	0. 0910483	0, 0925325	0. 0940295	13
14	0. 0797233	0. 0811556	0. 0826020	0. 0840623	0. 0855365	0, 0870246	0. 0885263	14
15	0. 0749444	0. 0763774	0. 0778255	0. 0792885	0. 0807665	0, 0822592	0. 0837666	15
16	0. 0707651	0. 0721996	0. 0736501	0. 0751166	0. 0765990	0. 0780971	0. 0796109	16
17	0. 0670797	0. 0685162	0. 0699698	0. 0714404	0. 0729278	0. 0744319	0. 0759525	17
18	0. 0638058	0. 0652449	0. 0667021	0. 0681772	0. 0696701	0. 0711806	0. 0727087	18
19	0. 0608785	0. 0623206	0. 0637818	0. 0652618	0. 0667606	0. 0682780	0. 0698139	19
20	0. 0582457	0. 0596912	0. 0611567	0. 0626421	0. 0641471	0. 0656717	0. 0672157	20
21	0. 0558655	0. 0573146	0. 0587848	0. 0602757	0. 0617873	0. 0633194	0. 0648718	21
22	0. 0537033	0. 0551564	0. 0566314	0. 0581282	0. 0596466	0. 0611864	0. 0627474	22
23	0. 0517308	0. 0531880	0. 0546681	0. 0561710	0. 0576964	0. 0592441	0. 0608139	23
24	0. 0499241	0. 0513857	0. 0528711	0. 0543802	0. 0559128	0. 0574686	0. 0590474	24
25	0. 0482635	0. 0497295	0. 0512204	0. 0527360	0. 0542759	0. 0558400	0. 0574279	25
26	0. 0467320	0. 0482027	0. 0496992	0. 0512213	0. 0527688	0. 0543412	0. 0559383	26
27	0. 0453153	0. 0467908	0. 0482931	0. 0498219	0. 0513769	0. 0529578	0. 0545642	27
28	0. 0440011	0. 0454815	0. 0469897	0. 0485253	0. 0500879	0. 0516774	0. 0532932	28
29	0. 0427788	0. 0442642	0. 0457784	0. 0473208	0. 0488913	0. 0504894	0. 0521147	29
30	0. 0416392	0. 0431298	0. 0446499	0. 0461993	0. 0477776	0. 0493844	0. 0510193	30
31	0. 0405743	0. 0420701	0. 0435963	0. 0451528	0. 0467390	0. 0483545	0. 0499989	31
32	0. 0395771	0. 0410781	0. 0426106	0. 0441742	0. 0457683	0. 0473926	0. 0490466	32
33	0. 0386414	0. 0401478	0. 0416865	0. 0432572	0. 0448594	0. 0464925	0. 0481561	33
34	0. 0377619	0. 0392736	0. 0408187	0. 0423966	0. 0440068	0. 0456488	0. 0473220	34
35	0. 0369336	0. 0384508	0. 0400022	0. 0415873	0. 0432056	0. 0448565	0. 0465393	35
36	0. 0361524	0. 0376751	0. 0392329	0. 0408252	0. 0424516	0. 0441113	0. 0458038	36
37	0. 0354144	0. 0369426	0. 0385068	0. 0401064	0. 0417409	0. 0434095	0. 0451116	37
38	0. 0347161	0. 0362499	0. 0378206	0. 0394275	0. 0410701	0. 0427476	0. 0444593	38
39	0. 0340546	0. 0355940	0. 0371711	0. 0387854	0. 0404362	0. 0421226	0. 0438439	39
40	0. 0334271	0. 0349721	0. 0365558	0. 0381774	0. 0398362	0. 0415315	0. 0432624	40
41	0. 0328311	0. 0343817	0. 0359719	0. 0376009	0. 0392679	0. 0409720	0. 0427124	41
42	0. 0322643	0. 0338206	0. 0354173	0. 0370536	0. 0387288	0. 0404418	0. 0421917	42
43	0. 0317247	0. 0332867	0. 0348899	0. 0365336	0. 0382169	0. 0399387	0. 0416981	43
44	0. 0312104	0. 0327781	0. 0343879	0. 0360390	0. 0377304	0. 0394610	0. 0412299	44
45	0. 0307198	0. 0322932	0. 0339096	0. 0355681	0. 0372675	0. 0390069	0. 0407852	45
46	0. 0302512	0. 0318304	0. 0334534	0. 0351192	0. 0368268	0. 0385749	0. 0403625	46
47	0. 0298034	0. 0313884	0. 0330179	0. 0346911	0. 0364067	0. 0381636	0. 0399605	47
48	0. 0293750	0. 0309657	0. 0326018	0. 0342823	0. 0360060	0. 0377716	0. 0395778	48
49	0. 0289648	0. 0305612	0. 0322040	0. 0338918	0. 0356235	0. 0373977	0. 0392131	49
50	0. 0285717	0. 0301739	0. 0318232	0. 0335184	0. 0352581	0. 0370409	0. 0388655	50
51	0. 0281947	0. 0298027	0. 0314586	0. 0331610	0. 0349087	0. 0367001	0. 0385338	51
52	0. 0278329	0. 0294466	0. 0311091	0. 0328188	0. 0345745	0. 0363744	0. 0382172	52
53	0. 0274854	0. 0291049	0. 0307739	0. 0324909	0. 0342545	0. 0360630	0. 0379147	53
54	0. 0271514	0. 0287767	0. 0304523	0. 0321765	0. 0339480	0. 0357649	0. 0376256	54
55	0. 0268302	0. 0284613	0. 0301434	0: 0318749	0. 0336542	0. 0354795	0. 0373491	55
56	0. 0265211	0. 0281580	0. 0298466	0. 0315853	0. 0333724	0. 0352061	0. 0370845	56
57	0. 0262234	0. 0278661	0. 0295612	0. 0313071	0. 0331020	0. 0349440	0. 0368311	57
58	0. 0259366	0. 0275850	0. 0292867	0. 0310398	0. 0328424	0. 0346927	0. 0365885	58
59	0. 0256601	0. 0273143	0. 0290224	0. 0307827	0. 0325931	0. 0344515	0. 0363559	59
60	0. 0253934	0. 0270534	0. 0287680	0. 0305353	0. 0323534	0. 0342200	0. 0361330	60

Table 36.—The annuity for n years which 1 will buy or the annuity needed to discharge a debt of 1 in n years with interest—Continued.

$$\frac{1}{a_{\overline{n}}} = \frac{i}{1 - v^n}$$

Years.	3½%.	4%.	4½%.	5%.	5½%.	6%.	7%.	Years.
1	1.0350000	1.0400000	1. 0450000	1. 0500000	1. 0550000	1. 0600000	1. 0700000	1
2	0.5264005	0.5301961	0. 5339976	0. 5378049	0. 5416180	0. 5454369	0. 5530918	2
3	0.3569342	0.3603485	0. 3637734	0. 3672086	0. 3706541	0. 3741098	0. 3810517	3
4	0.2722511	0.2754901	0. 2787437	0. 2820118	0. 2852945	0. 2885915	0. 2952281	4
5	0.2214814	0.2246271	0. 2277916	0. 2309748	0. 2341764	0. 2373964	0. 2438907	5
6 7 8 9	0.1876682 0.1635445 0.1454767 0.1314460 0.1202414	0.1907619 0.1666096 0.1485278 0.1344930 0.1232909	0. 1938784 0. 1697015 0. 1516097 0. 1375745 0. 1263788	0. 1970175 0. 1728198 0. 1547218 0. 1406901 0. 1295046	0. 2001790 0. 1759644 0. 1578640 0. 1438395 0. 1326678	0.2033626 0.1791350 0.1610359 0.1470222 0.1358680	0. 2097958 0. 1855532 0. 1674678 0. 1534865 0. 1423775	6 7 8 9 10
11	0.1110920	0.1141490	0. 1172482	0. 1203889	0. 1235707	0.1267929	0.1333569	11
12	0.1034840	0.1065522	0. 1096662	0. 1128254	0. 1160292	0.1192770	0.1259020	12
13	0.0970616	0.1001437	0. 1032754	0. 1064558	0. 1096843	0.1129601	0.1196509	13
14	0.0915707	0.0946690	0. 0978203	0. 1010240	0. 1042791	0.1075849	0.1143449	14
15	0.0868251	0.0899411	0. 0931138	0. 0963423	0. 0996256	0.1029628	0.1097946	15
16	0. 0826848	0.0858200	0. 0890154	0. 0922699	0. 0955825	0.0989521	0.1058577	16
17	0. 0790431	0.0821985	0. 0854176	0. 0886999	0. 0920420	0.0954448	0.1024252	17
18	0. 0758168	0.0789933	0. 0822369	0. 0855462	0. 0889199	0.0923565	0.0994126	18
19	0. 0729403	0.0761386	0. 0794073	0. 0827450	0. 0861501	0.0896209	0.0967530	19
20	0. 0703611	0.0735818	0. 0768761	0. 0802426	0. 0836793	0.0871846	0.0943929	20
21	0.0680366	0.0712801	0.0746006	0.0779961	0. 0814648	0. 0850046 0. 0830456 0. 0812785 0. 0796790 0. 0782267	0.0922890	21
22	0.0659321	0.0691988	0.0725457	0.0759705	0. 0794712		0.0904058	22
23	0.0640188	0.0673091	0.0706825	0.0741368	0. 0776696		0.0887139	23
24	0.0622728	0.0655868	0.0689870	0.0724709	0. 0760358		0.0871890	24
25	0.0606740	0.0640120	0.0674390	0.0709525	0. 0745494		0.0858105	25
26	0. 0592054	0.0625674	0.0660214	0.0695643	0.0731931	0. 0769044	0. 0845610	26
27	0. 0578524	0.0612385	0.0647195	0.0682919	0.0719523	0. 0756972	0. 0834257	27
28	0. 0566027	0.0600130	0.0635208	0.0671225	0.0708144	0. 0745926	0. 0823919	28
29	0. 0554454	0.0588799	0.0624146	0.0660455	0.0697686	0. 0735796	0. 0814487	29
30	0. 0543713	0.0578301	0.0613915	0.0650514	0.0688054	0. 0726489	0. 0805864	30
31	0.0533724	0.0568554	0.0604435	0.0641321	0.0679167 0.0670952 0.0663347 0.0656296 0.0649749	0.0717922	0.0797969	31
32	0.0524415	0.0559486	0.0595632	0.0632804		0.0710023	0.0790729	32
33	0.0515724	0.0551036	0.0587445	0.0624900		0.0702729	0.0784081	33
34	0.0507597	0.0543148	0.0579819	0.0617554		0.0695984	0.0777967	34
35	0.0499984	0.0535773	0.0572705	0.0610717		0.0689739	0.0772340	35
36	0.0492842	0.0528869	0. 0566058	0.0604345	0.0643664 0.0637999 0.0632722 0.0627799 0.0623203	0.0683948	0.0767153	36
37	0.0486133	0.0522396	0. 0559840	0.0598398		0.0678574	0.0762369	37
38	0.0479821	0.0516319	0. 0554017	0.0592842		0.0673581	0.0757951	38
39	0.0473878	0.0510608	0. 0548557	0.0587646		0.0668938	0.0753868	39
40	0.0468273	0.0505235	0. 0543432	0.0582782		0.0664615	0.0750091	40
41	0.0462982	0.0500174	0.0538616	0. 0578223	0.0618909	0.0660589	0. 0746596	41
42	0.0457983	0.0495402	0.0534087	0. 0573947	0.0614893	0.0656834	0. 0743359	42
43	0.0453254	0.0490899	0.0529824	0. 0569933	0.0611134	0.0653331	0. 0740359	43
44	0.0448777	0.0486645	0.0525807	0. 0566163	0.0607613	0.0650061	0. 0737577	44
45	0.0444534	0.0482625	0.0522020	0. 0562617	0.0604313	0.0647005	0. 0734996	45
46	0.0440511	0. 0478821	0.0518447	0.0559282	0.0601218	0.0644149	0.0732600	46
47	0.0436692	0. 0475219	0.0515073	0.0556142	0.0598313	0.0641477	0.0730374	47
48	0.0433065	0. 0471807	0.0511886	0.0553184	0.0595585	0.0638977	0.0728307	48
49	0.0429617	0. 0468571	0.0508872	0.0550397	0.0593023	0.0636636	0.0726385	49
50	0.0426337	0. 0465502	0.0506022	0.0547767	0.0590615	0.0634443	0.0724599	50
51	0.0423216	0. 0462589	0.0503323	0.0545287	0.0588350	0.0632388	0.0722937	51
52	0.0420243	0. 0459821	0.0500768	0.0542945	0.0586219	0.0630462	0.0721390	52
53	0.0417410	0. 0457192	0.0498347	0.0540733	0.0584213	0.0628655	0.0719951	53
54	0.0414709	0. 0454691	0.0496052	0.0538644	0.0582325	0.0626960	0.0718611	54
55	0.0412132	0. 0452312	0.0493875	0.0536669	0.0580546	0.0625370	0.0717363	55
56	0. 0409673	0. 0450049	0. 0491811	0.0534801	0.0578870	0.0623877	0.0716201	56
57	0. 0407325	0. 0447893	0. 0489851	0.0533034	0.0577290	0.0622474	0.0715118	57
58	0. 0405081	0. 0445840	0. 0487990	0.0531363	0.0575801	0.0621157	0.0714109	58
59	0. 0402937	0. 0443884	0. 0486222	0.0529780	0.0574396	0.0619920	0.0713169	59
60	0. 0400886	0. 0442019	0. 0484543	0.0528282	0.0573071	0.0618757	0.0712292	60

Table 37.—Bid on a bond for \$100 to realize a given net income, interest payable semiannually.

INTEREST 3½%.

Net income.	5 years.	10 years.	15 years.	20 years.	25 years.	30 years
3.00	102.31	104. 29	106.00	107.48	108.75	109.85
3.10	101.84	103.42	104.77	105. 93	106.92	107. 78
3. 20 3. 30	101.38	102.55	103.55	104.41	105.14	107. 78 105. 76
3.40	100. 91 100. 46	101. 69 100. 84	102.35 101.17	102. 91 101. 44	103.39 101.68	103.79 101.87
3.50	100.00	100.00	100.00	100.00	100.00	100.00
3.60	99.55	99.17	98, 85	98, 58	98.36	98.17
3. 70 3. 80	99.09	98.34 97.52	97. 71 96. 59	97. 19 95. 82	96. 76 95. 19	96, 39 94, 66
3.90	98. 20	96.71	95.49	94, 48	93.65	92.96
4.00	97.75 97.31	95. 91	94.40	93.16	92.14	91.31
4. 10 4. 20	96.87	95.12 94.33	93. 33 92. 27	91.86	90. 67 89. 23	89. 70 88. 12
4.30	96.44	93. 55	91.22	89.34	87.82	86.59
4.40	96.00	92.78	90.19	88.11	86.44	85, 09
4.50 4.60	95. 57 95. 14	92. 02 91. 26	89. 18 88. 18	86. 90 85. 72	85. 08 83. 76	83, 63 82, 20
4.70	94.71	90.51	87.19	84. 55	82.46	80.80
4.80 4.90	94. 28 93. 86	89.77 89.04	86. 21 85. 25	83. 40 82. 28	81. 19 79. 95	79. 44 78. 12
5.00	93. 44	88. 31	84.30	81.17	78. 73	76.82
		INT	TEREST	1 %.	I	l
3.00	104.61	108.58	112.01	114.96	117. 50	119.69
3.10	104 14	107. 69 106. 80 105. 92 105. 05	110.73	113.34	115.58	117.50
3. 20 3. 30	103. 67 103. 20	105, 80	109. 47 108. 23 107. 00	111.75 110.19	113. 70 111. 85	115. 35 113. 27
3. 40	102.74	105. 05	107.00	108.66	110.05	111. 23
3.50	102. 28 101. 82 101. 36	104. 19 103. 33 102. 49 101. 65 100. 82	105. 80	107. 15	108. 29	109. 24 107. 30 105. 41
3. 60 3. 70	101.82	103. 33	104.60 103.43	105. 67 104. 21	106, 56 104, 87	107.30
3. 70 3. 80	100.90	101.65	103. 43 102. 27 101. 13	104. 21 102. 78 101. 38	103. 21 101. 59	103. 56 101. 76
3. 90 4. 00	100. 45 100. 00	100. 82	101.13	101.38	101. 59	100.00
4.10	99. 55	99, 19	98. 89	98. 64	98.45	98. 28
4. 10 4. 20 4. 30	99.11 98.66	98.38	98. 89 97. 79 96. 71	98. 64 97. 31 96. 00	98. 45 96. 92	96.61 94.97
4. 40	98. 22	98.38 97.58 96.79	95.64	94.72	95. 43 93. 97	93.37
4.50	97.78	96.01	94. 59	93.45	92.54	91. 81 90. 29
4.60 4.70	97. 78 97. 35 96. 91	95, 23	93. 55	92. 21	91.14	90. 29
4. 60 4. 70 4. 80	96.48	95. 23 94. 47 93. 71 92. 95	92. 53 91. 52 90. 52	92. 21 90. 99 89. 79 88. 61	91. 14 89. 77 88. 42 87. 11	88. 80 87. 35
4. 90	96.05					85, 93
5, 00	95, 62	92. 21	89. 53	87.45	85, 82	84. 55
		INI	EREST 4	1½%.		
3.00	106. 92 106. 44	112.88	118.01	122. 44 120. 75	126. 25	129. 54
3. 10 3. 20 3. 30	105.96	111. 95	116. 69 115. 39 114. 11	119.09	124. 23 122, 26	124. 95
3.30	105. 49 105. 02	111. 96 111. 05 110. 15 109. 26	114.11 112.84	119. 09 117. 47 115. 87	120.32 118.43	127. 22 124. 95 122. 74 120. 59
3.40	105.02	109. 26	111.59	114.30	116. 57	118.48
3.60	104.08	108. 38 107. 50 106. 64	110 36	112, 75	114.75	116, 43
3. 70 3. 80	103. 62 103. 16 102. 70	106.64	109. 15 107. 95 106. 77	111. 24 109. 74	112. 98 111. 23	114. 42 112. 47 110. 56
3. 90	102.70	105. 78 104. 93	106. 77	108. 28	111. 23 109. 53	110.56
4.00	102, 25	104.09	105.60	106.84	107. 86	108.69
4. 10 4. 20	101.79 101.34	103. 25 102. 43	104. 45 103. 31	105. 42 104. 03	106. 22 104. 62	106. 87 105. 09
4.30	100.89	101.61	102.19	102.66	103.05	103.35
4. 40	100. 44	100.80	101.09	101.32	101.51	101.66
4.50 4.60	100.00 99.56	100.00 99.21	100.00 98.93	100.00 98.70	100.00 98.52	100.00 98.38
4.70	99.12	98. 42	97. 86	97.43	97. 08	96. 80
	98. 68	97.64	96. 82 95. 79	96.17 94.94	95. 66 94. 27	95. 26 93. 75
4, 80	1 9x 25					
4. 80 4. 90 5. 00	98, 25 97, 81	96. 87 96. 10	94. 77	93.72	92. 91	92. 27

Table 37.—Bid on a bond for \$100 to realize a given net income, interest payable semiannually—Continued.

INTEREST 5%.

Net income.	5 years.	10 years.	15 years.	20 years.	25 years.	30 years.
3, 00	109. 22	117. 17	124. 02	129. 92	135. 00	139. 38
3, 10	108. 74	116. 23	122. 65	128. 16	132. 89	136. 93
3, 20	108. 26	115. 30	121. 31	126. 44	130. 81	134. 55
3, 30	107. 78	114. 38	119. 99	124. 75	128. 79	132. 22
3, 40	107. 30	113. 47	118. 68	123. 08	126. 80	129. 94
3.50	106. 83	112. 56	117. 39	121. 45	124. 86	127. 72
3.60	106. 35	111. 67	116. 12	119. 84	122. 95	125. 55
3.70	105. 88	110. 78	114. 86	118. 26	121. 08	123. 44
3.80	105. 42	109. 91	113. 62	116. 70	119. 26	121. 37
3.90	104. 95	109. 04	112. 40	115. 18	117. 47	119. 35
4.00	104. 49	108. 18	111. 20	113. 68	115. 71	117. 38
4.10	104. 03	107. 32	110. 01	112. 20	113. 99	115. 45
4.20	103. 57	106. 48	108. 84	110. 75	112. 31	113. 57
4.30	103. 12	105. 64	107. 68	109. 33	110. 66	111. 74
4.40	102. 67	104. 81	106. 54	107. 93	109. 04	109. 94
4. 50	102. 22	103. 99	105. 41	106. 55	107. 46	108. 19
4. 60	101. 77	103. 18	104. 30	105. 19	105. 91	106. 47
4. 70	101. 32	102. 37	103. 20	103. 86	104. 38	104. 80
4. 80	100. 88	101. 57	102. 12	102. 55	102. 89	103. 16
4. 90	100. 44	100. 78	101. 05	101. 27	101. 43	101. 56
5, 00	100.00	100.00	100.00	100.00	100.00	100.00
	·	INT	EREST 6	%.		
3. 50	111. 38	120. 94	128. 98	135. 74	141. 43	146. 20
3. 60	110. 89	120. 01	127. 63	134. 01	139. 34	143. 81
3. 70	110. 41	119. 08	126. 30	132. 30	137. 30	141. 47
3. 80	109. 93	118. 16	124. 98	130. 63	135. 30	139. 18
3. 90	109. 46	117. 25	123. 68	128. 98	133. 34	136. 94
4.00	108. 98	116. 35	122. 40	127. 36	131, 42	134. 76
4.10	108. 51	115. 46	121. 13	125. 76	129, 54	132. 63
4.20	108. 04	114. 58	119. 88	124. 19	127, 70	130. 54
4.30	107. 58	113. 70	118. 65	122. 65	125, 89	128. 50
4.40	107. 11	112. 83	117. 43	121. 14	124, 11	126. 51
4.50	106. 65	111. 97	116. 23	119. 65	122. 38	124. 56
4.60	106. 19	111. 12	115. 05	118. 18	120. 67	122. 66
4.70	105. 73	110. 28	113. 88	116. 74	119. 00	120. 80
4.80	105. 28	109. 44	112. 73	115. 32	117. 36	118. 98
4.90	104. 83	108. 61	111. 59	113. 92	115. 76	117. 20
5. 00	104, 38	107. 79	110. 47	112. 55	114. 18	115. 45
5. 25	103, 26	105. 78	107. 72	109. 22	110. 38	111. 27
5. 50	102, 16	103. 81	105. 06	106. 02	106. 75	107. 31
5. 75	101, 07	101. 88	102. 49	102. 95	103. 29	103. 55
6. 00	100, 00	100. 00	100. 00	100. 00	100. 00	100. 00

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